

# Package ‘ordinalTables’

September 18, 2025

**Type** Package

**Title** Fit Models to Two-Way Tables with Correlated Ordered Response Categories

**Version** 1.0.0.3

**Description** Fit a variety of models to two-way tables with ordered categories.

Most of the models are appropriate to apply to tables of that have correlated ordered response categories. There is a particular interest in rater data and models for rescore tables. Some utility functions (e.g., Cohen's kappa and weighted kappa) support more general work on rater agreement.

Because the names of the models are very similar, the functions that implement them are organized by last name of the primary author of the article or book that suggested the model, with the name of the function beginning with that author's name and an underscore. This may make some models more difficult to locate if one doesn't have the original sources. The vignettes and tests can help to locate models of interest. For more details see the following references:

- Agresti, A. (1983) <[doi:10.1016/0167-7152\(83\)90051-2](https://doi.org/10.1016/0167-7152(83)90051-2)> ``A Simple Diagonals-Parameter Symmetry And Quasi-Symmetry Model'',  
Agresti, A. (1983) <[doi:10.2307/2531022](https://doi.org/10.2307/2531022)> ``Testing Marginal Homogeneity for Ordinal Categorical Variables'',  
Agresti, A. (1988) <[doi:10.2307/2531866](https://doi.org/10.2307/2531866)> ``A Model For Agreement Between Ratings On An Ordinal Scale'',  
Agresti, A. (1989) <[doi:10.1016/0167-7152\(89\)90104-1](https://doi.org/10.1016/0167-7152(89)90104-1)> ``An Agreement Model With Kappa As Parameter'',  
Agresti, A. (2010 ISBN:978-0470082898) ``Analysis Of Ordinal Categorical Data'',  
Bhapkar, V. P. (1966) <[doi:10.1080/01621459.1966.10502021](https://doi.org/10.1080/01621459.1966.10502021)> ``A Note On The Equivalence Of Two Test Criteria For Hypotheses In Categorical Data'',  
Bhapkar, V. P. (1979) <[doi:10.2307/2530344](https://doi.org/10.2307/2530344)> ``On Tests Of Marginal Symmetry And Quasi-Symmetry In Two And Three-Dimensional Contingency Tables'',  
Bowker, A. H. (1948) <[doi:10.2307/2280710](https://doi.org/10.2307/2280710)> ``A Test For Symmetry In Contingency Tables'',  
Clayton, D. G. (1974) <[doi:10.2307/2335638](https://doi.org/10.2307/2335638)> ``Some Odds Ratio Statistics For The Analysis Of Ordered Categorical Data'',  
Cliff, N. (1993) <[doi:10.1037/0033-2909.114.3.494](https://doi.org/10.1037/0033-2909.114.3.494)> ``Dominance Statistics: Ordinal Analyses To Answer Ordinal Questions'',  
Cliff, N. (1996 ISBN:978-0805813333) ``Ordinal Methods For Behavioral Data Analysis'',  
Goodman, L. A. (1979) <[doi:10.1080/01621459.1979.10481650](https://doi.org/10.1080/01621459.1979.10481650)> ``Simple Models For The Analysis Of Association In Cross-Classifications Having Ordered Categories'',

Goodman, L. A. (1979) <[doi:10.2307/2335159](https://doi.org/10.2307/2335159)> ``Multiplicative Models For Square Contingency Tables With Ordered Categories'',  
 Ireland, C. T., Ku, H. H., & Kullback, S. (1969) <[doi:10.2307/2286071](https://doi.org/10.2307/2286071)> ``Symmetry And Marginal Homogeneity Of An  $r \times r$  Contingency Table'',  
 Ishi-kuntz, M. (1994 ISBN:978-0803943766) ``Ordinal Log-linear Models'',  
 McCullah, P. (1977) <[doi:10.2307/2345320](https://doi.org/10.2307/2345320)> ``A Logistic Model For Paired Comparisons With Ordered Categorical Data'',  
 McCullagh, P. (1978) <[doi:10.2307/2335224](https://doi.org/10.2307/2335224)> A Class Of Parametric Models For The Analysis Of Square Contingency Tables With Ordered Categories``,  
 McCullagh, P. (1980) <[doi:10.1111/j.2517-6161.1980.tb01109.x](https://doi.org/10.1111/j.2517-6161.1980.tb01109.x)> "Regression Models For Ordinal Data``,  
 Penn State: Eberly College of Science (undated) <<https://online.stat.psu.edu/stat504/lesson/11>> "Stat 504: Analysis of Discrete Data, 11. Advanced Topics I``,  
 Schuster, C. (2001) <[doi:10.3102/10769986026003331](https://doi.org/10.3102/10769986026003331)> "Kappa As A Parameter Of A Symmetry Model For Rater Agreement``,  
 Shoukri, M. M. (2004 ISBN:978-1584883210). "Measures Of Interobserver Agreement``,  
 Stuart, A. (1953) <[doi:10.2307/2333101](https://doi.org/10.2307/2333101)> "The Estimation Of And Comparison Of Strengths Of Association In Contingency Tables``,  
 Stuart, A. (1955) <[doi:10.2307/2333387](https://doi.org/10.2307/2333387)> "A Test For Homogeneity Of The Marginal Distributions In A Two-Way Classification``,  
 von Eye, A., & Mun, E. Y. (2005 ISBN:978-0805849677) "Analyzing Rater Agreement: Manifest Variable Methods".

**License** MIT + file LICENSE

**Encoding** UTF-8

**LazyData** true

**Imports** MASS

**RoxygenNote** 7.3.2

**Suggests** knitr, rmarkdown, testthat

**Config/testthat/edition** 3

**Depends** R (>= 3.5)

**VignetteBuilder** knitr

**NeedsCompilation** no

**Author** John R. Donoghue [aut, cre]

**Maintainer** John R. Donoghue <jdonoghue0823@gmail.com>

**Repository** CRAN

**Date/Publication** 2025-09-18 08:00:02 UTC

## Contents

Agresti_bisection	10
Agresti_compute_lambda	10
Agresti_compute_pi	11
Agresti_create_design_matrix	11

Agresti_equation_1 . . . . .	12
Agresti_equation_2 . . . . .	12
Agresti_equation_3 . . . . .	13
Agresti_extract_delta . . . . .	13
Agresti_f . . . . .	14
Agresti_kappa_agreement . . . . .	14
Agresti_simple_diagonals_parameter_quasi_symmetry . . . . .	15
Agresti_starting_values . . . . .	15
Agresti_weighted_tau . . . . .	16
Agresti_w_diff . . . . .	16
Bhapkar_marginal_homogeneity . . . . .	17
Bhapkar_quasi_symmetry . . . . .	17
Bowker_symmetry . . . . .	18
budget_actual . . . . .	18
budget_expected . . . . .	19
Clayton_marginal_location . . . . .	19
Clayton_stratified_marginal_location . . . . .	20
Clayton_summarize . . . . .	21
Clayton_summarize_stratified . . . . .	21
Clayton_two_way_association . . . . .	22
Cliff_as_d_matrix . . . . .	22
Cliff_compute_d . . . . .	23
Cliff_counts_2 . . . . .	23
Cliff_counts_3 . . . . .	24
Cliff_counts_4 . . . . .	24
Cliff_counts_5 . . . . .	25
Cliff_counts_6 . . . . .	25
Cliff_dependent . . . . .	26
Cliff_dependent_compute_cov . . . . .	26
Cliff_dependent_compute_cov_from_d . . . . .	27
Cliff_dependent_compute_from_matrix . . . . .	27
Cliff_dependent_compute_from_table . . . . .	28
Cliff_dependent_compute_paired_d . . . . .	29
Cliff_independent . . . . .	30
Cliff_independent_from_matrix . . . . .	30
Cliff_independent_from_table . . . . .	31
Cliff_independent_weighted . . . . .	31
Cliff_weighted_d_matrix . . . . .	32
coal_g . . . . .	32
constant_of_integration . . . . .	33
depression . . . . .	33
dogs . . . . .	34
dreams . . . . .	34
dumping . . . . .	35
esophageal_cancer . . . . .	35
expand . . . . .	36
expit . . . . .	36
family_income . . . . .	37

gender_vision . . . . .	37
Goodman_constrained_diagonals_parameter_symmetry . . . . .	38
Goodman_diagonals_parameter_symmetry . . . . .	38
Goodman_fixed_parameter . . . . .	39
Goodman_ml . . . . .	40
Goodman_model_i . . . . .	41
Goodman_model_ii . . . . .	42
Goodman_model_ii_star . . . . .	43
Goodman_model_i_star . . . . .	43
Goodman_null_association . . . . .	44
Goodman_pi . . . . .	45
Goodman_pi_matrix . . . . .	46
Goodman_symmetric_association_model . . . . .	46
Goodman_uniform_association . . . . .	47
handle_max_i_i . . . . .	47
handle_max_i_k . . . . .	48
handle_max_k_k2 . . . . .	49
handle_one_maximum . . . . .	49
handle_tied_below_maximum . . . . .	50
handle_tied_maximum . . . . .	50
handle_untied_below_maximum . . . . .	51
homicide_black_black . . . . .	52
homicide_black_white . . . . .	52
homicide_white_black . . . . .	53
homicide_white_white . . . . .	53
hypothalamus_1 . . . . .	54
hypothalamus_2 . . . . .	54
interference_12 . . . . .	55
interference_control_1 . . . . .	55
interference_control_2 . . . . .	56
Ireland_marginal_homogeneity . . . . .	56
Ireland_mdis . . . . .	57
Ireland_normalize_for_truncation . . . . .	57
Ireland_quasi_symmetry . . . . .	58
Ireland_quasi_symmetry_model . . . . .	58
Ireland_symmetry . . . . .	59
is_invertible . . . . .	60
is_missing_or_infinite . . . . .	60
kappa . . . . .	61
likelihood_ratio_chisq . . . . .	61
loadRData . . . . .	62
logit . . . . .	62
log_likelihood . . . . .	63
log_linear_add_all_diagonals . . . . .	63
log_linear_append_column . . . . .	64
log_linear_create_coefficient_names . . . . .	65
log_linear_create_linear_by_linear . . . . .	65
log_Linear_create_log_n . . . . .	66

log_linear_equal_weight_agreement_design . . . . .	66
log_linear_fit . . . . .	67
log_linear_main_effect_design . . . . .	68
log_linear_matrix_to_vector . . . . .	68
log_linear_quasi_symmetry_model_design . . . . .	69
log_linear_remove_column . . . . .	69
log_linear_symmetry_design . . . . .	70
McCullagh_compute_condition . . . . .	70
McCullagh_compute_cumulatives . . . . .	71
McCullagh_compute_cumulative_sums . . . . .	71
McCullagh_compute_c_plus . . . . .	72
McCullagh_compute_df . . . . .	72
McCullagh_compute_gamma . . . . .	73
McCullagh_compute_gamma_from_phi . . . . .	73
McCullagh_compute_gamma_plus_1_from_phi . . . . .	74
McCullagh_compute_generalized_cumulatives . . . . .	74
McCullagh_compute_generalized_pi . . . . .	75
McCullagh_compute_lambda . . . . .	75
McCullagh_compute_log_1 . . . . .	76
McCullagh_compute_Nij . . . . .	76
McCullagh_compute_omega . . . . .	77
McCullagh_compute_phi . . . . .	77
McCullagh_compute_phi_matrix . . . . .	78
McCullagh_compute_pi . . . . .	78
McCullagh_compute_pi_from_beta . . . . .	79
McCullagh_compute_pi_from_gamma . . . . .	79
McCullagh_compute_regression_weights . . . . .	80
McCullagh_compute_s_plus . . . . .	80
McCullagh_compute_update . . . . .	81
McCullagh_compute_z . . . . .	81
McCullagh_conditional_symmetry . . . . .	82
McCullagh_conditional_symmetry_compute_s . . . . .	82
McCullagh_conditional_symmetry_initialize_phi . . . . .	83
McCullagh_conditional_symmetry_maximize_phi . . . . .	83
McCullagh_conditional_symmetry_maximize_theta . . . . .	84
McCullagh_conditional_symmetry_pi . . . . .	84
McCullagh_derivative_condition_wrt_psi . . . . .	85
McCullagh_derivative_gamma_plus_1_wrt_phi . . . . .	85
McCullagh_derivative_gamma_wrt_phi . . . . .	86
McCullagh_derivative_gamma_wrt_y . . . . .	86
McCullagh_derivative_lagrangian_wrt_delta . . . . .	87
McCullagh_derivative_lagrangian_wrt_delta_vec . . . . .	87
McCullagh_derivative_lagrangian_wrt_psi . . . . .	88
McCullagh_derivative_log_1_wrt_alpha . . . . .	89
McCullagh_derivative_log_1_wrt_beta . . . . .	89
McCullagh_derivative_log_1_wrt_c . . . . .	90
McCullagh_derivative_log_1_wrt_delta . . . . .	90
McCullagh_derivative_log_1_wrt_delta_vec . . . . .	91

McCullagh_derivative_log_l_wrt_params . . . . .	92
McCullagh_derivative_log_l_wrt_phi . . . . .	92
McCullagh_derivative_log_l_wrt_psi . . . . .	93
McCullagh_derivative_omega_wrt_alpha . . . . .	93
McCullagh_derivative_omega_wrt_c . . . . .	94
McCullagh_derivative_omega_wrt_delta . . . . .	94
McCullagh_derivative_omega_wrt_delta_vec . . . . .	95
McCullagh_derivative_omega_wrt_psi . . . . .	95
McCullagh_derivative_phi_wrt_gamma . . . . .	96
McCullagh_derivative_pij_wrt_alpha . . . . .	96
McCullagh_derivative_pij_wrt_c . . . . .	97
McCullagh_derivative_pij_wrt_delta . . . . .	98
McCullagh_derivative_pij_wrt_delta_vec . . . . .	98
McCullagh_derivative_pij_wrt_psi . . . . .	99
McCullagh_derivative_pi_wrt_alpha . . . . .	99
McCullagh_derivative_pi_wrt_c . . . . .	100
McCullagh_derivative_pi_wrt_delta . . . . .	101
McCullagh_derivative_pi_wrt_delta_vec . . . . .	101
McCullagh_derivative_pi_wrt_psi . . . . .	102
McCullagh_extract_weights . . . . .	102
McCullagh_fit_location_regression_model . . . . .	103
McCullagh_generalized_palindromic_symmetry . . . . .	104
McCullagh_generalized_pij_qij . . . . .	105
McCullagh_generate_names . . . . .	105
McCullagh_get_statistics . . . . .	106
McCullagh_gradient_log_l . . . . .	106
McCullagh_hessian_log_l . . . . .	107
McCullagh_initialize_beta . . . . .	107
McCullagh_initialize_delta . . . . .	108
McCullagh_initialize_delta_vec . . . . .	108
McCullagh_initialize_psi . . . . .	109
McCullagh_initialize_x . . . . .	109
McCullagh_is_in_constraint_set . . . . .	110
McCullagh_is_pi_invalid . . . . .	110
McCullagh_logistic_model . . . . .	111
McCullagh_logits . . . . .	111
McCullagh_log_L . . . . .	112
McCullagh_maximize_q_symmetry . . . . .	112
McCullagh_newton_raphson_update . . . . .	113
McCullagh_palindromic_symmetry . . . . .	114
McCullagh_penalized . . . . .	114
McCullagh_pij_qij . . . . .	115
McCullagh_proportional_hazards . . . . .	116
McCullagh_quasi_symmetry . . . . .	116
McCullagh_q_symmetry_initialize_alpha . . . . .	117
McCullagh_q_symmetry_initialize_phi . . . . .	117
McCullagh_q_symmetry_pi . . . . .	118
McCullagh_second_order_lagrangian_wrt_psi_2 . . . . .	118

McCullagh_second_order_lagrangian_wrt_psi_alpha . . . . .	119
McCullagh_second_order_lagrangian_wrt_psi_delta . . . . .	120
McCullagh_second_order_lagrangian_wrt_psi_delta_vec . . . . .	121
McCullagh_second_order_log_1_wrt_alpha_2 . . . . .	122
McCullagh_second_order_log_1_wrt_alpha_c . . . . .	122
McCullagh_second_order_log_1_wrt_beta_2 . . . . .	123
McCullagh_second_order_log_1_wrt_c_2 . . . . .	124
McCullagh_second_order_log_1_wrt_delta_2 . . . . .	124
McCullagh_second_order_log_1_wrt_delta_alpha . . . . .	125
McCullagh_second_order_log_1_wrt_delta_c . . . . .	126
McCullagh_second_order_log_1_wrt_delta_vec_2 . . . . .	126
McCullagh_second_order_log_1_wrt_delta_vec_alpha . . . . .	127
McCullagh_second_order_log_1_wrt_delta_vec_c . . . . .	128
McCullagh_second_order_log_1_wrt_parms . . . . .	128
McCullagh_second_order_log_1_wrt_psi_2 . . . . .	129
McCullagh_second_order_log_1_wrt_psi_alpha . . . . .	130
McCullagh_second_order_log_1_wrt_psi_c . . . . .	131
McCullagh_second_order_log_1_wrt_psi_delta . . . . .	131
McCullagh_second_order_log_1_wrt_psi_delta_vec . . . . .	132
McCullagh_second_order_omega_wrt_alpha_2 . . . . .	133
McCullagh_second_order_omega_wrt_alpha_c . . . . .	133
McCullagh_second_order_omega_wrt_c_2 . . . . .	134
McCullagh_second_order_omega_wrt_delta_2 . . . . .	135
McCullagh_second_order_omega_wrt_delta_alpha . . . . .	135
McCullagh_second_order_omega_wrt_delta_c . . . . .	136
McCullagh_second_order_omega_wrt_delta_vec_2 . . . . .	137
McCullagh_second_order_omega_wrt_delta_vec_alpha . . . . .	137
McCullagh_second_order_omega_wrt_delta_vec_c . . . . .	138
McCullagh_second_order_omega_wrt_psi_2 . . . . .	139
McCullagh_second_order_omega_wrt_psi_alpha . . . . .	140
McCullagh_second_order_omega_wrt_psi_c . . . . .	141
McCullagh_second_order_omega_wrt_psi_delta . . . . .	141
McCullagh_second_order_omega_wrt_psi_delta_vec . . . . .	142
McCullagh_second_order_pi_wrt_alpha_2 . . . . .	143
McCullagh_second_order_pi_wrt_alpha_c . . . . .	144
McCullagh_second_order_pi_wrt_c_2 . . . . .	144
McCullagh_second_order_pi_wrt_delta_2 . . . . .	145
McCullagh_second_order_pi_wrt_delta_alpha . . . . .	145
McCullagh_second_order_pi_wrt_delta_c . . . . .	146
McCullagh_second_order_pi_wrt_delta_vec_2 . . . . .	147
McCullagh_second_order_pi_wrt_delta_vec_alpha . . . . .	148
McCullagh_second_order_pi_wrt_delta_vec_c . . . . .	149
McCullagh_second_order_pi_wrt_psi_2 . . . . .	149
McCullagh_second_order_pi_wrt_psi_alpha . . . . .	150
McCullagh_second_order_pi_wrt_psi_c . . . . .	151
McCullagh_second_order_pi_wrt_psi_delta . . . . .	152
McCullagh_second_order_pi_wrt_psi_delta_vec . . . . .	152
McCullagh_update_parameters . . . . .	153

McCullagh_v_inverse . . . . .	154
mental_health . . . . .	155
model_ii_effects . . . . .	155
model_ii_fHat . . . . .	156
model_ii_ksi . . . . .	156
model_ii_starting_values . . . . .	157
model_ii_star_effects . . . . .	157
model_ii_star_fHat . . . . .	158
model_ii_star_update_phi . . . . .	158
model_ii_update_alpha . . . . .	159
model_ii_update_beta . . . . .	159
model_ii_update_rho . . . . .	160
model_ii_update_sigma . . . . .	160
model_i_column_theta . . . . .	161
model_i_effects . . . . .	161
model_i_fHat . . . . .	162
model_i_normalize_fHat . . . . .	162
model_i_row_column_odds_ratios . . . . .	163
model_i_row_theta . . . . .	163
model_i_starting_values . . . . .	164
model_i_star_effects . . . . .	164
model_i_star_fHat . . . . .	165
model_i_star_update_theta . . . . .	165
model_i_update_alpha . . . . .	166
model_i_update_beta . . . . .	166
model_i_update_delta . . . . .	167
model_i_update_gamma . . . . .	167
model_i_zeta . . . . .	168
movies . . . . .	168
new_orleans_data . . . . .	169
null_association_fHat . . . . .	169
occupational_status . . . . .	170
paranoia . . . . .	170
pearson_chisq . . . . .	171
radiology . . . . .	171
Schuster_compute_df . . . . .	172
Schuster_compute_pi . . . . .	172
Schuster_compute_starting_values . . . . .	173
Schuster_derivative_log_l_wrt_kappa . . . . .	173
Schuster_derivative_log_l_wrt_marginal_pi . . . . .	174
Schuster_derivative_log_l_wrt_v . . . . .	174
Schuster_derivative_pi_wrt_kappa . . . . .	175
Schuster_derivative_pi_wrt_marginal_pi . . . . .	175
Schuster_derivative_pi_wrt_v . . . . .	176
Schuster_derivative_v_wrt_v . . . . .	177
Schuster_enforce_constraints_on_v . . . . .	177
Schuster_gradient . . . . .	178
Schuster_hessian . . . . .	178

Schuster_is_pi_valid . . . . .	179
Schuster_newton_raphson . . . . .	179
Schuster_second_deriv_log_l_wrt_kappa_2 . . . . .	180
Schuster_second_deriv_log_l_wrt_kappa_v . . . . .	180
Schuster_second_deriv_log_l_wrt_marginal_pi_2 . . . . .	181
Schuster_second_deriv_log_l_wrt_marginal_pi_kappa . . . . .	181
Schuster_second_deriv_log_l_wrt_marginal_pi_v . . . . .	182
Schuster_second_deriv_log_l_wrt_v_2 . . . . .	182
Schuster_second_deriv_pi_wrt_kappa_2 . . . . .	183
Schuster_second_deriv_pi_wrt_kappa_v . . . . .	183
Schuster_second_deriv_pi_wrt_marginal_pi_2 . . . . .	184
Schuster_second_deriv_pi_wrt_marginal_pi_kappa . . . . .	184
Schuster_second_deriv_pi_wrt_marginal_pi_v . . . . .	185
Schuster_second_deriv_pi_wrt_v_2 . . . . .	186
Schuster_solve_for_v . . . . .	187
Schuster_solve_for_v1 . . . . .	187
Schuster_symmetric_rater_agreement_model . . . . .	188
Schuster_update . . . . .	188
Schuster_v_tilde . . . . .	189
social_status . . . . .	189
social_status2 . . . . .	190
Stuart_marginal_homogeneity . . . . .	190
taste . . . . .	191
teachers . . . . .	191
teaching_style . . . . .	192
tonsils . . . . .	192
tv . . . . .	193
uniform_association_fHat . . . . .	193
uniform_association_update_theta . . . . .	194
var_kappa . . . . .	194
var_weighted_kappa . . . . .	195
vision_data . . . . .	195
vision_data_men . . . . .	196
von_Eye_diagonal . . . . .	196
von_Eye_diagonal_linear_by_linear . . . . .	197
von_Eye_equal_weighted_diagonal . . . . .	197
von_Eye_equal_weight_diagonal_linear . . . . .	198
von_Eye_linear_by_linear . . . . .	198
von_Eye_main_effect . . . . .	199
von_Eye_weight_by_response_category_design . . . . .	199
weighted_cov . . . . .	200
weighted_kappa . . . . .	201
weighted_var . . . . .	201
winnipeg_data . . . . .	202

**Agresti\_bisection**      *Solves equation Agresti\_f() = 0 for delta by method of bisection..*

### Description

Solves equation Agresti\_f() = 0 for delta by method of bisection..

### Usage

```
Agresti_bisection(p, pi_margin, x_low = 0, x_high = 1)
```

### Arguments

p	matrix of observed proportions
pi_margin	current value of (row and column) marginal proportion
x_low	lower bound for search. Default value is 0.0
x_high	upper bound for search. Default value is 1.0

### Value

value of kappa that makes the function 0.0

**Agresti\_compute\_lambda**

*Computes value of lambda parameter*

### Description

Computes value of lambda parameter

### Usage

```
Agresti_compute_lambda(p, pi)
```

### Arguments

p	matrix of observed proportions
pi	matrix of model-supplied proportions

### Value

value of the lambda parameter

`Agresti_compute_pi`      *Computes the matrix pi of model-based proportions*

### Description

Computes the matrix pi of model-based proportions

### Usage

```
Agresti_compute_pi(pi_margin, kappa)
```

### Arguments

<code>pi_margin</code>	current value of (row and column) marginal proportion
<code>kappa</code>	current estimate of kappa coefficient

### Value

matrix of model-based proportions

`Agresti_create_design_matrix`

*Creates the design matrix for Agresti's simple diagonal quasi-symmetry model.*

### Description

This parameterization does not match equation (2.2) in the paper, but it yields results that are identical to those in the paper. Agresti, A. (1983), A simple diagonals-parameter symmetry and quasi-symmetry model. Statistics and Probability Letters I, 313-316.

### Usage

```
Agresti_create_design_matrix(n_dim)
```

### Arguments

<code>n_dim</code>	the size of the date matrix
--------------------	-----------------------------

### Value

the design matrix for the model, that can bee used with `ml_for_log_linear`

Agresti\_equation\_1     *First equation in section 3. Solved for kappa.*

### Description

First equation in section 3. Solved for kappa.

### Usage

```
Agresti_equation_1(p, pi_margin, kappa)
```

### Arguments

p	matrix of observed proportions
pi_margin	current value of (row and column) marginal proportion
kappa	current value of coefficient kappa

Agresti\_equation\_2     *Second equation in section 3. Solved for pi\_margin.*

### Description

Second equation in section 3. Solved for pi\_margin.

### Usage

```
Agresti_equation_2(p, pi_margin, lambda, kappa)
```

### Arguments

p	matrix of observed proportions
pi_margin	current value of (row and column) marginal proportion
lambda	value of quantity lambda defined in third equation
kappa	current value of coefficient kappa

`Agresti_equation_3`     *Third equation in section 3. Solved for lambda*

### Description

Third equation in section 3. Solved for lambda

### Usage

```
Agresti_equation_3(p, pi_margin, kappa)
```

### Arguments

<code>p</code>	matrix of observed proportions
<code>pi_margin</code>	current value of (row and column) marginal proportion
<code>kappa</code>	current value of coefficient kappa

`Agresti_extract_delta` *Extracts the quasi-symmetry information from the result provided.*

### Description

Extracts the quasi-symmetry information from the result provided.

### Usage

```
Agresti_extract_delta(result)
```

### Arguments

<code>result</code>	result of call to <code>log_linear_fit()</code>
---------------------	---

### Value

list consisting of beta: the beta coefficient se: the standard error of beta z: the ratio beta / se delta: the delta coefficient =  $\exp(2.0 * \beta)$

**Agresti\_f***Function value for first equation in section 3.***Description**

Used by Agresti\_bisection()

**Usage**

```
Agresti_f(p, pi_margin, kappa)
```

**Arguments**

p	matrix of observed proportions
pi_margin	current value of (row and column) marginal proportion
kappa	current estimate of kappa coefficient

**Agresti\_kappa\_agreement***Fits Agresti's agreement model that includes kappa as a parameter.***Description**

Agresti, A. (1989). An agreement model with kappa as a parameter. Statistics and Probability Letters, 7, 271-273.

**Usage**

```
Agresti_kappa_agreement(n, verbose = FALSE)
```

**Arguments**

n	matrix of observed counts
verbose	should cycle-by-cycle info be printed as messages? The default is FALSE.

**Value**

a list containing kappa: value of kappa coefficient pi\_margin: value of marginal p-values. They apply to rows and columns chisq: Pearson X^2 df: degrees of freedom expected: fitted frequencies

**Agresti\_simple\_diagonals\_parameter\_quasi\_symmetry**  
*Agresti's simple diagonal quasi-symmetry model.*

### Description

This parameterization does not match equation (2.2) in the paper, but it yields results that are identical to those in the paper. Agresti, A. (1983), A simple diagonals-parameter symmetry and quasi-symmetry model. Statistics and Probability Letters I, 313-316.

### Usage

```
Agresti_simple_diagonals_parameter_quasi_symmetry(n)
```

### Arguments

n                   the matrix of observed counts

### Value

a list containing expected: matrix of expected cell frequencies, chisq: Pearson X^2 g\_squared: likelihood ratio G^2 df: degrees of freedom beta: the parameter estimated sigma\_beta: standard error of beta z: z-score for beta delta: transformation of the the parameter into the model formulation

### Examples

```
Agresti_simple_diagonals_parameter_quasi_symmetry(vision_data)
```

**Agresti\_starting\_values**  
*Computes staring values for marginal pi.*

### Description

Computes staring values for marginal pi.

### Usage

```
Agresti_starting_values(p)
```

### Arguments

p                   matrix of observed proportions

### Value

vector containing pi

---

**Agresti\_weighted\_tau**    *Computes weighted tau from Section 2.1. Agresti, A. (1983). Testing marginal homogeneity for ordinal categorical variables. Biometrics, 39(2), 505-510.*

---

**Description**

Computes weighted tau from Section 2.1. Agresti, A. (1983). Testing marginal homogeneity for ordinal categorical variables. Biometrics, 39(2), 505-510.

**Usage**

```
Agresti_weighted_tau(n)
```

**Arguments**

n                  matrix of observed counts

**Value**

a list containing tau: value of tau-d coefficient sigma\_tau: SE(tau) z\_tau: z-score for tau

---

**Agresti\_w\_diff**                  *Computes the weighted statistics listed in section 2.3.*

---

**Description**

Computes weighted contrast of the two margins. Agresti, A. (1983). Testing marginal homogeneity for ordinal categorical variables. Biometrics, 39(2), 505-510.

**Usage**

```
Agresti_w_diff(w, n)
```

**Arguments**

w                  a vector of weights to be treated as scores  
n                  matrix of observed counts

**Value**

a list containing diff: the weighted contrast computed using weights w sigma\_diff: SE(diff) z\_diff: z-score for diff

**Examples**

```
weights = c(-3.0, -1.0, 1.0, 3.0)
Agresti_w_diff(weights, vision_data)
```

**Bhapkar\_marginal\_homogeneity***Bhapkar's (1979) test for marginal homogeneity***Description**

Fits the marginal homogeneity model using WLS.

**Usage**

```
Bhapkar_marginal_homogeneity(n)
```

**Arguments**

n	matrix containing the table to analyze
---	--

**Details**

See: Bhapkar, V. P. (1966). A Note on the Equivalence of Two Test Criteria for Hypotheses in Categorical Data. *Journal of the American Statistical Association*, 61(313), pp.228-235.

**Value**

a list containing the chi-square statistic, the df and p-value.

**Examples**

```
Bhapkar_marginal_homogeneity(vision_data)
```

**Bhapkar\_quasi\_symmetry***Bhapkar's 1979 test for quasi-symmetry.***Description**

Fits the quasi-symmetry model using WLS. Bhapkar, V. P. (1979). On tests of marginal symmetry and quasi-symmetry in two and three-dimensional contingency tables. *Biometrics* 35(2), 417-426.

**Usage**

```
Bhapkar_quasi_symmetry(n)
```

**Arguments**

n	the matrix to be analyzed
---	---------------------------

**Value**

a list containing the chi-square and df.

**Examples**

```
Bhapkar_quasi_symmetry(vision_data)
```

Bowker_symmetry	<i>Computes Bowker's test of symmetry.</i>
-----------------	--

**Description**

Computes the test of table symmetry in Bowker (1948). Bowker, A. H. (1948). A test for symmetry in contingency tables. *Journal of the American Statistical Association* 43, 572-574.

**Usage**

```
Bowker_symmetry(n)
```

**Arguments**

n	the matrix to be tested for symmetry
---	--------------------------------------

**Value**

a list containing the chi-square: Pearson X^2 g\_square: likelihood ratio G^2 df: degrees of freedom p-value: p-value for Pearson X^2 expected: fitted values

**Examples**

```
Bowker_symmetry(vision_data)
```

budget_actual	<i>Participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly</i>
---------------	--

**Description**

Participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly

**Usage**

```
budget_actual
```

**Format**

```
## 'budget_actual' A matrix with 3 rows and 3 columns
```

**Source**

Schuster, C, (2001). Kappa as a parameter of a symmetry model for rater agreement. Journal of Educational and Behavioral Statistics, 26(3), 331-342.

budget\_expected

*Ratings of expected participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly*

**Description**

Ratings of expected participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly

**Usage**

```
budget_expected
```

**Format**

```
## 'budget_expected' a matrix with 3 rows and 3 columns.
```

**Source**

Schuster, C, (2001). Kappa as a parameter of a symmetry model for rater agreement. Journal of Educational and Behavioral Statistics, 26(3), 331-342.

Clayton\_marginal\_location

*Fits the tests comparing locations of the margins of a two-way table.*

**Description**

The measure is based on the weighted cdfs. No "scores" are used, just the weighted (cumulative sums). Clayton, D. G. (1974) Odds ratio statistics for the analysis of ordered categorical data. Biometrika, 61(3), 525-531.

**Usage**

```
Clayton_marginal_location(wx, wy)
```

**Arguments**

<code>wx</code>	vector containing frequencies for the first margin of the table
<code>wy</code>	vector containing frequencies for the second margin of the table

**Value**

a list of results odds\_ratios: odds ratios comparing cumulative frequencies of adjacent categories  
`log_theta_hat`: log of estimate of the common odds-ratio  
`theta_hat`: estimate of the common odds-ratio  
`log_mh_theta_hat`: log of the Mantel-Haenszel type odds-ratio  
`mh_theta_hat`: Mantel-Haenszel type odds-ratio  
`var_log_theta_hat` = variance of the log of the odds-ratios  
`chisq_theta_hat`: chi-square for odds-ratio  
`chisq_mh_theta_hat`: chi-square for Mantel-Haenszel odds-ratio  
`df`: degrees of freedom for chis-square = 1

**Examples**

```
Clayton_marginal_location(tonsils[1,], tonsils[2,])
```

**Clayton\_stratified\_marginal\_location**

*Clayton's stratified version of the marginal location comparison.*

**Description**

Compares marginal location conditional on a stratifying variable. Clayton, D. G. (1974) Odds ratio statistics for the analysis of ordered categorical data. Biometrika, 61(3), 525-531.

**Usage**

```
Clayton_stratified_marginal_location(mx, my)
```

**Arguments**

<code>mx</code>	matrix with
<code>my</code>	matrix with

**Value**

a list of results odds\_ratios: odds ratios comparing cumulative frequencies of adjacent categories  
`log_theta_hat`: log of estimate of the common odds-ratio  
`theta_hat`: estimate of the common odds-ratio  
`log_mh_theta_hat`: log of the Mantel-Haenszel type odds-ratio  
`mh_theta_hat`: Mantel-Haenszel type odds-ratio  
`var_log_theta_hat` = variance of the log of the odds-ratios  
`chisq_theta_hat`: chi-square for odds-ratio  
`chisq_mh_theta_hat`: chi-square for Mantel-Haenszel odds-ratio  
`df`: degrees of freedom for chis-square = 1

**See Also**

[Clayton\_marginal\_location()]

---

Clayton\_summarize      *Computes summary, cumulative proportions up to index provided*

---

### Description

Computes summary, cumulative proportions up to index provided

### Usage

```
Clayton_summarize(weights, m)
```

### Arguments

weights	matrix of counts
m	index of summation, weights[1:m]

### Value

a list containing: n: the sum of the weights p: matrix of proportion values gamma: cumulative proportions 1:m

---

---

Clayton\_summarize\_stratified  
Analysis stratified by column variable j.

---

### Description

Analysis stratified by column variable j.

### Usage

```
Clayton_summarize_stratified(weight_matrix, m)
```

### Arguments

weight_matrix	matrix of cell weights from the table
m	the column index to stratify on

### Value

a list containing: n: the number of strata p: matrix of proportion values gamma: cumulative proportions

### See Also

[Clayton\_summarize()]

**Clayton\_two\_way\_association***Clayton's stratified measure of association***Description**

Quantifies association between two ordinal variables. Clayton, D. G. (1974) Odds ratio statistics for the analysis of ordered categorical data. Biometrika, 61(3), 525-531.

**Usage**

```
Clayton_two_way_association(f)
```

**Arguments**

f	matrix of frequencies
---	-----------------------

**Value**

a list of results log\_theta\_hat: log odds-ratio measure of association theta\_hat: odds-ratio measure of association log\_mh\_theta\_hat: log of Mantel-Haenszel odds-ratio measure of association mh\_theta\_hat: Mantel-Haenszel odds-ratio measure of association var\_log\_theta\_hat: variance of the log odds-ratio measures chisq\_theta\_hat: chi-square for measure of association chisq\_mh\_theta\_hat: chi-square for Mantel-Haenszel measure of association df: degrees of freedom = 1, corr\_theta\_hat: theta-hat association converted to correlation metric corr\_mh\_theta\_hat: Mantel-Haenszel theta-hat converted to correlation metric

**Cliff\_as\_d\_matrix**

*Converts two vectors containing scores and integer frequencies (cell counts) into a d-matrix*

**Description**

Converts two vectors containing scores and integer frequencies (cell counts) into a d-matrix

**Usage**

```
Cliff_as_d_matrix(scores, cells, nrow = NULL)
```

**Arguments**

scores	vector of scores, typically 1:r
cells	vector of integer weights, i.e. cell frequencies
nrow	number of score categories in table. Default is NULL. If NULL, takes 1:length(scores)

**Value**

d-matrix of results

---

Cliff\_compute\_d      *Computes between groups dominance matrix "d".*

---

**Description**

Computes between groups dominance matrix "d".

**Usage**

cliff\_compute\_d(x, y)

**Arguments**

x	first vector of scores
y	second vector of scores

**Value**

N X N dominance matrix

---

Cliff\_counts\_2      *Generates counts from table frequencies for 2 category items*

---

**Description**

Generates counts from table frequencies for 2 category items

**Usage**

cliff\_counts\_2(mij)

**Arguments**

mij	Matrix of counts.
-----	-------------------

**Value**

a list containing  
wm1m1: for -1, -1  
wm10: for -1, 0  
wm11: for -1, 1  
w00: for 0, 0  
w01: for 0, 1  
w11: for 1, 1

**Cliff\_counts\_3**      *Generates counts from table frequencies for 3 category items*

### Description

Generates counts from table frequencies for 3 category items

### Usage

```
Cliff_counts_3(mij)
```

### Arguments

**mij**      Matrix of counts.

### Value

a list containing  
 $wm1m1:$  for -1, -1  
 $wm10:$  for -1, 0  
 $wm11:$  for -1, 1  
 $w00:$  for 0, 0  
 $w01:$  for 0, 1  
 $w11:$  for 1, 1

**Cliff\_counts\_4**      *Generates counts from table frequencies for 4 category items*

### Description

Generates counts from table frequencies for 4 category items

### Usage

```
Cliff_counts_4(mij)
```

### Arguments

**mij**      Matrix of counts.

### Value

a list containing  
 $wm1m1:$  for -1, -1  
 $wm10:$  for -1, 0  
 $wm11:$  for -1, 1  
 $w00:$  for 0, 0  
 $w01:$  for 0, 1  
 $w11:$  for 1, 1

---

Cliff\_counts\_5      *Generates counts from table frequencies for 5 category items*

---

**Description**

Generates counts from table frequencies for 5 category items

**Usage**

Cliff\_counts\_5(mij)

**Arguments**

mij      Matrix of counts.

**Value**

a list containing  
wm1m1: for -1, -1  
wm10: for -1, 0  
wm11: for -1, 1  
w00: for 0, 0  
w01: for 0, 1  
w11: for 1, 1

---

Cliff\_counts\_6      *Generates counts from table frequencies for 6 category items*

---

**Description**

Generates counts from table frequencies for 6 category items

**Usage**

Cliff\_counts\_6(mij)

**Arguments**

mij      Matrix of counts.

**Value**

a list containing  
wm1m1: for -1, -1  
wm10: for -1, 0  
wm11: for -1, 1  
w00: for 0, 0  
w01: for 0, 1  
w11: for 1, 1

**Cliff\_dependent**      *Computes Cliff's dependent d-statistics based on a dominance matrix.*

### Description

Takes the dominance matrix provided and computes the d-statistics: dw - within-subjects d-statistic db - between-subjects d-statistic db\_dw - sum of dw and db, omnibus test of whether one group is higher than the other Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. Psychological Bulletin, 114(3), 494-509. Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mawhaw NJ: Lawerence Erlbaum.

### Usage

```
Cliff_dependent(d_matrix)
```

### Arguments

d_matrix	N x N within-subjects dominance matrix
----------	--

### Value

a list containing dw: within-subjects d-statistic sigma\_dw: SE of dw z\_dw: z-score for dw db: between-subjects d-statistic sigma\_db: SE of db z\_db: z-score for db db\_dw: sum db + dw, omnibus measure sigma\_db\_dw: SE of db + dw z\_db\_dw: z-score of db \_ dw cov\_db\_dw: covariance between db and dw

### Examples

```
Cliff_dependent(interference_control_1)
```

**Cliff\_dependent\_compute\_cov**      *Computes sum term in covariance db-dw for weighted dominance matrix.*

### Description

Computes sum term in covariance db-dw for weighted dominance matrix.

### Usage

```
Cliff_dependent_compute_cov(wd)
```

### Arguments

wd	weighted dominance matrix
----	---------------------------

`Cliff_dependent_compute_cov_from_d`

*Compute the sum in the covariance of db+dw*

### Description

Compute the sum in the covariance of db+dw

### Usage

`Cliff_dependent_compute_cov_from_d(d_matrix)`

### Arguments

`d_matrix`      d-matrix of dominances

### Value

the sum for the covariance term

`Cliff_dependent_compute_from_matrix`

*Computes Cliff's dependent d-statistics based on a dominance matrix.*

### Description

Takes the dominance matrix provided and computes the d-statistics: dw - within-subjects d-statistic db - between-subjects d-statistic db\_dw - sum of db and dw, omnibus test of whether one group is higher than the other Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. Psychological Bulletin, 114(3), 494-509. Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mawhaw NJ: Lawerence-Erlbaum.

### Usage

`Cliff_dependent_compute_from_matrix(d_matrix)`

### Arguments

`d_matrix`      N x N within-subjects dominance matrix

### Value

a list containing dw: within-subjects d-statistic sigma\_dw: SE of dw z\_dw: z-score for dw db: between-suspects d-statistic sigma\_db: SE of db z\_db: z-score for db db\_dw: sum db + dw, omnibus measure sigma\_db\_dw: SE of db + dw z\_db\_dw: z-score of db \_ dw cov\_db\_dw: covariance between db and dw

**Examples**

```
Cliff_dependent_compute_from_matrix(interference_control_1)
```

**Cliff\_dependent\_compute\_from\_table**

*Computes Cliff's dependent d-statistics based on a table of frequency counts.*

**Description**

Takes the r X r table and returns: dw - within-subjects d-statistic db - between-subjects d-statistic db\_dw - sum of dw and db, omnibus test of whether one group is higher than the other No intermediate dominance matrix is computed, so this is much faster than *Cliff\_dependent\_compute\_from\_matrix()*. Large number of terms are needed to compute intermediate  $d_{ij\_ji}$ . These are contained in separate functions for  $r \leq 6$ . Results for  $r [7, 10]$  are available, but the files are so large that they cause an error if included in the library.

**Usage**

```
Cliff_dependent_compute_from_table(mij)
```

**Arguments**

mi j	an r x r table of paired observations
------	---------------------------------------

**Details**

See: Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. *Psychological Bulletin*, 114(3), 494-509. Cliff, N. (1996). *Ordinal methods for behavioral data analysis*. Mawhaw NJ: Lawerence-Erlbaum.

**Value**

a list containing dw: within-subjects d-statistic sigma\_dw: SE of dw z\_dw: z-score for dw db: between-suspects d-statistic sigma\_db: SE of db z\_db: z-score for db db\_dw: sum db + dw, omnibus measure sigma\_db\_dw: SE of db + dw z\_db\_dw: z-score of db \_ dw cov\_db\_dw: covariance between db and dw

**See Also**

[*Cliff\_dependent\_compute\_paired\_d()*]

**Examples**

```
Cliff_dependent_compute_from_table(movies)
```

---

**cliff\_dependent\_compute\_paired\_d**

*Computes Cliff's dependent d-statistics based on cell frequencies.*

---

**Description**

Computes d-matrix and then analyzes it. This can be time consuming. Try Cliff\_dependent\_from\_table() instead. The current function is provided mainly for comparison & validation. For an example, compare running this function on vision\_data to running Cliff\_dependent\_from\_table(vision\_data).

**Usage**

```
Cliff_dependent_compute_paired_d(cells)
```

**Arguments**

cells            r x r matrix of frequencies

**Details**

dw - within-subjects d-statistic  
db - between-subjects d-statistic  
db\_dw - sum of dw and db, omnibus test of whether one group is higher than the other  
Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. Psychological Bulletin, 114(3), 494-509. Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mawhaw NJ: Lawerence-Erlbaum.

**Value**

a list containing  
dw: within-subjects d-statistic  
sigma\_dw: SE of dw  
z\_dw: z-score for dw  
db: between-subjects d-statistic  
sigma\_db: SE of db  
z\_db: z-score for db  
db\_dw: sum db + dw, omnibus measure  
sigma\_db\_dw: SE of db + dw  
z\_db\_dw: z-score of db + dw  
cov\_db\_dw: covariance between db and dw

**See Also**

[Cliff\_dependent\_compute\_from\_table()]

**Examples**

```
Cliff_dependent_compute_paired_d(movies)
```

**Cliff\_independent**      *Computes the independent groups d-statistic comparing the two vectors provided.*

### Description

Computes the independent groups d-statistic comparing the two vectors provided.

### Usage

```
Cliff_independent(x, y)
```

### Arguments

x	vector of scores for first group
y	vector of scores for second group

### Value

list containing d, SE(d) and z(d)

**Cliff\_independent\_from\_matrix**      *Computes d-statistic from dominance matrix provided.*

### Description

Computes d-statistic from dominance matrix provided.

### Usage

```
Cliff_independent_from_matrix(d)
```

### Arguments

d	N X M dominance matrix
---	------------------------

### Value

list containing d, SE(d) and z(d)

---

**Cliff\_independent\_from\_table**

*Computes independent group's d-statistic from the matrix of frequencies provided.*

---

**Description**

Computes intermediate d-matrix, so can be slow for large N

**Usage**

```
Cliff_independent_from_table(n)
```

**Arguments**

n                  matrix of counts

**Value**

list containing d, SE(d) and z(d)

---

**Cliff\_independent\_weighted**

*Computes d-statistic based on scores and integer weights(frequencies) for each group.*

---

**Description**

Computes d-statistic based on scores and integer weights(frequencies) for each group.

**Usage**

```
Cliff_independent_weighted(x, w_x, y, w_y)
```

**Arguments**

x	first vector of scores
w_x	weights associated with first vector of scores
y	second vector of scores
w_y	weights associated with second vector of scores

**Value**

list containing d, SE(d) and z(d)

**Cliff\_weighted\_d\_matrix***Computes weighted version of dominance matrix "d"*

---

**Description**

Arguments are scores and associated weights. Not useful for tables. Use Cliff\_compute\_d\_matrix instead.

**Usage**

```
Cliff_weighted_d_matrix(x, y, w.x = rep(1, length(x)), w.y = rep(1, length(y)))
```

**Arguments**

x	first vector of scores
y	second vector of scores
w.x	first vector of weights, to apply to x. Defaults to vector of 1.0
w.y	second vector of weights, to apply to y. Defaults to vector of 1.0

**Value**

an n X m d-matrix, where n is length(x) and m is length(y)

**coal\_g***Degree of disease measured at two points in time for mine workers.*

---

**Description**

Based on radiological measurements, the matrix contains the degree of pneumoconiosis in coal workers. 1 = least severe disease and 4 = most severe.

**Usage**

```
coal_g
```

**Format**

```
## 'coal_g' A matrix with 4 rows and 4 columns.
```

**Source**

McCullagh, P. (1977). A logistic model for paired comparisons with ordered categorical data. *Biometrika*, 64(3), 449-453.

---

constant\_of\_integration

*Computes the constant of integration of a multinomial sample.*

---

### Description

$N! / \text{product}(n[i]!)$

### Usage

```
constant_of_integration(n, exclude_diagonal = FALSE)
```

### Arguments

n Matrix of observed counts

exclude\_diagonal

logical. Should the diagonal cells of a square matrix be excluded from the computation. Default is FALSE,

### Value

value of constant of integration for observed matrix provided

---

depression

*Ratings of severity of patient's depression by two therapists.*

---

### Description

1 = slight 2 = moderate 3 = severe

### Usage

depression

### Format

```
## 'depression' A matrix with 3 rows and 3 columns.
```

### Source

von Eye, A. & Mun, E. Y. (2005, p.41). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

dogs	<i>Dehydration in dogs data set.</i>
------	--------------------------------------

---

**Description**

An interrater agreement data set from Shourki, M. M. (2005, p.80). It is agreement study of two clinicians evaluating whether dogs were dehydrated. The lowest score indicates normal, and the highest score indicates dehydrated (above 10 The "g" in the name indicates that this is taken from mine "G" in the original study).

**Usage**

dogs

**Format**

## 'dogs' A matrix with 4 rows and 4 columns.

**Source**

Shoukri, M. M. (2005). The measurement of interobserver agreement. New York: Chapman & Hall.

---

dreams	<i>Severity of disturbing dreams in adolescent boys, measured at two ages..</i>
--------	---

---

**Description**

Severity of disturbing dreams in adolescent boys, measured at two ages..

**Usage**

dreams

**Format**

## 'dreams' A matrix with 4 rows and 4 columns.

**Source**

McCullagh, P. (1980, p.117). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142.

---

dumping

*Occurrence of side effects after gastro-intestinal surgery.*

---

**Description**

Columns 1 = None 2 = Slight 3 = Moderate

**Usage**

dumping

**Format**

## 'dumping' A matrix with 4 rows and 3 columns

**Details**

Rows Hospital A Hospital B Hospital C Hospital D

**Source**

Agresti, A. (1984, p. 63). Analysis of ordinal categorical data. New York: Wiley.

---

esophageal\_cancer

*Ratings of number of hot drinks consumed by cases with cancer of the esophagus, compared with control subjects.*

---

**Description**

Ratings of number of hot drinks consumed by cases with cancer of the esophagus, compared with control subjects.

**Usage**

esophageal\_cancer

**Format**

## 'esophageal\_cancer' A matrix with 4 rows and 4 columns.

**Source**

Agresti, A. (1984, p. 217). Analysis of ordinal categorical data. New York, Wiley.

expand	<i>Converts weighted (x, w) pairs into unweighted data by replicating x[i] w[i] times</i>
--------	---

**Description**

Takes a set of (value, weight) pairs and converts into unweighted vector (w[i]) for each i Weights are assumed to be integers

**Usage**

```
expand(x, w)
```

**Arguments**

- |   |   |
|---|---|
| x | Numeric vector of scores.                                   |
| w | Numeric vector of weights. These are assumed to be integers |

**Value**

new unweighted vector of scores

expit	<i>Computes the "expit" function – inverse of logit.</i>
-------	--

**Description**

Computes the "expit" function – inverse of logit.

**Usage**

```
expit(z)
```

**Arguments**

- |   |  |
|---|--|
| z | Numeric. Real valued argument to expit() function. |
|---|--|

**Value**

$\exp(z) / (1.0 + \exp(z))$

---

`family_income`

*Family income for two years from US census.*

---

**Description**

Family income for two years from US census.

**Usage**`family_income`**Format**

## 'family\_income' A matrix with 2 rows and 7 columns. Rows are years 1960 and 1970. Columns are income range.

**Source**

McCullagh, P. (1980, p.114). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142.

---

---

`gender_vision`

*Ratings of visual acuity for men and women employed at the Royal Ordnance factories, 1943-1946.*

---

**Description**

1 = best visual acuity 4 = worst visual acuity

**Usage**`gender_vision`**Format**

## 'gender\_vision' A matrix with 2 rows for the genders and 4 columns for visual acuity.

**Source**

McCullagh, P. (1980, p. 119). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142.

**Goodman\_constrained\_diagonals\_parameter\_symmetry**

*Fits the model where some of the delta parameters are constrained to be equal to one another.*

**Description**

Fits the model where some of the delta parameters are constrained to be equal to one another.

**Usage**

```
Goodman_constrained_diagonals_parameter_symmetry(n, equality)
```

**Arguments**

- |          |  |
|----------|--|
| n        | the matrix of observed counts  |
| equality | logical vector indicating whether corresponding delta parameter is part of the equality set. |

**Value**

a list containing  
 pooled\_chisq: Pearson chi-square for the pooled delta values  
 pooled\_df: degrees of freedom for pooled chisq  
 omnibus\_chisq: Pearson chi-square for overall model fit, subject to equality constraints  
 omnibus\_df: degrees of freedom for omnibus\_chisq  
 equality\_chisq: Pearson chi-square for test that remaining deltas are all equal  
 equality\_df: degrees of freedom for equality\_chisq  
 delta\_pooled: estimate of pooled delta

**Examples**

```
equality = c(TRUE, TRUE, FALSE)
Goodman_diagonals_parameter_symmetry(vision_data)
```

**Goodman\_diagonals\_parameter\_symmetry**

*Fit's Goodman's diagonals parameter symmetry model.*

**Description**

Goodman, L. A. (1979). Multiplicative models for square contingency tables with ordered categories. *Biometrika*, 66(3), 413-316.

**Usage**

```
Goodman_diagonals_parameter_symmetry(n)
```

### Arguments

n the matrix of obsever counts

### Value

a list containing individual\_chisq: chi-square value for each diagonal individual\_df: degrees of freedom for individual\_chisq omnibus\_chisq: overall chi-square for the model omnibus\_df: degrees for freedom for omnibus\_chisq equality\_chisq: chi-square for test that all delta values are equal equality\_df: degrees of freedom from equality\_chisq delta: the vector of estimated delta values (without any equality constraints)

### Examples

```
Goodman_diagonals_parameter_symmetry(vision_data)
```

### Goodman\_fixed\_parameter

*Fits the model with given parameters fixed to specific values.*

### Description

The model has simple closed form solutions when fitting either the unconstrained version of the version that species equality of delta parameters. However, I could not see how to adapt that to the case where specific parameters were constrained to have a specific value. This routine is to fit that model. It will also fit the unconstrained model, but Goodman gives the estimator for that case.

### Usage

```
Goodman_fixed_parameter(
  n,
  delta,
  fixed,
  convergence = 1e-04,
  max_iter = 50,
  verbose = FALSE
)
```

### Arguments

n	the r X r matrix of observed counts
delta	the vector of asymmetry r - 1 parameters
fixed	r - 1 logical vector that specifies whether a delta parameter is fixed (TRUE) or allowed to be estimated (FALSE).
convergence	maximum change in a parameter across iterations. Default is 1.0e-4
max_iter	maximum number of iterations, Default is 50.
verbose	should progress information be printed to the console. Default is FALSE, do not print.

**Value**

list containing phi, delta, max\_change largest change in parameter for last the iteration, chisq: Pearson chi-square g\_squared: likelihood ratio G^2 df: degrees of freedom

**See Also**

[Goodman\_diagonals\_parameter\_symmetry()]  
 [Goodman\_ml()]

**Examples**

```
fixed <- c(FALSE, TRUE, FALSE)
delta <- c(1.0, 1.0, 1.0)
phi <- matrix(0.0, nrow=4, ncol=4)
diag(phi) = rep(1.0, 4)
Goodman_fixed_parameter(vision_data, delta, fixed)
```

Goodman\_ml

*Performs ML estimation of the model.***Description**

The model has simple closed form solutions when fitting either the unconstrained version of the version that species equality of delta parameters. However, I could not see how to adapt that to the case where specific parameters were constrained to have a specific value. This routine is to fit that model. It will also fit the unconstrained model, but Goodman gives the estimator for that case.

**Usage**

```
Goodman_ml(n, phi, delta, fixed)
```

**Arguments**

n	the r X r matrix of observed counts
phi	the symmetric matrix parameter
delta	the vector of asymmetry r - 1 parameters
fixed	r - 1 logical vector that specifies whether a delta parameter is fixed (TRUE) or allowed to be estimated (FALSE).

**Value**

list containing new estimates of phi and delta

**See Also**

[Goodman\_diagonals\_parameter\_symmetry()]

## Examples

```
fixed <- c(FALSE, TRUE, FALSE)
delta <- c(1.0, 1.0, 1.0)
phi <- matrix(0.0, nrow=4, ncol=4)
for (i in 1:4) {
  phi[i, i] = 1.0
}
Goodman_ml(vision_data, phi, delta, fixed)
```

Goodman\_model\_i      *Fits Goodman's (1979) Model I*

## Description

Fits Goodman's (1979) Model I

## Usage

```
Goodman_model_i(
  n,
  row_effects = TRUE,
  column_effects = TRUE,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

## Arguments

<code>n</code>	matrix of observed counts
<code>row_effects</code>	should row effects be included in the model? Default is TRUE
<code>column_effects</code>	should column effects be included in the model? Default is TRUE
<code>max_iter</code>	maximum number of iterations. Default is 10
<code>verbose</code>	logical. Should cycle-by-cycle output be printed? Default is no
<code>exclude_diagonal</code>	logical. For square tables, should the cells on the diagonal be excluded? Default is FALSE, include all cells

## Value

a list containing alpha: row effects beta: column effects gamma: row location weights delta: column location weights log\_likelihood: log(likelihood) g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom

---

Goodman\_model\_ii      *Fits Goodman's (1979) Model II*

---

## Description

Fits Goodman's (1979) Model II

## Usage

```
Goodman_model_ii(
  n,
  rho = 1:nrow(n) - (nrow(n) + 1)/2,
  sigma = 1:ncol(n) - (ncol(n) + 1)/2,
  update_rows = TRUE,
  update_columns = TRUE,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

## Arguments

n	matrix of observed counts
rho	values of row locations. Default is 1:nrow(n) - (nrow(n) + 1) / 2
sigma	values of column locations. Default is 1:ncol(n) - (ncol(n) + 1) / 2
update_rows	should values of row locations be updated? Default is TRUE, update
update_columns	should value of column locations be updated? Default is TRUE, update
max_iter	maximum number of iterations to perform. Default is 10
verbose	should cycle-by-cycle output be produced? Default is FALSE
exclude_diagonal	logical. Should the diagonal be excluded from the computation. Default is FALSE.

## Value

a list containing alpha: row effects beta: column effects rho: centered row locations mu: row locations sigma: centered column locations nu: column locations log\_likelihood: log(likelihood) g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom

---

Goodman\_model\_ii\_star *Fits Goodman's (1979) model II\*, where row and column effects are equal.*

---

### Description

Fits Goodman's (1979) model II\*, where row and column effects are equal.

### Usage

```
Goodman_model_ii_star(
  n,
  exclude_diagonal = FALSE,
  max_iter = 25,
  verbose = FALSE
)
```

### Arguments

n	matrix of observed counts
exclude_diagonal	should the cells of the main diagonal be excluded? Default is FALSE, include all cells
max_iter	maximum number of iterations
verbose	should cycle-by-cycle information be printed out? Default is FALSE, do not print

### Value

a list containing alpha: vector of alpha (row) parameters  
 beta: vector of beta (column) parameters  
 phi: vector of common row/column effects  
 log\_likelihood: value of the log(likelihood) function at completion  
 g\_squared: G^2 fit measure  
 chisq: X^2 fit measure  
 df: degrees of freedom

---

Goodman\_model\_i\_star *Fits Goodman's (1979) Model I\**

---

### Description

Fits Goodman's (1979) Model I\*

**Usage**

```
Goodman_model_i_star(
  n,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

**Arguments**

n	matrix of observed counts
max_iter	maximum number of iterations
verbose	should cycle-by-cycle information be printed out? Default is FALSE, do not print
exclude_diagonal	should the cells along the main diagonal be excluded? Default is FALSE, include all cells

**Value**

a list containing alpha: vector of row parameters  
 beta: vector of column parameters  
 theta: vector of common row/column estimates  
 log\_likelihood: log(likelihood) at completion  
 g\_squared: G^2 fit measure  
 chisq: X^2 fit measure  
 df: degrees of freedom

**Goodman\_null\_association**

*Fits Goodman's L. A. (1979) Simple Models for the Analysis of Association in Cross-Classifications Having Ordered Categories*

**Description**

null association model

**Usage**

```
Goodman_null_association(
  n,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

**Arguments**

n	matrix of observed counts
max_iter	maximum number of iterations. Default is 10
verbose	should cycle-by-cycle info be printed? Default is FALSE
exclude_diagonal	logical, Should the diagonal be excluded from the computations. Default is FALSE

**Value**

a list containing alpha: row effects beta: column effects log\_likelihood: log(likelihood) g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom

Goodman\_pi

*Computes the model-based probability for cell i, j*

**Description**

Computes the model-based probability for cell i, j

**Usage**

```
Goodman_pi(phi, delta, i, j)
```

**Arguments**

phi	symmetry matrix
delta	vector of asymmetry parameters
i	row index
j	column index

**Value**

pi for that cell

`Goodman_pi_matrix`      *Computes the full matrix of model-based cell probabilities.*

### Description

Computes the full matrix of model-based cell probabilities.

### Usage

```
Goodman_pi_matrix(phi, delta)
```

### Arguments

phi	the symmetric matrix
delta	the vector of asymmetry parameters

### Value

matrix of model-based probabilities

`Goodman_symmetric_association_model`

*Fits the symmetric association model from Goodman (1979). Note the model is a reparameterized version of the quasi-symmetry model, so the quasi-symmetry model has the same fit indices.*

### Description

Fits the symmetric association model from Goodman (1979). Note the model is a reparameterized version of the quasi-symmetry model, so the quasi-symmetry model has the same fit indices.

### Usage

```
Goodman_symmetric_association_model(n)
```

### Arguments

n	matrix of observed counts
---	---------------------------

### Value

a list containing x: design matrix used for the `glm()` regression  
 beta: parameter estimates  
 se: standard errors of beta  
 g\_squared:  $G^2$  measure of fit  
 chisq:  $\chi^2$  measure of fit  
 df: degrees of freedom  
 expected: model-based expected cell counts

---

**Goodman\_uniform\_association**

*Fits Goodman's (1979) uniform association model*

---

**Description**

Fits Goodman's (1979) uniform association model

**Usage**

```
Goodman_uniform_association(
  n,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

**Arguments**

n	matrix of observed counts
max_iter	maximum number of iterations. Default is 10.
verbose	should cycle-by-cycle info be printed out? Default is FALSE
exclude_diagonal	logical. Should the cells of the main diagonal be excluded from the computations? Default is FALSE, include all cells.

**Value**

a list containing alpha: row effects beta: column effects theta: uniform association parameter log\_likelihood: log(likelihood) g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom

---

**handle\_max\_i\_i**      *Case where j == r, i == k == k2*

---

**Description**

Case where j == r, i == k == k2

**Usage**

```
handle_max_i_i(i, marginal_pi, kappa, v)
```

**Arguments**

i	index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second-order derivative

**handle\_max\_i\_k**

*Case where j == r, i != k, i == k2*

**Description**

Case where j == r, i != k, i == k2

**Usage**

```
handle_max_i_k(i, k, marginal_pi, kappa, v)
```

**Arguments**

i	index into pi
k	index into v (other is i)
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second-order derivative

handle_max_k_k2	<i>Case where j == r; i != k &amp;&amp; i != k2</i>
-----------------	---

**Description**

Case where  $j == r, i \neq k \&\& i \neq k2$

**Usage**

```
handle_max_k_k2(i, k, k2, marginal_pi, kappa, v)
```

**Arguments**

i	index into pi
k	first index into marginal_pi
k2	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second-order derivative

handle_one_maximum	<i>Case where pi[i, r] with k and k2</i>
--------------------	--

**Description**

Case where  $\pi[i, r]$  with k and k2

**Usage**

```
handle_one_maximum(i, j, k, k2, marginal_pi, kappa, v)
```

**Arguments**

i	first index of pi
j	second index of pi
k	first index into marginal_pi
k2	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second order derivative

---



---

**handle\_tied\_below\_maximum**

*Case where i == j, i < r, j < r*

---

**Description**

Case where  $i == j, i < r, j < r$

**Usage**

`handle_tied_below_maximum(j, k, k2, marginal_pi, kappa, v)`

**Arguments**

j	index of pi
k	first index into marginal_pi
k2	second index into marginal_pi
marginal_pi	expected proportions for each of the categories
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

derivative

---



---

**handle\_tied\_maximum**

*Case where pi[r, r] with k and k2*

---

**Description**

Case where  $\pi[r, r]$  with k and k2

**Usage**

`handle_tied_maximum(k, k2, marginal_pi, kappa, v)`

**Arguments**

k	first index into marginal_pi
k2	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second order derivative

---

**handle\_untied\_below\_maximum**

*Case where i != j, i < r && j < r*

---

**Description**

Case where  $i \neq j, i < r \&\& j < r$

**Usage**

```
handle_untied_below_maximum(i, j, k, k2, marginal_pi, kappa, v)
```

**Arguments**

i	first index of pi
j	second index of pi
k	first index of marginal_pi
k2	second index of marginal_pi
marginal_pi	expected proportions of each of the categories
kappa	current value of kappa coefficient
v	symmetry matrix

`homicide_black_black` *Data about charges of homicide in the state of Florida.*

### Description

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_". The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore

### Usage

`homicide_black_black`

### Format

## 'homicide\_black\_black' Each is a matrix with 3 rows and 3 columns. Rows are classification by police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 2 = Felony

### Source

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

`homicide_black_white` *Data about charges of homicide in the state of Florida.*

### Description

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_". The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore.

### Usage

`homicide_black_white`

### Format

## 'homicide\_black\_white' Each is a matrix with 3 rows and 3 columns. Rows are classification by police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 2 = Felony

### Source

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

---

homicide\_white\_black    *Data about charges of homicide in the state of Florida.*

---

**Description**

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_". The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore

**Usage**

```
homicide_white_black
```

**Format**

## 'homicide\_white\_black' Each is a matrix with 3 rows and 3 columns. Rows are classification by police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 2 = Felony

**Source**

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

---

---

homicide\_white\_white    *Data about charges of homicide in the state of Florida.*

---

**Description**

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_". The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore

**Usage**

```
homicide_white_white
```

**Format**

## 'homicide\_white\_white' Each is a matrix with 3 rows and 3 columns. Rows are classification by police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 2 = Felony

**Source**

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

---

*hypothalamus\_1                          Measures of men's hypothalamus taken from cadavers. First data set.*

---

**Description**

Measures of men's hypothalamus taken from cadavers. First data set.

**Usage**

`hypothalamus_1`

**Format**

# 'hypothalamus\_1' Each set is a dominance matrix (see e.g., Cliff 1996).

**Source**

Cliff, N. (1996), Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum.

---

*hypothalamus\_2                          Measures of men's hypothalamus taken from cadavers. Second data set.*

---

**Description**

Measures of men's hypothalamus taken from cadavers. Second data set.

**Usage**

`hypothalamus_2`

**Format**

# 'hypothalamus\_2' Each set is a dominance matrix (see e.g., Cliff 1996).

**Source**

Cliff, N. (1996), Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum.

---

`interference_12`

*Measures of interference in memory recall study.*

---

**Description**

Measures are within subjects, comparing a control condition to two conditions with interference.  
Interference condition 1 v. interference condition 2

**Usage**`interference_12`**Format**

`## 'interference_control_1', 'interference_control_2', 'interference_12'` Within-persons dominance matrices.

**Source**

Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum

---

---

`interference_control_1`

*Measures of interference in memory recall study.*

---

**Description**

Measures are within subjects, comparing a control condition to two conditions with interference.  
Control v. interference condition 1

**Usage**`interference_control_1`**Format**

`## 'interference_control_1', 'interference_control_2', 'interference_12'` Within-persons dominance matrices.

**Source**

Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum.

**interference\_control\_2**

*Measures of interference in memory recall study.*

**Description**

Measures are within subjects, comparing a control condition to two conditions with interference.  
Control v. interference condition 2

**Usage**

```
interference_control_2
```

**Format**

```
## 'interference_control_1', 'interference_control_2', 'interference_12' Within-persons dominance  
matrices.
```

**Source**

Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum

**Ireland\_marginal\_homogeneity**

*Fits marginal homogeneity model*

**Description**

Fits the marginal homogeneity model according to the minimum discriminant information. Ireland, C. T., Ku, H. H., & Kullback, S. (1969). Symmetry and marginal homogeneity of an  $r \times r$  contingency table. Journal of the American Statistical Association, 64(328), 1323-1341.

**Usage**

```
Ireland_marginal_homogeneity(  
  n,  
  truncated = FALSE,  
  max_iter = 15,  
  verbose = FALSE  
)
```

**Arguments**

n	matrix of observed counts
truncated	should the diagonal be excluded. Default is FALSE, include the diagonal.
max_iter	maximum number of iterations to perform
verbose	should cycle-by-cycle information be printed out. Default is FALSE.

**Value**

a list containing mdis: value of the minimum discriminant information statistic (approx chi-squared)  
 df: degrees of freedom x\_star: matrix of model-based counts p\_star: matrix of model-based p-values

**Examples**

```
Ireland_marginal_homogeneity(vision_data)
```

---

Ireland\_mdis

*Computes the MDIS between the two matrices provided.*

---

**Description**

Computes the MDIS between the two matrices provided.

**Usage**

```
Ireland_mdis(n, x_star, truncated = FALSE)
```

**Arguments**

- |           |  |
|-----------|--|
| n         | first matrix (usually observed counts)   |
| x_star    | second matrix (usually model-based)  |
| truncated | should the diagonal be ignored. Default is FALSE, include the diagonal elements. |

**Value**

value of the MDIS criterion

---

Ireland\_normalize\_for\_truncation

*Renormalize counts to account for truncation of diagonal*

---

**Description**

Renormalize counts to account for truncation of diagonal

**Usage**

```
Ireland_normalize_for_truncation(n)
```

**Arguments**

- |   |                           |
|---|---------------------------|
| n | matrix of observed counts |
|---|---------------------------|

**Value**

matrix n with diagonal set to 0.0

---

**Ireland\_quasi\_symmetry**

*Fit for quasi-symmetry model. Obtained by subtraction, so no model-based probabilities.*

---

**Description**

Fit for quasi-symmetry model. Obtained by subtraction, so no model-based probabilities.

**Usage**

```
Ireland_quasi_symmetry(n, truncated = FALSE)
```

**Arguments**

- |           |  |
|-----------|--|
| n         | matrix of observed counts  |
| truncated | should the diagonal be excluded, Default is FALSE, include the diagonal. |

**Value**

a list with mdis = MDIS value and df = degrees of freedom for quasi-symmetry model

**See Also**

[Ireland\_quasi\_symmetry\_model()]

**Examples**

```
Ireland_quasi_symmetry(vision_data)
```

**Ireland\_quasi\_symmetry\_model**

*Fits the quasi-symmetry model.*

---

**Description**

Fits the model according to the MDIS criterion.

**Usage**

```
Ireland_quasi_symmetry_model(
  n,
  truncated = FALSE,
  max_iter = 5,
  verbose = FALSE
)
```

**Arguments**

n	matrix of observed counts
truncated	should the diagonal be excluded. Default is FALSE, include diagonal cells.
max_iter	maximum number of iterations in minimizing the criterion. Default is 4
verbose	logical variable, should cycle-by-cycle info be printed. Defaultlt is FALSE.

**Value**

a list containing  
 mdis: value of the MDIS at termination  
 df: degrees of freedom  
 x\_star: matrix of model-reproduced counts  
 p\_star: matrix of model-reproduced p-values

**See Also**

[Ireland\_quasi\_symmetry()]

**Examples**

```
Ireland_quasi_symmetry_model(vision_data)
```

Ireland\_symmetry      *Fits symmetry model.*

**Description**

Ireland, C. T., Ku, H. H., & Kullback, S. (1969). Symmetry and marginal homogeneity of an  $r \times r$  contingency table. Journal of the American Statistical Association, 64(328), 1323-1341.

**Usage**

```
Ireland_symmetry(n, truncated = FALSE)
```

**Arguments**

n	matrix of observed counts
truncated	should the diagonal be excluded. Default is FALSE, include the diagonal.

**Value**

a list containing mdis: value of the minimum discriminant information statistic (approx chi-squared)  
df: degrees of freedom x\_star: matrix of model-based counts p\_star: matrix of model-based p-values

**Examples**

```
Ireland_symmetry(vision_data)
```

**is\_invertible**

*Tests whether a square matrix is invertible (non singular)*

**Description**

from stackoverflow: <https://stackoverflow.com/questions/24961983/how-to-check-if-a-matrix-has-an-inverse-in-the-r-language>

**Usage**

```
is_invertible(X)
```

**Arguments**

X Matrix to be tested. It is assumed X is square

**Value**

logical: TRUE if inversion succeeds, FALSE otherwise

**is\_missing\_or\_infinite**

*Determines if its argument is not a valid number.*

**Description**

Determines if its argument is not a valid number.

**Usage**

```
is_missing_or_infinite(x)
```

**Arguments**

x Numeric. Number of be evaluated

**Value**

TRUE if is.na(), is.nan(), or is.infinite() returns TRUE. FALSE otherwise.

---

kappa	<i>Computes Cohen's 1960 kappa coefficient</i>
-------	--

---

**Description**

Computes Cohen's 1960 kappa coefficient

**Usage**

```
kappa(n)
```

**Arguments**

n matrix of observed counts

**Value**

kappa coefficient

---

likelihood_ratio_chisq	
------------------------	--

*Computes the likelihood ratio G^2 measure of fit.*

---

**Description**

Computes the likelihood ratio G^2 measure of fit.

**Usage**

```
likelihood_ratio_chisq(n, pi, exclude_diagonal = FALSE)
```

**Arguments**

n Matrix of observed counts

pi Matrix of same dimensions as n. Model-based matrix of predicted proportions

exclude\_diagonal

logical. Should the diagonal cells of a square matrix be excluded from the computation. Default is FALSE. The effect of setting it to TRUE for non-square matrices may be unintuitive and should be avoided.

**Value**

G^2

**loadRData***Function to load a data set written out using save().***Description**

The first (should be the only) element read from the RData file is returned From: <https://stackoverflow.com/questions/55772211/can-i-load-an-object-into-a-variable-name-that-i-specify-from-an-r-data-file>

**Usage**

```
loadRData(file_name)
```

**Arguments**

file_name	Character. Name of the file containing the RData
-----------	--

**Details**

```
usage x <- loadRData(file_name="")
```

**Value**

the first object from the restored RData

**logit***Computes the log-odds (logit) for the value provided***Description**

Computes the log-odds (logit) for the value provided

**Usage**

```
logit(p)
```

**Arguments**

p	Numeric. Assumed to lie in interval(0, 1)
---	---

**Value**

```
log(p / (1.0 - p))
```

---

log\_likelihood      *Computes the multinomial log(likelihood).*

---

### Description

Computes the multinomial log(likelihood).

### Usage

```
log_likelihood(n, pi, exclude_diagonal = FALSE)
```

### Arguments

n	Matrix of observed counts
pi	Matrix of same dimensions as n. Model-based matrix of predicted proportions
exclude_diagonal	logical. Should diagonal cells of square matrix be excluded from the computation? Default is FALSE. The effect of setting it to TRUE for non-square matrices may be unintuitive and should be avoided.

### Value

log(likelihood)

---

log\_linear\_add\_all\_diagonals

*Adds indicator variables for the diagonal cells in table n.*

---

### Description

Adds indicator variables for the diagonal cells in table n.

### Usage

```
log_linear_add_all_diagonals(n, x)
```

### Arguments

n	the matrix of observed counts
x	the design matrix to be augmented

### Value

new design matrix with nrow(n) columns added. The columns are all 0 unless the row corresponds to a diagonal cell in n, in which case the entry is 1

**Examples**

```
x <- log_linear_main_effect_design(vision_data)
x_prime <- log_linear_add_all_diagonals(vision_data, x)
```

**log\_linear\_append\_column**

*Appends a column to an existing design matrix.*

**Description**

Takes the design matrix provided and appends the new column

**Usage**

```
log_linear_append_column(x, x_new, position = ncol(x) + 1)
```

**Arguments**

- |          |   |
|----------|---|
| x        | the original design matrix  |
| x_new    | the column to be appended   |
| position | column index within the new matrix for the new column. Defaults to last position = appending the column |

**Value**

the new design matrix

**Examples**

```
x <- log_linear_main_effect_design(vision_data)
new_column <- c(1, 0, 0, 0,
              0, 1, 0, 0,
              0, 0, 1, 0,
              0, 0, 0, 1)
x_prime <- log_linear_append_column(x, new_column)
```

---

```
log_linear_create_coefficient_names  
Creates missing column names
```

---

### Description

Creates missing column names

### Usage

```
log_linear_create_coefficient_names(x, n, effect_names = NULL)
```

### Arguments

x	the design matrix being modified
n	the matrix of observed counts
effect_names	user specified names to be applied to effects after the intercept and main effects. Default is NULL

### Value

a vector of names to apply to x

---

```
log_linear_create_linear_by_linear  
Creates a vector containing the linear-by-linear vector.
```

---

### Description

Uses the ordinal ranks (1, 2, ..., nrow(n)) as data.

### Usage

```
log_linear_create_linear_by_linear(n, centered = FALSE)
```

### Arguments

n	the matrix of observed cell counts
centered	should the variables be centered before the product is computed

### Value

a vector containing the new variable

## Examples

```
linear <- log_linear_create_linear(vision_data)
x <- log_linear_equal_weight_agreement_design(vision_data)
x_prime <- log_linear_append_column(x, linear)
```

### log\_Linear\_create\_log\_n

*Computes the logs of the cell frequencies.*

## Description

In the case of an observed 0, epsilon is inserted into the cell before the log is taken.

## Usage

```
log_Linear_create_log_n(n, epsilon = 1e-06, all_cells = FALSE)
```

## Arguments

n	matrix of cell counts
epsilon	amount to be inserted into cell with observed 0.
all_cells	add epsilon to all cells or just those with 0 observed frequencies

## Value

a list containing: log\_n – a vector of log frequencies and dat – modified version of the cell counts data

### log\_linear\_equal\_weight\_agreement\_design

*Creates design matrix for model with main effects and a single agreement parameter delta.*

## Description

The model has main effects for rows and for columns, plus an additional parameter for the agreement (diagonal) cells.

## Usage

```
log_linear_equal_weight_agreement_design(n, n_raters = 2)
```

**Arguments**

- n the matrix of cell counts  
 n\_raters number of raters. Currently only 2 (the default) are supported. This is an extension point for future work.

**Value**

design matrix for the model

**Examples**

```
x <- log_linear_equal_weight_agreement_design(vision_data)
```

`log_linear_fit`

*Fits a log-linear model to the data provided, using the design matrix provided. Names for the effects will be "rows1", "cols1" etc. If there are remaining entries, they can be specified as the "effect\_names" character vector. This function is a wrapper around a call to glm() that handles some of the details of the call and packages the output in a more convenient form.*

**Description**

Fits a log-linear model to the data provided, using the design matrix provided. Names for the effects will be "rows1", "cols1" etc. If there are remaining entries, they can be specified as the "effect\_names" character vector. This function is a wrapper around a call to glm() that handles some of the details of the call and packages the output in a more convenient form.

**Usage**

```
log_linear_fit(n, x, effect_names = NULL)
```

**Arguments**

- n matrix of observed counts to be fit  
 x design matrix for predictor variables  
 effect\_names character vector of additional names to apply to the columns of x. The default is NULL, in which case the columns will be labeled "model1" etc.

**Value**

a list containing x: the design matrix beta: the regression parameters se: the vector of standard errors g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

---

`log_linear_main_effect_design`

*Design matrix for baseline independence model with main effects for rows and columns.*

---

## Description

It is intended as a straw-man model as it assumes no agreement beyond chance.

## Usage

```
log_linear_main_effect_design(n, n_raters = 2)
```

## Arguments

<code>n</code>	the matrix of cell counts
<code>n_raters</code>	number of raters. Currently only 2 (the default) are supported. This is an extension point for future work.

## Value

the design matrix for the model

## Examples

```
x <- log_linear_main_effect_design(vision_data)
```

---

`log_linear_matrix_to_vector`

*Converts a matrix of data into a vector suitable for use in analysis with the design matrices created. Unlike simply calling `vector()` on the matrix the resulting vector is organized by rows, then columns. This order corresponds to the order in the design matrix.*

---

## Description

Converts a matrix of data into a vector suitable for use in analysis with the design matrices created. Unlike simply calling `vector()` on the matrix the resulting vector is organized by rows, then columns. This order corresponds to the order in the design matrix.

## Usage

```
log_linear_matrix_to_vector(dat)
```

**Arguments**

dat                   the matrix to be converted a vector

**Value**

a vector suitable to use as dependent variable, e.g. in a call to `glm()`

---

`log_linear_quasi_symmetry_model_design`

*Creates the design matrix for a quasi-symmetry design*

---

**Description**

Creates the design matrix for a quasi-symmetry design

**Usage**

`log_linear_quasi_symmetry_model_design(n)`

**Arguments**

n                   matrix of observed counts

**Value**

design matrix for quasi-symmetry design

---

`log_linear_remove_column`

*Removes a column from an existing design matrix.*

---

**Description**

Takes the design matrix provided and removes the column in the position specified

**Usage**

`log_linear_remove_column(x, position = ncol(x))`

**Arguments**

x                   the original design matrix

position           column index within the new matrix for the new column. Defaults to last position

**Value**

the new design matrix

**Examples**

```
x <- log_linear_main_effect_design(vision_data)
linear <- log_linear_create_linear_by_linear(vision_data)
x_prime <- log_linear_append_column(x, linear)
x_again <- log_linear_remove_column(x_prime, ncol(x_prime))
```

---

**log\_linear\_symmetry\_design**

*Creates design matrix for symmetry model.*

---

**Description**

Creates design matrix for symmetry model.

**Usage**

```
log_linear_symmetry_design(n)
```

**Arguments**

n	matrix of observed counts
---	---------------------------

**Value**

design matrix for the model

---

**McCullagh\_compute\_condition**

*Compute the linear constraint on psi elements for identifiability.*

---

**Description**

Compute the linear constraint on psi elements for identifiability.

**Usage**

```
McCullagh_compute_condition(psi)
```

**Arguments**

psi	symmetry matrix
-----	-----------------

**Value**

value of the constraint

---

McCullagh\_compute\_cumulatives

*Computes the model-based cumulative probability matrices  $p_{ij}$  and  $q_{ij}$*

---

**Description**

Computes the model-based cumulative probability matrices  $p_{ij}$  and  $q_{ij}$

**Usage**

```
McCullagh_compute_cumulatives(psi, delta, alpha, c = 1)
```

**Arguments**

psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

list containing matrices  $p_{ij}$  and  $q_{ij}$

---

McCullagh\_compute\_cumulative\_sums

*Computes cumulative sums for rows,*

---

**Description**

Computes cumulative sums for rows,

**Usage**

```
McCullagh_compute_cumulative_sums(n)
```

**Arguments**

n	matrix of observed counts
---	---------------------------

**Value**

R where R[i, ] contains cumulative sum of n[i, ]

**McCullagh\_compute\_c\_plus***Computes sums c+ used in maximizing the log(likelihod)*

---

**Description**

Computes sums c+ used in maximizing the log(likelihod)

**Usage**

```
McCullagh_compute_c_plus(phi, alpha)
```

**Arguments**

phi	matrix of symmetry parameters
alpha	vector of asymmetry parameters

**Value**

list of c\_i\_plus and c\_plus\_i

**McCullagh\_compute\_df***Computes the degrees of freedom for the model*

---

**Description**

Computes the degrees of freedom for the model

**Usage**

```
McCullagh_compute_df(M, generalized = FALSE)
```

**Arguments**

M	the size of the M X M observed matrix
generalized	is the generalized model being fit? Default is FALSE, regular model

---

McCullagh\_compute\_gamma

*Computes gamma from x and beta*

---

**Description**

Computes gamma from x and beta

**Usage**

```
McCullagh_compute_gamma(x, beta, s, c)
```

**Arguments**

x	predictor variables
beta	vector of regression coefficients
s	number of rows in the table
c	number of score levels in table

**Value**

vector of model-based gamma coefficients

---

---

McCullagh\_compute\_gamma\_from\_phi

*Computes value of gamma from phi. Inverse of usual computation.*

---

**Description**

Computes value of gamma from phi. Inverse of usual computation.

**Usage**

```
McCullagh_compute_gamma_from_phi(phi, j, gamma)
```

**Arguments**

phi	value to compute from
j	index to use in computation
gamma	vector of gamma values (model-based cumulative logits)

**Value**

gamma[j] given phi and gamma[j + 1]

`McCullagh_compute_gamma_plus_1_from_phi`

*Computes value of gamma[j + 1] from phi.*

### Description

Computes value of gamma[j + 1] from phi.

### Usage

```
McCullagh_compute_gamma_plus_1_from_phi(phi, j, gamma)
```

### Arguments

phi	value used in computation
j	index to use in computation
gamma	vector of gamma values (model-based cumulative logits)

### Value

gamma[j + 1] given phi and gamma[j]

`McCullagh_compute_generalized_cumulatives`

*Compute the model-based cumulative probabilities pij and qij.*

### Description

Compute the model-based cumulative probabilities pij and qij.

### Usage

```
McCullagh_compute_generalized_cumulatives(psi, delta_vec, alpha, c = 1)
```

### Arguments

psi	symmetry matrix
delta_vec	vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant so pis sum to 1. Defaults to 1.0

### Value

matrices of model-based cumulative probabilities pij and qij

**McCullagh\_compute\_generalized\_pi**

*Cpompute matrix pi under generalized model.*

**Description**

Cpompute matrix pi under generalized model.

**Usage**

```
McCullagh_compute_generalized_pi(psi, delta_vec, alpha, c = 1)
```

**Arguments**

psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

the matrix pi

**McCullagh\_compute\_lambda**

*Computes lambda, log of cumulative odds.*

**Description**

Computes lambda, log of cumulative odds.

**Usage**

```
McCullagh_compute_lambda(n, use_half = TRUE)
```

**Arguments**

n	matrix of observed counts
use_half	logical whether or not to add half to the cell count before taking the logit. Default value is TRUE.

**McCullagh\_compute\_log\_l**

*Computes the log(likelihood) for the general nonlinear model.*

**Description**

Computes the log(likelihood) for the general nonlinear model.

**Usage**

```
McCullagh_compute_log_l(n, phi)
```

**Arguments**

n	matrix of observed counts
phi	vector of model-based parameters

**Value**

log(likelihood)

**McCullagh\_compute\_Nij** *Compute the observed sums Nij***Description**

Compute the observed sums Nij

**Usage**

```
McCullagh_compute_Nij(n)
```

**Arguments**

n	the matrix of observed counts
---	-------------------------------

**Value**

a list containing Pij and Qij

---

McCullagh\_compute\_omega

*Compute the value of the Lagrange multiplier for the constraint on psi.*

---

**Description**

Compute the value of the Lagrange multiplier for the constraint on psi.

**Usage**

```
McCullagh_compute_omega(n, pi)
```

**Arguments**

n	matrix of observed counts
pi	matrix of model-based probabilities pi.

**Value**

the value of the Lagrange multiplier.

---

McCullagh\_compute\_phi *Computes phi based on gamma*

---

**Description**

Computes phi based on gamma

**Usage**

```
McCullagh_compute_phi(gamma, j)
```

**Arguments**

gamma	vector of gamma parameters
j	index of phi to compute

**Value**

phi[j]

**McCullagh\_compute\_phi\_matrix***Compute matrix of model-based logits***Description**

Compute matrix of model-based logits

**Usage**`McCullagh_compute_phi_matrix(gamma)`**Arguments**

<code>gamma</code>	matrix of model-based cumulative odds
--------------------	---------------------------------------

**Value**

matrix of model-based logits

**McCullagh\_compute\_pi**    *Compute the regular (non-cumulative) model-based pi values***Description**

Compute the regular (non-cumulative) model-based pi values

**Usage**`McCullagh_compute_pi(psi, delta, alpha, c)`**Arguments**

<code>psi</code>	the matrix of symmetry parameters
<code>delta</code>	the scalar asymmetry parameter
<code>alpha</code>	the vector of asymmetry parameters
<code>c</code>	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

the matrix pi

---

McCullagh\_compute\_pi\_from\_beta

*Computes matrix of p-values pi based on x and current value of beta.*

---

**Description**

Computes matrix of p-values pi based on x and current value of beta.

**Usage**

```
McCullagh_compute_pi_from_beta(n, x, beta)
```

**Arguments**

n	matrix of observed counts
x	design matrix
beta	current values of location model regression parameters

**Value**

matrix of model-based pi values

---

McCullagh\_compute\_pi\_from\_gamma

*Compute the cell probabilities pi from gamma.*

---

**Description**

Compute the cell probabilities pi from gamma.

**Usage**

```
McCullagh_compute_pi_from_gamma(gamma)
```

**Arguments**

gamma	matrix of gamma values
-------	------------------------

**Value**

c X c matrix of p-values pi

**McCullagh\_compute\_regression\_weights**

*Computes regression weights w; R\_dot\_j \* (N - R\_dot\_j[j]) \* (n\_do\_j[j] a= na\_dot\_j[j+ 1] )*

---

**Description**

Computes regression weights w; R\_dot\_j \* (N - R\_dot\_j[j]) \* (n\_do\_j[j] a= na\_dot\_j[j+ 1] )

**Usage**

```
McCullagh_compute_regression_weights(n)
```

**Arguments**

n matrix of observed counts

**Value**

list of w, and sum(w)

---

**McCullagh\_compute\_s\_plus**

*Compute sums too use in maximizing log(likelihood)*

---

**Description**

Compute sums too use in maximizing log(likelihood)

**Usage**

```
McCullagh_compute_s_plus(n)
```

**Arguments**

n matrix of observed counts

**Value**

list of s\_i\_plus and s\_plus\_i

---

McCullagh\_compute\_update

*Compute the Newton-Raphson update.*

---

**Description**

Compute the Newton-Raphson update.

**Usage**

```
McCullagh_compute_update(gradient, hessian)
```

**Arguments**

gradient	gradient vector of log(likelihood) wrt parameters
hessian	hessian of log(likelihood) wrt parameters

**Value**

vector with update values for each of the parameters

---

## McCullagh\_compute\_z

*Computes Z, where z is w \* lambda.*

---

**Description**

Computes Z, where z is w \* lambda.

**Usage**

```
McCullagh_compute_z(lambda, w)
```

**Arguments**

lambda	cumulative logits
w	weights to apply to the logits

**Value**

z, sum pf product of lambda

**McCullagh\_conditional\_symmetry***Fits the McCullagh (1978) conditional-symmetry model.***Description**

McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. *Biometrika*, 65(2) 413-418.

**Usage**

```
McCullagh_conditional_symmetry(n, max_iter = 5, verbose = FALSE)
```

**Arguments**

- |          |  |
|----------|--|
| n        | matrix of observed counts                                    |
| max_iter | maximum number of iterations to maximize the log(likelihood) |
| verbose  | should cycle-by-cycle info be printed. Default is FALSE.     |

**Value**

a list containing theta: the asymmetry parameter chisq: chi-square g\_squared: likelihood ratio G^2 df: degrees of freedom

**Examples**

```
McCullagh_conditional_symmetry(vision_data)
```

**McCullagh\_conditional\_symmetry\_compute\_s***Computes sums used in maximizing theta.***Description**

Computes sums used in maximizing theta.

**Usage**

```
McCullagh_conditional_symmetry_compute_s(n)
```

**Arguments**

- |   |                           |
|---|---------------------------|
| n | matrix of observed counts |
|---|---------------------------|

**Value**

list with s\_i\_plus and s\_plus-i

---

McCullagh\_conditional\_symmetry\_initialize\_phi  
Initializes symmetry matrix phi

---

**Description**

Initializes symmetry matrix phi

**Usage**

McCullagh\_conditional\_symmetry\_initialize\_phi(M)

**Arguments**

M                   the number of rows/columns in phi

**Value**

the phi matrix

---

McCullagh\_conditional\_symmetry\_maximize\_phi  
Maximizes log(likelihood) wrt phi.

---

**Description**

Maximizes log(likelihood) wrt phi.

**Usage**

McCullagh\_conditional\_symmetry\_maximize\_phi(n)

**Arguments**

n                   matrix of observed counts

**Value**

phi matrix

**McCullagh\_conditional\_symmetry\_maximize\_theta**

*Maximizes the log(likelihood) wrt theta.*

### Description

Maximizes the log(likelihood) wrt theta.

### Usage

`McCullagh_conditional_symmetry_maximize_theta(n)`

### Arguments

`n` matrix of observed counts

### Value

value of asymmetry parameter theta

**McCullagh\_conditional\_symmetry\_pi**

*Computes model-based proportions.*

### Description

Computes model-based proportions.

### Usage

`McCullagh_conditional_symmetry_pi(phi, theta)`

### Arguments

`phi` the symmetric matrix

`theta` the asymmetry parameter

### Value

matrix of model-based p-values

---

McCullagh\_derivative\_condition\_wrt\_psi

*Derivative of the condition wrt  $\psi[i, j]$ .*

---

### Description

Derivative of the condition wrt  $\psi[i, j]$ .

### Usage

`McCullagh_derivative_condition_wrt_psi(i, j)`

### Arguments

i	first index of $\psi$
j	second index of $\psi$

### Value

derivative

---

---

McCullagh\_derivative\_gamma\_plus\_1\_wrt\_phi

*Derivative of  $\gamma_j + 1$  wrt  $\phi$ .*

---

### Description

Derivative of  $\gamma_j + 1$  wrt  $\phi$ .

### Usage

`McCullagh_derivative_gamma_plus_1_wrt_phi(gamma, j, phi)`

### Arguments

gamma	vector
j	index of gamma to take derivative of
phi	scalar phi taking derivative wrt

### Value

derivative

**McCullagh\_derivative\_gamma\_wrt\_phi**  
*Derivative of gamma wrt phi.*

### Description

Version given in McCullagh isn't right.

### Usage

`McCullagh_derivative_gamma_wrt_phi(gamma, j, phi)`

### Arguments

<code>gamma</code>	vector of cumulative logits
<code>j</code>	index of derivative sought
<code>phi</code>	scalar phi taking derivative wrt

### Value

derivative

**McCullagh\_derivative\_gamma\_wrt\_y**  
*Derivative of y wrt gamma.*

### Description

Assumes a logit link is being used.

### Usage

`McCullagh_derivative_gamma_wrt_y(gamma, i, j)`

### Arguments

<code>gamma</code>	matrix of gamma values
<code>i</code>	row index of gamma
<code>j</code>	column index of gamma

### Value

derivative

---

```
McCullagh_derivative_lagrangian_wrt_delta
```

*Derivative of Lagrange multiplier wrt scalar delta.*

---

### Description

Derivative of Lagrange multiplier wrt scalar delta.

### Usage

```
McCullagh_derivative_lagrangian_wrt_delta(n, psi, delta, alpha, c = 1)
```

### Arguments

n	matrix of observed counts
psi	symmetry matrix
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing coefficient so that sum o pi = 1. Default value is 1.0

### Value

value of the derivative

---

```
McCullagh_derivative_lagrangian_wrt_delta_vec
```

*Derivative of Lagrangian wrt delta\_vec.*

---

### Description

Derivative of Lagrangian wrt delta\_vec.

### Usage

```
McCullagh_derivative_lagrangian_wrt_delta_vec(  
  n,  
  k,  
  psi,  
  delta_vec,  
  alpha,  
  c = 1  
)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec to compute derivative wrt
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_derivative\_lagrangian\_wrt\_psi***Derivative of Lagrangian wrt psi[i1, j1].***Description**

Derivative of Lagrangian wrt psi[i1, j1].

**Usage**`McCullagh_derivative_lagrangian_wrt_psi(n, i1, j1, psi, delta, alpha, c = 1)`**Arguments**

n	matrix of observed counts
i1	first index of psi
j1	first index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_derivative\_log\_l\_wrt\_alpha**  
*Derivative of log(likelihood) wrt alpha[index].*

**Description**

Derivative of log(likelihood) wrt alpha[index].

**Usage**

```
McCullagh_derivative_log_l_wrt_alpha(n, index, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_derivative\_log\_l\_wrt\_beta**  
*Derivative of log(likelihood) wrt beta, as given in appendix of McCullagh.*

**Description**

McCullagh, P. (1980). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142. With assist from appendix of Agresti, (1984). Agresti, A. (1984). Analysis of ordinal categorical data. New York, Wiley, p. 244-246.

**Usage**

```
McCullagh_derivative_log_l_wrt_beta(n, x, gamma)
```

**Arguments**

n	matrix of observed counts
x	design matrix for location
gamma	matrix of model-based cumulative logits

**Value**

```
derivative
```

---

**McCullagh\_derivative\_log\_l\_wrt\_c**

*Derivative of log(likelihood) wrt c.*

---

**Description**

Derivative of log(likelihood) wrt c.

**Usage**

```
McCullagh_derivative_log_l_wrt_c(n, psi, delta, alpha, c)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

```
derivative
```

---

**McCullagh\_derivative\_log\_l\_wrt\_delta**

*Derivative of log(likelihood) wrt delta (scalar or vector0.*

---

**Description**

Derivative of log(likelihood) wrt delta (scalar or vector0.

**Usage**

```
McCullagh_derivative_log_l_wrt_delta(n, psi, delta, alpha, c = 1, k = 1)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.
k	index into delta_vec. Defaults to 1.

**Value**

derivative

McCullagh\_derivative\_log\_l\_wrt\_delta\_vec  
*Derivative of log(likelihood) wrt delta\_vec[k].*

**Description**

Derivative of log(likelihood) wrt delta\_vec[k].

**Usage**

McCullagh\_derivative\_log\_l\_wrt\_delta\_vec(n, k, psi, delta\_vec, alpha, c = 1)

**Arguments**

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_derivative\_log\_l\_wrt\_params**  
*Derivative of log(likelihood) wrt parameters.*

### Description

Derivative of log(likelihood) wrt parameters.

### Usage

`McCullagh_derivative_log_l_wrt_params(n, x, beta)`

### Arguments

n	matrix of observed counts
x	design matrix for location model
beta	vector of regression parameters for location model

### Value

gradient vector

**McCullagh\_derivative\_log\_l\_wrt\_phi**  
*Derivative of log(likelihood) wrt phi[i, j]*

### Description

Derivative of log(likelihood) wrt phi[i, j]

### Usage

`McCullagh_derivative_log_l_wrt_phi(n, phi, i, j)`

### Arguments

n	matrix of observed counts
phi	matrix of phi-values
i	row index of phi
j	column index of phi

### Value

derivative

**McCullagh\_derivative\_log\_l\_wrt\_psi**  
*Derivative of log(likelihood) wrt psi.*

**Description**

Derivative of log(likelihood) wrt psi.

**Usage**

```
McCullagh_derivative_log_l_wrt_psi(n, i1, j1, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_derivative\_omega\_wrt\_alpha**  
*Derivative of Lagrange multiplier omega wrt alpha[index].*

**Description**

Derivative of Lagrange multiplier omega wrt alpha[index].

**Usage**

```
McCullagh_derivative_omega_wrt_alpha(n, index, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_omega\_wrt\_c

*Derivative of Lagrange multiplier omega wrt c.*

---

**Description**

Derivative of Lagrange multiplier omega wrt c.

**Usage**

McCullagh\_derivative\_omega\_wrt\_c(n, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_omega\_wrt\_delta

*Derivative of Lagrange multiplier omega wrt scalar delta.*

---

**Description**

Derivative of Lagrange multiplier omega wrt scalar delta.

**Usage**

McCullagh\_derivative\_omega\_wrt\_delta(n, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

**McCullagh\_derivative\_omega\_wrt\_delta\_vec**

*Derivative of Lagrange multiplier omega wrt vector delta[k].*

---

**Description**

Derivative of Lagrange multiplier omega wrt vector delta[k].

**Usage**

```
McCullagh_derivative_omega_wrt_delta_vec(n, k, psi, delta_vec, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

**McCullagh\_derivative\_omega\_wrt\_psi**

*Derivative of Lagrange multiplier omega wrt psi[i, j].*

---

**Description**

Derivative of Lagrange multiplier omega wrt psi[i, j].

**Usage**

```
McCullagh_derivative_omega_wrt_psi(n, i, j, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
i	first index of psi
j	second index of psi
psi	symmetry matrix
delta	scalar or vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Defaults to 1.0

## McCullagh\_derivative\_phi\_wrt\_gamma

*Derivative of phi wrt gamma.***Description**

Derivative of phi wrt gamma.

**Usage**

McCullagh\_derivative\_phi\_wrt\_gamma(gamma, j)

**Arguments**

gamma	vector of gamma values
j	index of gamma for which to compute the derivative

**Value**

derivative

## McCullagh\_derivative\_pij\_wrt\_alpha

*Derivative of pij[i, j] wrt alpha[index]***Description**

Derivative of pij[i, j] wrt alpha[index]

**Usage**

McCullagh\_derivative\_pij\_wrt\_alpha(i, j, index, psi, delta, alpha, c = 1)

**Arguments**

i	row index of pij
j	column index of pij
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant to make pi sum to 1.0. Default ot 1.0

**Value**

derivative

**McCullagh\_derivative\_pij\_wrt\_c***Derivative pij[i, j] wrt c.***Description**

Derivative pij[i, j] wrt c.

**Usage**

McCullagh\_derivative\_pij\_wrt\_c(i, j, psi, delta, alpha, c)

**Arguments**

i	row index of pij
j	column index of pij
psi	matrix of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant to make pi sum to 1.0

**Value**

derivative

`McCullagh_derivative_pij_wrt_delta`

*Derivative of  $p_{ij}[i, j]$  wrt scalar delta.*

### Description

Derivative of  $p_{ij}[i, j]$  wrt scalar delta.

### Usage

```
McCullagh_derivative_pij_wrt_delta(i, j, psi, delta, alpha, c = 1)
```

### Arguments

i	row index of $p_{ij}$
j	column index of $p_{ij}$
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing constant so that $\pi$ sum to 1.0. Default value is 1.0

### Value

derivative

`McCullagh_derivative_pij_wrt_delta_vec`

*Derivative  $p_{ij}[i,j]$  wrt vector  $\delta[k]$ .*

### Description

Derivative  $p_{ij}[i,j]$  wrt vector  $\delta[k]$ .

### Usage

```
McCullagh_derivative_pij_wrt_delta_vec(i, j, k, psi, delta_vec, alpha, c = 1)
```

### Arguments

i	row index of $p_{ij}$
j	column index of $p_{ij}$
k	index of $\delta$
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

list containing matrices pij and qij

**McCullagh\_derivative\_pij\_wrt\_psi**

*Derivative of  $p_{ij}[a, b]$  wrt  $\psi[h, k]$*

**Description**

Derivative of  $p_{ij}[a, b]$  wrt  $\psi[h, k]$

**Usage**

```
McCullagh_derivative_pij_wrt_psi(a, b, h, k, delta, alpha, c = 1)
```

**Arguments**

a	row index of pi
b	column index of pi
h	row index of phi
k	column index of phi
delta	scalar or vector version of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant for to make pi sum to 1. Defaults to 1.0

**Value**

derivative

**McCullagh\_derivative\_pi\_wrt\_alpha**

*Derivative of  $\pi[i, j]$  wrt  $\alpha[index]$ .*

**Description**

Derivative of  $\pi[i, j]$  wrt  $\alpha[index]$ .

**Usage**

```
McCullagh_derivative_pi_wrt_alpha(i, j, index, psi, delta, alpha, c = 1)
```

**Arguments**

i	row index of pi
j	column index of pi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

**McCullagh\_derivative\_pi\_wrt\_c***Derivative pi[i, j] wrt c.***Description**

Derivative pi[i, j] wrt c.

**Usage**`McCullagh_derivative_pi_wrt_c(i, j, psi, delta, alpha, c)`**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar or vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

**Value**

derivative

---

McCullagh\_derivative\_pi\_wrt\_delta

*Derivative of pi[i, j] wrt delta.*

---

### Description

Derivative of pi[i, j] wrt delta.

### Usage

```
McCullagh_derivative_pi_wrt_delta(i, j, psi, delta, alpha, c = 1)
```

### Arguments

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

derivative

---



---

McCullagh\_derivative\_pi\_wrt\_delta\_vec

*Derivative pi[i, j] wrt delta[k].*

---

### Description

Derivative pi[i, j] wrt delta[k].

### Usage

```
McCullagh_derivative_pi_wrt_delta_vec(i, j, k, psi, delta_vec, alpha, c = 1)
```

### Arguments

i	row index of pi
j	column index of pi
k	index of delta_vec
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

```
derivative
```

---

**McCullagh\_derivative\_pi\_wrt\_psi**

*Derivative of pi[i, j] wrt psi[i1, j1].*

---

**Description**

Derivative of pi[i, j] wrt psi[i1, j1].

**Usage**

```
McCullagh_derivative_pi_wrt_psi(i, j, i1, j1, psi, delta, alpha, c = 1)
```

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

```
derivative
```

---

**McCullagh\_extract\_weights**

*Extracts the weights to convert cumulative model-based probabilities to regular probabilities.*

---

**Description**

Extracts the weights to convert cumulative model-based probabilities to regular probabilities.

**Usage**

```
McCullagh_extract_weights(i, j, M)
```

**Arguments**

- i row index sought
- j column index sought
- M the number of rows/columns in observed matrix

**Value**

a list containing w\_psi for when i == j w\_pij for when i < j w\_qij for when j < i weight populated with correct entry based on actual i and j

**McCullagh\_fit\_location\_regression\_model**

*Fit location model*

**Description**

Fit location model

**Usage**

```
McCullagh_fit_location_regression_model(n, x, max_iter = 5, verbose = FALSE)
```

**Arguments**

- n matrix of observed counts
- x design matrix for regression model
- max\_iter maximum number of Fisher scoring iterations
- verbose logical: should cycle-by-cycle info be printed out? Default value is FALSE, do not print

**Value**

a list containing beta: regression parameter estimates se: matrix of estimated standard errors cov: covariance matrix of parameter estimates g\_squared: G^2 likelihood ratio chi-square for model chisq: Pearson chi-square for model df: degrees of freedom

**McCullagh\_generalized\_palindromic\_symmetry***Generalized version of palindromic symmetry model*

---

**Description**

delta now is a vector, varying by index McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. Biometrika, 65(2). 413-416.

**Usage**

```
McCullagh_generalized_palindromic_symmetry(
  n,
  max_iter = 15,
  verbose = FALSE,
  start_values = FALSE
)
```

**Arguments**

n	matrix of observed counts
max_iter	maximum number of iterations to maximize log(likelihood)
verbose	should cycle-by-cycle information be printed out? Default is FALSE, do not print
start_values	logical should the regular palindromic symmetry model be fit first to get good starting values. Default is FALSE.

**Value**

a list containing  
 a list containing delta: the vector of asymmetry parameter delta sigma\_delta: vector of SE(delta)  
 logL: value of log(likelihood) for final estimates chisq: Pearson chi-square for solution df: degrees of freedom for solution chisq psi: matrix of symmetry parameters alpha: c: constraint, sum of pi - values condition: constraint on psi to make model identified, Lagrange multiplier SE: vector of standard errors for all parameters

**Examples**

```
McCullagh_generalized_palindromic_symmetry(vision_data)
```

**McCullagh\_generalized\_pij\_qij**

*Computes culiative model probabilities for the generalized model using vector delta.*

**Description**

Computes culiative model probabilities for the generalized model using vector delta.

**Usage**

```
McCullagh_generalized_pij_qij(i, j, psi, delta_vec, alpha, c1 = 1)
```

**Arguments**

i	row index
j	column index
psi	symmetry matrix
delta_vec	vector of delta values
alpha	vector of asymmetry values
c1	normalizing value for pi. Defaults to 1.0

**Value**

model-based cumulative probability pi\_ij

**McCullagh\_generate\_names**

*Generates names to label the parameters.*

**Description**

Generates names to label the parameters.

**Usage**

```
McCullagh_generate_names(psi, delta, alpha, c)
```

**Arguments**

psi	matrix of symmetry parameters
delta	scalar or matrix of asymmetry parameters
alpha	vector of asymmetry parameters
c	scling factor to ensure sup of pi is 1.0

**Value**

character vector of labels for the SE values

---

**McCullagh\_get\_statistics**

*Computes summary statistics needed to compute estimate of delta.*

---

**Description**

Computes summary statistics needed to compute estimate of delta.

**Usage**

```
McCullagh_get_statistics(m)
```

**Arguments**

m matrix of observed counts

**Value**

a list containing: N: matrix of sums above and below the diagonal n: vector, size of binomial r: vector, observed sums, number of successes for binomial

---

**McCullagh\_gradient\_log\_1**

*Gradient vector of log(likelihood)*

---

**Description**

Gradient vector of log(likelihood)

**Usage**

```
McCullagh_gradient_log_1(n, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar or vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

gradient vector of first-order partials wrt log(likelihood0)

---

McCullagh\_hessian\_log\_1  
*Hessian matrix of log(likelihood)*

---

**Description**

Hessian matrix of log(likelihood)

**Usage**

```
McCullagh_hessian_log_1(n, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar or vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

hessian matrix of second-order partials wrt log(likelihood0)

---

---

McCullagh\_initialize\_beta  
*Initializes the beta vector.*

---

**Description**

Initializes the beta vector.

**Usage**

```
McCullagh_initialize_beta(n, c, v)
```

**Arguments**

n	matrix of observed counts
c	number of score levels in table
v	number of levels of beta beyond c

**Value**

initialized beta vector

---

**McCullagh\_initialize\_delta**

*Compute initial values for scalar delta*

---

**Description**

Compute initial values for scalar delta

**Usage**

`McCullagh_initialize_delta(n)`

**Arguments**

`n` matrix of observed counts

**Value**

value of delta

---

**McCullagh\_initialize\_delta\_vec**

*Initialize vector delta*

---

**Description**

Initialize vector delta

**Usage**

`McCullagh_initialize_delta_vec(n)`

**Arguments**

`n` matrix of observed counts

**Value**

vector of delta values

---

**McCullagh\_initialize\_psi**

*Initialize the symmetry matrix psi*

---

**Description**

Initialize the symmetry matrix psi

**Usage**

```
McCullagh_initialize_psi(n, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
delta	scalar delta value
alpha	vector of asymmetry parameters
c	normalizing value of pi. Default is 1.0

**Value**

matrix psi

---

**McCullagh\_initialize\_x**

*Initialize design matrix for location model.*

---

**Description**

This is the simplest possible implementation, that fits thresholds and a single group contrast. More complex problems will implement the matrix X themselves.

**Usage**

```
McCullagh_initialize_x(s, c, v)
```

**Arguments**

s	number of levels of stratification variable
c	number of score levels
v	number of predictors above thresholds

**Value**

design matrix X

**McCullagh\_is\_in\_constraint\_set**

*Logical test of whether a specific psi will be in the constraint set.*

**Description**

Logical test of whether a specific psi will be in the constraint set.

**Usage**

```
McCullagh_is_in_constraint_set(i, j)
```

**Arguments**

- |   |                     |
|---|---------------------|
| i | first index of psi  |
| j | second index of psi |

**Value**

TRUE if it falls within the set, FALSE otherwise.

**McCullagh\_is\_pi\_invalid**

*Test whether pi matrix is valid, i.e.,  $0 < \text{all values}$ .*

**Description**

Test whether pi matrix is valid, i.e.,  $0 < \text{all values}$ .

**Usage**

```
McCullagh_is_pi_invalid(pi)
```

**Arguments**

- |    |                                   |
|----|-----------------------------------|
| pi | matrix of pi values to be tested. |
|----|-----------------------------------|

**Value**

TRUE if all  $\pi_i > 0$ , FALSE otherwise.

---

**McCullagh\_logistic\_model**  
*McCullagh's logistic model.*

---

**Description**

McCullagh, P. (1977). A logistic model for paired comparisons with ordered categorical data. *Biometrika*, 64(3), 449-453.

**Usage**

```
McCullagh_logistic_model(m)
```

**Arguments**

<code>m</code>	matrix of observed counts
----------------	---------------------------

**Value**

a list containing w\_tilde: vector of model weights for sum of normally distributed components  
 delta\_tilde: delta parameter computed using w\_tilde  
 w\_star: vector of weights for Mantel-Haenszel type numerator and denominator  
 delta\_star: delta parameter computed using w\_star  
 var: variance of delta estimate

**Examples**

```
McCullagh_logistic_model(coal_g)
```

---

**McCullagh\_logits**      *Computed cumulative logits.*

---

**Description**

Computed cumulative logits.

**Usage**

```
McCullagh_logits(cumulative, use_half = TRUE)
```

**Arguments**

<code>cumulative</code>	vector of cumulative counts
<code>use_half</code>	logical indicating whether or not to add 0.5 to numerator and denominator counts before computing logits, Default value is TRUE, add 0.5.

---

McCullagh_log_L	<i>Computes the log(likelihood).</i>
-----------------	--------------------------------------

---

**Description**

Computes the log(likelihood).

**Usage**

```
McCullagh_log_L(n, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar or vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh_maximize_q_symmetry	<i>Maximize the log(likelihood) wrt parameters phi and alpha</i>
-------------------------------	--

---

**Description**

Maximize the log(likelihood) wrt parameters phi and alpha

**Usage**

```
McCullagh_maximize_q_symmetry(n, phi, alpha)
```

**Arguments**

n	matrix of observed counts
phi	matrix of symmetry parameters
alpha	vector of asymmetry parameters

**Value**

list with new values of phi and alpha

---

McCullagh\_newton\_raphson\_update  
*Newton-Raphson update.*

---

## Description

Using gradient and hessian, it finds the update direction. Then it tries increasingly smaller step sizes until the step\*update yields a valid pi matrix.

## Usage

```
McCullagh_newton_raphson_update(  
  n,  
  gradient,  
  hessian,  
  psi,  
  delta,  
  alpha,  
  c = 1,  
  max_iter = 50,  
  verbose = FALSE  
)
```

## Arguments

n	matrix of observed counts
gradient	gradient vector
hessian	hessian matrix
psi	matrix of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	scaling factor to ensure pi sums to 1.0. Default is 1.0
max_iter	maximum number of iterations. Default is 50.
verbose	should cycle-by-cycle info be printed out. Default is FALSE, do not print.

## Value

list containing new parameters psi: matrix of symmetry parameters delta; scalar or vector of asymmetry parameters alpha: vector of asymmetry parameters c: scaling coefficient to ensure pi sums to 1.0

**McCullagh\_palindromic\_symmetry***McCullagh's palindromic symmetry model***Description**

McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. *Biometrika*, 65(2). 413-416.

**Usage**

```
McCullagh_palindromic_symmetry(n, max_iter = 15, verbose = FALSE)
```

**Arguments**

n	matrix of observed counts
max_iter	maximum number of iterations to maximize the log(likelihood)
verbose	should cycle-by-cycle info be printed out? Default is FALSE, don't print.

**Value**

a list containing delta: the value of the asymmetry parameter sigma\_delta: SE(delta) logL: value of log(likelihood) for final estimates chisq: Pearson chi-square for solution df: degrees of freedom for solution chisq psi: matrix of symmetry parameters alpha: c: constraint, sum of pi - values condition: constraint on psi to make model identified, Lagrange multiplier SE: vector of standard errors for all parameters

**Examples**

```
McCullagh_palindromic_symmetry(vision_data)
```

**McCullagh\_penalized***Computes the penalized value of a derivative by adding the derivative of the penalty to it.***Description**

Computes the penalized value of a derivative by adding the derivative of the penalty to it.

**Usage**

```
McCullagh_penalized(derivative, i1, j1, n, psi, delta, alpha, c = 1)
```

**Arguments**

derivative	the base derivative
i1	first index of psi
j1	second index of psi
n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

McCullagh\_pij\_qij      *Compute model-based cumulative probabilities*

**Description**

Compute model-based cumulative probabilities

**Usage**

McCullagh\_pij\_qij(i, j, psi, delta, alpha, c = 1)

**Arguments**

i	row index
j	column index
psi	the symmetry matrix
delta	the asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for pi. Default is 1.0

**Value**

the model-based cumulative probability pi\_ij

**McCullagh\_proportional\_hazards**  
*Computes the proportional hazards.*

### Description

Computes the proportional hazards.

### Usage

```
McCullagh_proportional_hazards(n)
```

### Arguments

n matrix of observed counts

### Value

```
loga(-log(survival))
```

**McCullagh\_quasi\_symmetry**  
*Fits McCullagh's (1978) quasi-symmetry model.*

### Description

McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. *Biometrika*, 65(2) 413-418.

### Usage

```
McCullagh_quasi_symmetry(n, max_iter = 15, verbose = FALSE)
```

### Arguments

n	matrix of observed counts
max_iter	maximum number of iterations in maximizing log(likelihood), Default is 15.
verbose	should cycle-by-cycle information be printed out? Default is FALSE, do not print

### Value

a list containing phi: symmetry matrix alpha: vector of asymmetry parameters chisq: Pearson chi-square value df: degrees of freedom

### Examples

```
McCullagh_quasi_symmetry(vision_data)
```

---

McCullagh\_q\_symmetry\_initialize\_alpha  
Initializes the asymmetry vector alpha

---

**Description**

Initializes the asymmetry vector alpha

**Usage**

McCullagh\_q\_symmetry\_initialize\_alpha(M)

**Arguments**

M size of alpha vector to create = nrow(matrix to analyze)

**Value**

vector of asymmetry parameters alpha

---

---

McCullagh\_q\_symmetry\_initialize\_phi  
Initializes the phi matrix

---

**Description**

Initializes the phi matrix

**Usage**

McCullagh\_q\_symmetry\_initialize\_phi(M)

**Arguments**

M size of the psi matrix to create

**Value**

the symmetry matrix phi

**McCullagh\_q\_symmetry\_pi***Computes the model-based p-values***Description**

Computes the model-based p-values

**Usage**

McCullagh\_q\_symmetry\_pi(phi, alpha)

**Arguments**

- phi                the matrix of symmetry parameters
- alpha              the vector of asymmetry parameters

**Value**

matrix pi of model-based p-values

**McCullagh\_second\_order\_lagrangian\_wrt\_psi\_2***Second derivative of Lagrangian wrt psi^2.***Description**

Second derivative of Lagrangian wrt psi^2.

**Usage**

```
McCullagh_second_order_lagrangian_wrt_psi_2(
  n,
  i1,
  j1,
  i2,
  j2,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	first row index of psi
j1	first column index of psi
i2	second row index of psi
j2	second column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_lagrangian\_wrt\_psi\_alpha***Second derivative of Lagrangian wrt psi[i1, j1] and alpha[index].***Description**

Second derivative of Lagrangian wrt psi[i1, j1] and alpha[index].

**Usage**

```
McCullagh_second_order_lagrangian_wrt_psi_alpha(
  n,
  i1,
  j1,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
index	second row index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

*McCullagh\_second\_order\_lagrangian\_wrt\_psi\_delta*

*Second derivative of Lagrangian wrt psi[i1, j1] and delta.*

**Description**

Second derivative of Lagrangian wrt psi[i1, j1] and delta.

**Usage**

```
McCullagh_second_order_lagrangian_wrt_psi_delta(
  n,
  i1,
  j1,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_lagrangian\_wrt\_psi\_delta\_vec

*Second derivative of Lagrangian wrt psi[i1, j1] and delta\_vec[k].*

---

## Description

Second derivative of Lagrangian wrt psi[i1, j1] and delta\_vec[k].

## Usage

```
McCullagh_second_order_lagrangian_wrt_psi_delta_vec(  
    n,  
    i1,  
    j1,  
    k,  
    psi,  
    delta_vec,  
    alpha,  
    c = 1  
)
```

## Arguments

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

## Value

derivative

McCullagh\_second\_order\_log\_l\_wrt\_alpha\_2

*Second derivative of log(likelihood) wrt alpha^2.*

### Description

Second derivative of log(likelihood) wrt alpha^2.

### Usage

```
McCullagh_second_order_log_l_wrt_alpha_2(
  n,
  index_a,
  index_b,
  psi,
  delta,
  alpha,
  c = 1
)
```

### Arguments

n	matrix of observed counts
index_a	first index of alpha
index_b	second column index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

### Value

derivative

McCullagh\_second\_order\_log\_l\_wrt\_alpha\_c

*Second derivative of log(likelihood) wrt alpha[index] and c.*

### Description

Second derivative of log(likelihood) wrt alpha[index] and c.

**Usage**

```
McCullagh_second_order_log_l_wrt_alpha_c(n, index, psi, delta, alpha, c)
```

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_beta\_2**

*Expected values of second order derivatives of log(likelihood) wrt beta.*

**Description**

Appendix of McCullagh, P. (1980). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142. and appendix B3 of Agresti, A. (1984). Analysis of ordinal categorical data, New York, Wiley, p. 242-244.

**Usage**

```
McCullagh_second_order_log_l_wrt_beta_2(n, x, gamma)
```

**Arguments**

n	matrix of observed counts
x	design matrix for location model
gamma	current value of model-based cumulative logits.

**Value**

matrix of second order partial derivatives

**McCullagh\_second\_order\_log\_l\_wrt\_c\_2**

*Second derivative of log(likelihood) wrt c^2.*

**Description**

Second derivative of log(likelihood) wrt c^2.

**Usage**

```
McCullagh_second_order_log_l_wrt_c_2(n, psi, delta, alpha, c)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_delta\_2**

*Second derivative of log(likelihood) wrt delta^2.*

**Description**

Second derivative of log(likelihood) wrt delta^2.

**Usage**

```
McCullagh_second_order_log_l_wrt_delta_2(n, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

**McCullagh\_second\_order\_log\_l\_wrt\_delta\_alpha**

*Second derivative of log(likelihood) wrt delta and alpha[index].*

---

**Description**

Second derivative of log(likelihood) wrt delta and alpha[index].

**Usage**

```
McCullagh_second_order_log_l_wrt_delta_alpha(  
  n,  
  index,  
  psi,  
  delta,  
  alpha,  
  c = 1  
)
```

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_delta\_c**

*Second derivative of log(likelihood) wrt scalar delta and c.*

### Description

Second derivative of log(likelihood) wrt scalar delta and c.

### Usage

```
McCullagh_second_order_log_l_wrt_delta_c(n, psi, delta, alpha, c)
```

### Arguments

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0..

### Value

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_delta\_vec\_2**

*Second derivative of log(likelihood) wrt delta\_vec^2.*

### Description

Second derivative of log(likelihood) wrt delta\_vec^2.

### Usage

```
McCullagh_second_order_log_l_wrt_delta_vec_2(
  n,
  k1,
  k2,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k1	first index of delta_vec
k2	second index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

McCullagh\_second\_order\_log\_l\_wrt\_delta\_vec\_alpha

*Second derivative of log(likelihood) wrt delta[k] and alpha[index].***Description**

Second derivative of log(likelihood) wrt delta[k] and alpha[index].

**Usage**

```
McCullagh_second_order_log_l_wrt_delta_vec_alpha(
  n,
  k,
  index,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
index	index of alpha
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_delta\_vec\_c**

*Second derivative of log(likelihood) wrt delta\_vec[k] and c.*

**Description**

Second derivative of log(likelihood) wrt delta\_vec[k] and c.

**Usage**

```
McCullagh_second_order_log_l_wrt_delta_vec_c(n, k, psi, delta_vec, alpha, c)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_parms**

*Expected second order derivatives of log(likelihood)*

**Description**

Expected second order derivatives of log(likelihood)

**Usage**

```
McCullagh_second_order_log_l_wrt_parms(n, x, beta)
```

**Arguments**

n	matrix of observed counts
x	design matrix for location model
beta	vector of regression parameters for location model

**Value**

matrix of expected second derivatives

**McCullagh\_second\_order\_log\_l\_wrt\_psi\_2**  
*Second derivative of log(likelihoood) wrt psi^2.*

**Description**

Second derivative of log(likelihoood) wrt psi^2.

**Usage**

```
McCullagh_second_order_log_l_wrt_psi_2(
  n,
  i1,
  j1,
  i2,
  j2,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	first row index of psi
j1	first column index of psi
i2	second row index of psi
j2	second column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_psi\_alpha**

*Second derivative of log(likelihoood) wrt ps[i1, j1] and alpha[index].*

**Description**

Second derivative of log(likelihoood) wrt ps[i1, j1] and alpha[index].

**Usage**

```
McCullagh_second_order_log_l_wrt_psi_alpha(
  n,
  i1,
  j1,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_psi\_c**

*Second derivative of log(likelihood) wrt psi[i1, j1] and c.*

**Description**

Second derivative of log(likelihood) wrt psi[i1, j1] and c.

**Usage**

```
McCullagh_second_order_log_l_wrt_psi_c(n, i1, j1, psi, delta, alpha, c)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_psi\_delta**

*Second derivative of log(likelihood) wrt psi[i1, j1] and scalar delta..*

**Description**

Second derivative of log(likelihood) wrt psi[i1, j1] and scalar delta..

**Usage**

```
McCullagh_second_order_log_l_wrt_psi_delta(n, i1, j1, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_log\_l\_wrt\_psi\_delta\_vec***Second derivative of log(likelihood) wrt psi[i1, j1] and delta\_vec[k].***Description**

Second derivative of log(likelihood) wrt psi[i1, j1] and delta\_vec[k].

**Usage**

```
McCullagh_second_order_log_l_wrt_psi_delta_vec(
  n,
  i1,
  j1,
  k,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
k	second row index of delta
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

**McCullagh\_second\_order\_omega\_wrt\_alpha\_2**

*Second derivative of Lagrange multiplier omega wrt alpha^2.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt alpha^2.

**Usage**

```
McCullagh_second_order_omega_wrt_alpha_2(n, k1, k2, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
k1	first index of alpha
k2	second index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

**McCullagh\_second\_order\_omega\_wrt\_alpha\_c**

*Second derivative of Lagrange multiplier omega wrt alpha[index] and c.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt alpha[index] and c.

**Usage**

```
McCullagh_second_order_omega_wrt_alpha_c(n, index, psi, delta, alpha, c)
```

**Arguments**

n	matrix of observed counts
index	row index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_c\_2***Second derivative of Lagrange multiplier omega wrt c^2.***Description**Second derivative of Lagrange multiplier omega wrt  $c^2$ .**Usage**`McCullagh_second_order_omega_wrt_c_2(n, psi, delta, alpha, c)`**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_delta\_2**

*Second derivative of Lagrange multiplier omega wrt scalae delta^2.*

### Description

Second derivative of Lagrange multiplier omega wrt scalae delta^2.

### Usage

```
McCullagh_second_order_omega_wrt_delta_2(n, psi, delta, alpha, c = 1)
```

### Arguments

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

### Value

derivative

**McCullagh\_second\_order\_omega\_wrt\_delta\_alpha**

*Second derivative of Lagrange multiplier omega wrt delta and alpha[index].*

### Description

Second derivative of Lagrange multiplier omega wrt delta and alpha[index].

### Usage

```
McCullagh_second_order_omega_wrt_delta_alpha(
  n,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

*McCullagh\_second\_order\_omega\_wrt\_delta\_c*

*Second derivative of Lagrange multiplier omega wrt scalar delta and c.*

**Description**

Second derivative of Lagrange multiplier omega wrt scalar delta and c.

**Usage**

```
McCullagh_second_order_omega_wrt_delta_c(n, psi, delta, alpha, c)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_delta\_vec\_2**

*Second derivative of Lagrange multiplier omega wrt delta\_vec^2.*

### Description

Second derivative of Lagrange multiplier omega wrt delta\_vec^2.

### Usage

```
McCullagh_second_order_omega_wrt_delta_vec_2(
  n,
  k1,
  k2,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

### Arguments

n	matrix of observed counts
k1	first index of delta_vec
k2	second index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

### Value

derivative

**McCullagh\_second\_order\_omega\_wrt\_delta\_vec\_alpha**

*Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and alpha[index].*

### Description

Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and alpha[index].

**Usage**

```
McCullagh_second_order_omega_wrt_delta_vec_alpha(
  n,
  k,
  index,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
index	index of alpha
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_delta\_vec\_c**

*Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and c.*

**Description**

Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and c.

**Usage**

```
McCullagh_second_order_omega_wrt_delta_vec_c(n, k, psi, delta_vec, alpha, c)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector of asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

---

**McCullagh\_second\_order\_omega\_wrt\_psi\_2**

*Second derivative of Lagrange multiplier omega wrt psi^2.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt psi^2.

**Usage**

```
McCullagh_second_order_omega_wrt_psi_2(
  n,
  i1,
  j1,
  i2,
  j2,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	first row index of psi
j1	first column index of psi
i2	second row index of psi
j2	second column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_psi\_alpha**

*Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and alpha[index].*

**Description**

Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and alpha[index].

**Usage**

```
McCullagh_second_order_omega_wrt_psi_alpha(
  n,
  i1,
  j1,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_psi\_c**

*Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and c.*

**Description**

Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and c.

**Usage**

```
McCullagh_second_order_omega_wrt_psi_c(n, i1, j1, psi, delta, alpha, c)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_psi\_delta**

*Second derivative of Lagrange multiplier omega wrt psi and scalar delta.*

**Description**

Second derivative of Lagrange multiplier omega wrt psi and scalar delta.

**Usage**

```
McCullagh_second_order_omega_wrt_psi_delta(n, i1, j1, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

**McCullagh\_second\_order\_omega\_wrt\_psi\_delta\_vec**

*Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and delta\_vec[k].*

**Description**

Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and delta\_vec[k].

**Usage**

```
McCullagh_second_order_omega_wrt_psi_delta_vec(
  n,
  i1,
  j1,
  k,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

**McCullagh\_second\_order\_pi\_wrt\_alpha\_2**

*Second derivative of pi[i, j] wrt alpha^2.*

---

**Description**

Second derivative of pi[i, j] wrt alpha^2.

**Usage**

```
McCullagh_second_order_pi_wrt_alpha_2(  
    i,  
    j,  
    index1,  
    index2,  
    psi,  
    delta,  
    alpha,  
    c = 1  
)
```

**Arguments**

i	row index of pi
j	column index of pi
index1	index of first alpha
index2	index of second alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

**McCullagh\_second\_order\_pi\_wrt\_alpha\_c**

*Second derivaitve of pi[i, j] wrt alpha[index] and c.*

**Description**

Second derivaitve of pi[i, j] wrt alpha[index] and c.

**Usage**

```
McCullagh_second_order_pi_wrt_alpha_c(i, j, index, psi, delta, alpha, c)
```

**Arguments**

i	row index of pi
j	column index of pi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

**Value**

derivative

**McCullagh\_second\_order\_pi\_wrt\_c\_2**

*Second order derivative of pi[i, j] wrt c^2.*

**Description**

Second order derivative of pi[i, j] wrt c^2.

**Usage**

```
McCullagh_second_order_pi_wrt_c_2(i, j, psi, delta, alpha, c)
```

**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

```
derivative
```

---

`McCullagh_second_order_pi_wrt_delta_2`

*Second order derivative of pi[i, j] wrt scalar delta.*

---

**Description**

Second order derivative of pi[i, j] wrt scalar delta.

**Usage**

```
McCullagh_second_order_pi_wrt_delta_2(i, j, psi, delta, alpha, c = 1)
```

**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

```
derivative
```

---

`McCullagh_second_order_pi_wrt_delta_alpha`

*Second order derivative of pi[i, j] wrt scalar delta and alpha[index]*

---

**Description**

Second order derivative of pi[i, j] wrt scalar delta and alpha[index]

**Usage**

```
McCullagh_second_order_pi_wrt_delta_alpha(
    i,
    j,
    index,
    psi,
    delta,
    alpha,
    c = 1
)
```

**Arguments**

i	row index of pi
j	column index of pi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

**McCullagh\_second\_order\_pi\_wrt\_delta\_c***Second order derivative of pi[i, j] wrt scalae delta and c.***Description**

Second order derivative of pi[i, j] wrt scalae delta and c.

**Usage**

McCullagh\_second\_order\_pi\_wrt\_delta\_c(i, j, psi, delta, alpha, c)

**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_delta\_vec\_2  
*Derivative of pi[i, j] wrt delta^2.*

---

### Description

Derivative of pi[i, j] wrt delta^2.

### Usage

```
McCullagh_second_order_pi_wrt_delta_vec_2(  
    i,  
    j,  
    k1,  
    k2,  
    psi,  
    delta_vec,  
    alpha,  
    c = 1  
)
```

### Arguments

i	row index of pi
j	column index of pi
k1	first index of delta
k2	second index of delta
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

derivative

---

McCullagh\_second\_order\_pi\_wrt\_delta\_vec\_alpha

*Second order derivative of pi[i, j] wrt delta[k] alpha[index].*

---

## Description

Second order derivative of pi[i, j] wrt delta[k] alpha[index].

## Usage

```
McCullagh_second_order_pi_wrt_delta_vec_alpha(
    i,
    j,
    k,
    index,
    psi,
    delta_vec,
    alpha,
    c = 1
)
```

## Arguments

i	row index of pi
j	column index of pi
k	index of delta
index	index of alpha
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

## Value

derivative

`McCullagh_second_order_pi_wrt_delta_vec_c`

*Second derivative of pi[i, j] wrt delta[k] and c.*

### Description

Second derivative of pi[i, j] wrt delta[k] and c.

### Usage

```
McCullagh_second_order_pi_wrt_delta_vec_c(i, j, k, psi, delta_vec, alpha, c)
```

### Arguments

i	row index of pi
j	column index of pi
k	index of delta
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

derivative

`McCullagh_second_order_pi_wrt_psi_2`

*Second order derivative wrt psi^2.*

### Description

Second order derivative wrt psi^2.

### Usage

```
McCullagh_second_order_pi_wrt_psi_2(
  i,
  j,
  i1,
  j1,
  i2,
  j2,
  psi,
```

```

    delta,
    alpha,
    c = 1
)

```

**Arguments**

i	row index of pi
j	column index of pi
i1	first row index of psi
j1	first column index of psi
i2	second row index of psi
j2	second column index of pis
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

**McCullagh\_second\_order\_pi\_wrt\_psi\_alpha**

*Second order derivative of pi[i, j] wrt psi[i1, j1] and alpha[index].*

**Description**

Second order derivative of pi[i, j] wrt psi[i1, j1] and alpha[index].

**Usage**

```

McCullagh_second_order_pi_wrt_psi_alpha(
    i,
    j,
    i1,
    j1,
    index,
    psi,
    delta,
    alpha,
    c = 1
)

```

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

**McCullagh\_second\_order\_pi\_wrt\_psi\_c***Second order derivative of pi[i, j] wrt psi[i1, j1] and c.***Description**

Second order derivative of pi[i, j] wrt psi[i1, j1] and c.

**Usage**

McCullagh\_second\_order\_pi\_wrt\_psi\_c(i, j, i1, j1, psi, delta, alpha, c)

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_psi\_delta

*Second order derivaitve of pi wrt pshi and scalar delta.*

---

### Description

Second order derivaitve of pi wrt pshi and scalar delta.

### Usage

```
McCullagh_second_order_pi_wrt_psi_delta(i, j, i1, j1, psi, delta, alpha, c = 1)
```

### Arguments

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

derivative

---

McCullagh\_second\_order\_pi\_wrt\_psi\_delta\_vec

*Second order derivaitve of pi[i, j] wrt psi[i1, j1] and kelta[k].*

---

### Description

Second order derivaitve of pi[i, j] wrt psi[i1, j1] and kelta[k].

**Usage**

```
McCullagh_second_order_pi_wrt_psi_delta_vec(  
    i,  
    j,  
    i1,  
    j1,  
    k,  
    psi,  
    delta_vec,  
    alpha,  
    c = 1  
)
```

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
k	index of delta
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

**McCullagh\_update\_parameters**

*Update the parameters based on Newton-Raphson step.*

---

**Description**

Update the parameters based on Newton-Raphson step.

**Usage**

```
McCullagh_update_parameters(update, step, psi, delta, alpha, c = 1)
```

**Arguments**

update	vector of update values
step	size of candidate step along direction of update
psi	vector of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalization factor to make sum of pi = 1.0. Default value is 1.0.

**Value**

list containing new parameters psi: matrix of symmetry parameters delta; scalar or vector of asymmetry parameters alpha: vector of asymmetry parameters c: scaling coefficient to ensure pi sums to 1.0

**McCullagh\_v\_inverse**    *Compute v\_inverse (from appendix).*

**Description**

Compute v\_inverse (from appendix).

**Usage**

```
McCullagh_v_inverse(gamma, i, j)
```

**Arguments**

gamma	matrix of cumulative logits
i	row index
j	column index

**Value**

$V^{-1} : d\phi / d\gamma_{ij}$

---

mental_health	<i>Relationship between child's mental health and parents' socioeconomic status.</i>
---------------	--

---

**Description**

Rows are child's mental health (ranging from 1 = well to 4 = impaired), and columns are parents' socioeconomic status, A - F.

**Usage**

```
mental_health
```

**Format**

```
## 'mental_health' A matrix with 4 rows and 6 columns
```

**Source**

Goodman, L. A. (1979). Simple models for the analysis of association in cross-classifications having ordered categories.

---

model_ii_effects	<i>Gets the effects phi, ksi_i_dot and ksi_dot_j for Model II results.</i>
------------------	--

---

**Description**

Gets the effects phi, ksi\_i\_dot and ksi\_dot\_j for Model II results.

**Usage**

```
model_ii_effects(result)
```

**Arguments**

result	a result object from Model II
--------	-------------------------------

**Value**

a list containing: phi: the overall effect ksi\_i\_dot: the row effects ksi\_dot\_j: the column effects

<code>model_ii_fHat</code>	<i>Computes expected counts for Model II</i>
----------------------------	--

### Description

Computes expected counts for Model II

### Usage

```
model_ii_fHat(alpha, beta, rho, sigma)
```

### Arguments

<code>alpha</code>	row effects
<code>beta</code>	column effects
<code>rho</code>	row locations
<code>sigma</code>	column locations

### Value

matrix of model-based expected counts

<code>model_ii_ksi</code>	<i>Gets the effects phi, ksi_i_dot and ksi_dot_j for Model II matrix of odds-ratios.</i>
---------------------------	--

### Description

Gets the effects phi, ksi\_i\_dot and ksi\_dot\_j for Model II matrix of odds-ratios.

### Usage

```
model_ii_ksi(odds)
```

### Arguments

<code>odds</code>	matrix of adjacent odds-ratios
-------------------	--------------------------------

### Value

a list containing: `phi`: the overall effect in log metric  
`ksi_i_dot`: the row effects  
`ksi_dot_j`: the column effects

---

```
model_ii_starting_values
```

*Computes crude starting values for Model II*

---

### Description

Computes crude starting values for Model II

### Usage

```
model_ii_starting_values(n)
```

### Arguments

n matrix of observed counts

### Value

a list containing alpha: vector of row parameters beta: vector of column parameters rho: row coefficients sigma: column coefficients mu: alternative row coefficients nu: alternative column coefficients

---

---

```
model_ii_star_effects Gets the effects for Model II*
```

---

### Description

Gets the effects for Model II\*

### Usage

```
model_ii_star_effects(result)
```

### Arguments

result a Model II\* result object

### Value

a list containing phi: common effect in log metric ksi: vector of ksi parameters

`model_ii_star_fHat`      *Computes expected counts for Model II\**

### Description

Computes expected counts for Model II\*

### Usage

```
model_ii_star_fHat(alpha, beta, phi)
```

### Arguments

<code>alpha</code>	row effects
<code>beta</code>	column effects
<code>phi</code>	row/column locations

### Value

matrix of model-based expected counts

`model_ii_star_update_phi`  
Updates estimate of phi vector

### Description

Updates estimate of phi vector

### Usage

```
model_ii_star_update_phi(n, fHat, mu, phi, exclude_diagonal = FALSE)
```

### Arguments

<code>n</code>	matrix of observed counts
<code>fHat</code>	current model-based counts for each cell
<code>mu</code>	alternative row coefficients
<code>phi</code>	vector of column location parameters
<code>exclude_diagonal</code>	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

### Value

list containing: `phi`: updated estimate of the phi vector `mu`: updated estimate of vector `mu`

---

model\_ii\_update\_alpha *Updates the estimate of the alpha vector for Model II*

---

**Description**

Updates the estimate of the alpha vector for Model II

**Usage**

```
model_ii_update_alpha(alpha, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

alpha	current estimate of alpha
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

**Value**

updated estimate of alpha vector

---

model\_ii\_update\_beta *Updates the estimate of the beta vector for Model II*

---

**Description**

Updates the estimate of the beta vector for Model II

**Usage**

```
model_ii_update_beta(beta, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

beta	current estimate of beta
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

**Value**

updated estimate of beta vector

**model\_ii\_update\_rho**     *Updates the estimate of the rho vector for Model II*

### Description

Updates the estimate of the rho vector for Model II

### Usage

```
model_ii_update_rho(n, fHat, mu, sigma, exclude_diagonal = FALSE)
```

### Arguments

n	matrix of observed counts
fHat	current model-based counts for each cell
mu	alternative row coefficients
sigma	vector of column location parameters
exclude_diagonal	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

### Value

updated estimate of alpha vector

**model\_ii\_update\_sigma**     *Updates the estimate of the sigma vector for Model II*

### Description

Updates the estimate of the sigma vector for Model II

### Usage

```
model_ii_update_sigma(n, fHat, nu, rho, exclude_diagonal = FALSE)
```

### Arguments

n	matrix of observed counts
fHat	current model-based counts for each cell
nu	vector of column coefficients
rho	vector of row location parameters
exclude_diagonal	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

**Value**

updated estimate of sigma vector

---

model\_i\_column\_theta    *Computes the column association values theta-hat*

---

**Description**

Computes the column association values theta-hat

**Usage**

model\_i\_column\_theta(fHat)

**Arguments**

fHat                matrix of model-based expected counts

**Value**

thetaHat vector of association parameters

---

model\_i\_effects        *Gets the overall effects for Model I.*

---

**Description**

Gets the overall effects for Model I.

**Usage**

model\_i\_effects(result)

**Arguments**

result                a Model I result object

**Value**

a list containing theta: the overall association zeta\_i\_dot: row effects for association zeta\_dot\_j: column effects for association

`model_i_fHat`*Computes model-based expected cell counts for Model I***Description**

Computes model-based expected cell counts for Model I

**Usage**

```
model_i_fHat(alpha, beta, gamma, delta)
```

**Arguments**

<code>alpha</code>	row effects
<code>beta</code>	column effects
<code>gamma</code>	row location weights
<code>delta</code>	column location weights

**Value**

matrix of model-based expected counts

`model_i_normalize_fHat`

*Normalizes pi(fHat) to sum to 1.0. If exclude\_diagonal is TRUE, the sum of the off-diagonal terms sums to 1.0.*

**Description**

Normalizes pi(fHat) to sum to 1.0. If `exclude_diagonal` is TRUE, the sum of the off-diagonal terms sums to 1.0.

**Usage**

```
model_i_normalize_fHat(fHat, exclude_diagonal = FALSE)
```

**Arguments**

<code>fHat</code>	matrix of model-based cell frequencies
<code>exclude_diagonal</code>	logical. Should the cells on the main diagonal be excluded? Default is FALSE, include all cells

**Value**

matrix of model-based proportions pi

---

```
model_i_row_column_odds_ratios
```

*Computes the table of adjacent odds-ratios theta-hat.*

---

### Description

Computes the table of adjacent odds-ratios theta-hat.

### Usage

```
model_i_row_column_odds_ratios(fHat)
```

### Arguments

fHat                  matrix of model-based expected counts

### Value

thetaHat matrix of adjacent odds-ratios

---

---

```
model_i_row_theta
```

*Computes the row association values theta-hat*

---

### Description

Computes the row association values theta-hat

### Usage

```
model_i_row_theta(fHat)
```

### Arguments

fHat                  matrix of model-based expected counts

### Value

thetaHat vector of association parameters

`model_i_starting_values`

*Computes crude starting values for Model I.*

**Description**

Computes crude starting values for Model I.

**Usage**`model_i_starting_values(n)`**Arguments**

`n` matrix of observed counts

**Value**

a list containing alpha: vector of row parameters  
beta: vector of column parameters  
gamma: vector of row locations  
delta: vector of column locations

`model_i_star_effects` *Gets the Model I\* effects.***Description**

Gets the Model I\* effects.

**Usage**`model_i_star_effects(result)`**Arguments**

`result` a Model I\* effect object

**Value**

a list containing theta: the overall association  
zeta: the row/column effect

`model_i_star_fHat`      *Computes expected frequencies for Model I\**

### Description

Computes expected frequencies for Model I\*

### Usage

```
model_i_star_fHat(alpha, beta, theta)
```

### Arguments

alpha	row effect parameters
beta	column effect parameters
theta	row/column parameters

### Value

matrix of model-based expected cell counts

`model_i_star_update_theta`

*Updates the row/column parameters for Model I\*.*

### Description

Updates the row/column parameters for Model I\*.

### Usage

```
model_i_star_update_theta(theta, n, fHat, exclude_diagonal = FALSE)
```

### Arguments

theta	vector of estimated row/column effects
n	matrix of observed counts
fHat	matrix of model-based expected frequencies
exclude_diagonal	should the cells of the main diagonal be excluded? Default is FALSE, include all cells

### Value

new value of theta vector

`model_i_update_alpha`    *Updates the estimate of the alpha vector for Model I*

### Description

Updates the estimate of the alpha vector for Model I

### Usage

```
model_i_update_alpha(alpha, n, fHat, exclude_diagonal = FALSE)
```

### Arguments

<code>alpha</code>	current estimate of beta
<code>n</code>	matrix of observed counts
<code>fHat</code>	current model-based counts for each cell
<code>exclude_diagonal</code>	logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells.

### Value

updated estimate of alpha vector

`model_i_update_beta`    *Updates the estimate of the beta vector for Model I*

### Description

Updates the estimate of the beta vector for Model I

### Usage

```
model_i_update_beta(beta, n, fHat, exclude_diagonal = FALSE)
```

### Arguments

<code>beta</code>	current estimate of alpha
<code>n</code>	matrix of observed counts
<code>fHat</code>	current model-based counts for each cell
<code>exclude_diagonal</code>	logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells

### Value

updated estimate of beta vector

---

model\_i\_update\_delta    *Updates the estimate of the delta vector for Model I*

---

**Description**

Updates the estimate of the delta vector for Model I

**Usage**

```
model_i_update_delta(delta, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

delta	current estimate of delta
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells

**Value**

updated estimate of delta vector

---

model\_i\_update\_gamma    *Updates the estimate of the gamma vector for Model I*

---

**Description**

Updates the estimate of the gamma vector for Model I

**Usage**

```
model_i_update_gamma(gamma, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

gamma	current estimate of gamma
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells

**Value**

updated estimate of gamma vector

---

<code>model_i_zeta</code>	<i>Computes the overall association theta and the row and column effects zeta</i>
---------------------------	---

---

**Description**

Computes the overall association theta and the row and column effects zeta

**Usage**

```
model_i_zeta(odds)
```

**Arguments**

<code>odds</code>	matrix of adjacent odds-ratios
-------------------	--------------------------------

**Value**

a list containing theta: the overall association zeta\_i\_dot: row effects for association zeta\_dot\_j: column effects for association

---

<code>movies</code>	<i>Movie ratings by two film critics, Siskel and Ebert.</i>
---------------------	---

---

**Description**

Movie ratings by two film critics, Siskel and Ebert.

**Usage**

```
movies
```

**Format**

```
## 'movies' A matrix with 3 rows and 3 columns 1 is con 2 is mixed 3 is pro
```

**Source**

<https://online.stat.psu.edu/stat504/lesson/11/11.3>

---

new_orleans_data	<i>Agreement between two clinicians on presence of multiple sclerosis based on file.</i>
------------------	--

---

**Description**

See companion winnipeg\_data.

**Usage**

```
new_orleans_data
```

**Format**

```
## 'new_orleans_data' A matrix with 4 rows and 4 columns Ratings range from definite presence  
of disease to definite absence.
```

**Source**

???

---

null_association_fHat	<i>Computes expected counts for null association model</i>
-----------------------	--

---

**Description**

Computes expected counts for null association model

**Usage**

```
null_association_fHat(alpha, beta)
```

**Arguments**

alpha	row effects
beta	column effects

**Value**

matrix of model-based expected counts

---

occupational_status	<i>Cross tabulation of father's employment status with son's employment status.</i>
---------------------	---

---

**Description**

Higher numbers correspond to higher status occupation

**Usage**

```
occupational_status
```

**Format**

```
## 'occupational_status' A matrix with 6 rows and 6 columns
```

**Source**

???

---

paranoia	<i>Interrater agreement of two psychologists' ratings of paranoia.</i>
----------	--

---

**Description**

Severity corresponds to level 1 low 3 high

**Usage**

```
paranoia
```

**Format**

```
## 'paranoia' A matrix with 3 rows and 3 columns.
```

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 70). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

pearson\_chisq*Computes the Pearson X^2 statistic.*

---

**Description**

Computes the Pearson X<sup>2</sup> statistic.

**Usage**

```
pearson_chisq(n, pi, exclude_diagonal = FALSE)
```

**Arguments**

- |                  |  |
|------------------|--|
| n                | Matrix of observed counts  |
| pi               | Matrix with same dimensions as n. Model-based matrix of predicted proportions  |
| exclude_diagonal | logical. Should diagonal cells of square matrix be excluded from the computation? Default is FALSE. The effect of setting it to TRUE for non-square matrices may be unintuitive and should be avoided. |

**Value**

X<sup>2</sup>

---

radiology*Interrater agreement of two radiologists diagnosis of severity of carcinoma.*

---

**Description**

The data contains a comparison vector of (simulated) covariate data.

**Usage**

```
radiology
```

**Format**

```
## 'radiology' 'covariate' A matrix with 4 rows and 4 columns, and a vector of 16 elements.
```

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 60). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

**Schuster\_compute\_df**    *Computes the degrees of freedom for the model.*

### Description

Computes the degrees of freedom for the model.

### Usage

```
Schuster_compute_df(pi_margin)
```

### Arguments

pi_margin	expected proportions for each of the categories
-----------	---

### Value

the df for the model

**Schuster\_compute\_pi**    *Compute matrix of model-based proportions pi.*

### Description

Compute matrix of model-based proportions pi.

### Usage

```
Schuster_compute_pi(marginal_pi, kappa, v, validate = TRUE)
```

### Arguments

marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix
validate	logical. should the cells be validated within this function? Defaults to TRUE

### Value

matrix of model-based cell proportions

---

**Schuster\_compute\_starting\_values**

*Computes starting values for the model.*

---

**Description**

Patterned after example in code in appendix to article

**Usage**

```
Schuster_compute_starting_values(n)
```

**Arguments**

n matrix of observed counts

**Value**

a list containing marginal\_pi: vector of expected proportions for each category kappa: kappa coefficient of agreement v: matrix of symmetry parameters

---

---

**Schuster\_derivative\_log\_l\_wrt\_kappa**

*Derivative of log(likelihood) wrt kappa.*

---

**Description**

Derivative of log(likelihood) wrt kappa.

**Usage**

```
Schuster_derivative_log_l_wrt_kappa(n, marginal_pi, kappa, v)
```

**Arguments**

n matrix of observed counts  
marginal\_pi expected proportions for each category  
kappa current value of kappa coefficient  
v symmetry matrix

**Value**

derivative of log(L) wrt kappa

**Schuster\_derivative\_log\_l\_wrt\_marginal\_pi**  
*Derivative of log(likelihood) wrt marginal\_pi[k]*

### Description

Derivative of log(likelihood) wrt marginal\_pi[k]

### Usage

`Schuster_derivative_log_l_wrt_marginal_pi(n, k, marginal_pi, kappa, v)`

### Arguments

n	matrix of observed counts
k	index into marginal_pi
marginal_pi	expected proportions of each of the categories
kappa	current value of the kappa coefficient
v	symmetry matrix

### Value

derivative of log(L) wrt marginal\_pi[k]

**Schuster\_derivative\_log\_l\_wrt\_v**  
*Derivative of log(likelihood) wrt v[i1, j1]*

### Description

Derivative of log(likelihood) wrt v[i1, j1]

### Usage

`Schuster_derivative_log_l_wrt_v(n, i1, j1, marginal_pi, kappa, v)`

### Arguments

n	matrix of observed counts
i1	first index into v
j1	second index into v
marginal_pi	expected marginal proportions
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

derivative of  $\log(L)$  wrt  $v[i1, j1]$

---

Schuster\_derivative\_pi\_wrt\_kappa

*Derivative of  $\pi[i, j]$  wrt kappa coefficient.*

---

**Description**

Derivative of  $\pi[i, j]$  wrt kappa coefficient.

**Usage**

`Schuster_derivative_pi_wrt_kappa(i, j, marginal_pi, kappa, v)`

**Arguments**

i	first index into pi
j	second index into pi
marginal_pi	expected proportions in each category
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

the derivative of  $\pi[i, j]$  wrt kappa

---

Schuster\_derivative\_pi\_wrt\_marginal\_pi

*Derivative of  $\pi[i, j]$  wrt marginal\_pi[k].*

---

**Description**

Derivative of  $\pi[i, j]$  wrt marginal\_pi[k].

**Usage**

`Schuster_derivative_pi_wrt_marginal_pi(i, j, k, marginal_pi, kappa, v)`

**Arguments**

i	first index into pi
j	second index into pi
k	index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

derivative of  $\pi[i, j]$  wrt  $\text{marginal\_pi}[k]$

**Schuster\_derivative\_pi\_wrt\_v**

*Computes derivative of  $\pi[i, j]$  wrt  $v[i1, j1]$*

**Description**

Computes derivative of  $\pi[i, j]$  wrt  $v[i1, j1]$

**Usage**

```
Schuster_derivative_pi_wrt_v(i, j, i1, j1, marginal_pi, kappa, v)
```

**Arguments**

i	first index into pi
j	second index into pi
i1	first index into v
j1	second index into v
marginal_pi	expected marginal proportions
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

value of derivative of specified pi wrt specified element of v

---

Schuster\_derivative\_v\_wrt\_v*Computes derivative of v[i1, j1] wrt v[i2, j2]*

---

**Description**

Needed because of computed v terms in column r

**Usage**

```
Schuster_derivative_v_wrt_v(i1, j1, i2, j2, marginal_pi, kappa, v)
```

**Arguments**

i1	first index into target v
j1	second index into target v
i2	first index into
j2	second index into
marginal_pi	expected marginal proportions
kappa	current estimate of kappa coefficient
v	matrix of symmetry parameters

**Value**

derivative of v[i1, j1] wrt v[i2, j2]

---

## Schuster\_enforce\_constraints\_on\_v

*Compute v matrix subject to constraints on rows 1..r-1.*

---

**Description**

Compute v matrix subject to constraints on rows 1..r-1.

**Usage**

```
Schuster_enforce_constraints_on_v(marginal_pi, kappa, v)
```

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

new v matrix with last row/column set to agree with constraints. Element v[r, r] is set to v-tilde

**Schuster\_gradient**      *Gradient vector  $\log(L)$  wrt parameters.*

**Description**

Work is delegated to functions that compute partial derivatives. This function is responsible for laying them out in correct positions in the vector.

**Usage**

```
Schuster_gradient(n, marginal_pi, kappa, v)
```

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

gradient vector

**Schuster\_hessian**      *Computes the hessian matrix of second-order partial derivatives of  $\log(L)$ .*

**Description**

Work is delegated to functions that compute second-order partial derivatives. This function is responsible for laying them out in correct positions in the matrix.

**Usage**

```
Schuster_hessian(n, marginal_pi, kappa, v)
```

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

hessian matrix

---

Schuster\_is\_pi\_valid *Determines whether the candidate pi matrix is valid.*

---

**Description**

All elements must lie in (0, 1)

**Usage**

Schuster\_is\_pi\_valid(pi)

**Arguments**

pi matrix of model-based proportions

**Value**

logical value indicating whether or not the matrix is valid.

---

Schuster\_newton\_raphson

*Performs Newton-Raphson step.*

---

**Description**

The step size is determined to be the largest that yields valid results for all quantities marginal\_pi and v. Both must be positive, and the elements of marginal\_pi must be valid proportions that sum to 1.0.

**Usage**

Schuster\_newton\_raphson(n, marginal\_pi, kappa, v)

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

a list containing updated versions of model quantities marginal\_pi kappa v

**Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_2**

*Second order partial log(L) wrt kappa^2.*

### Description

Second order partial log(L) wrt kappa^2.

### Usage

`Schuster_second_deriv_log_l_wrt_kappa_2(n, marginal_pi, kappa, v)`

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt kappa^2

**Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_v**

*Second order partial log(L) wrt kappa and v.*

### Description

Second order partial log(L) wrt kappa and v.

### Usage

`Schuster_second_deriv_log_l_wrt_kappa_v(n, marginal_pi, kappa, v)`

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt kappa and v

**Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_2**

*Second order partial log(L) wrt marginal\_pi^2.*

### Description

Second order partial log(L) wrt marginal\_pi^2.

### Usage

```
Schuster_second_deriv_log_l_wrt_marginal_pi_2(n, marginal_pi, kappa, v)
```

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt marginal_pi^2

**Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_kappa**

*Second order partial log(L) wrt marginal\_pi and kappa.*

### Description

Second order partial log(L) wrt marginal\_pi and kappa.

### Usage

```
Schuster_second_deriv_log_l_wrt_marginal_pi_kappa(n, marginal_pi, kappa, v)
```

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt marginal_pi and kappa

**Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_v**

*Second order partial log(L) wrt marginal\_pi and v.*

### Description

Second order partial log(L) wrt marginal\_pi and v.

### Usage

`Schuster_second_deriv_log_l_wrt_marginal_pi_v(n, marginal_pi, kappa, v)`

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt marginal_pi and v

**Schuster\_second\_deriv\_log\_l\_wrt\_v\_2**

*Second order partial log(L) wrt v^2.*

### Description

Second order partial log(L) wrt v^2.

### Usage

`Schuster_second_deriv_log_l_wrt_v_2(n, marginal_pi, kappa, v)`

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt v^2

Schuster\_second\_deriv\_pi\_wrt\_kappa\_2  
*Second order partial wrt kappa, kappa*

**Description**

Derivative is uniformly 0

**Usage**

`Schuster_second_deriv_pi_wrt_kappa_2(i, j, marginal_pi, kappa, v)`

**Arguments**

i	first index of pi
j	second index of pi
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

Schuster\_second\_deriv\_pi\_wrt\_kappa\_v  
*Second order partial wrt kappa, v*

**Description**

Derivative is uniformly 0

**Usage**

`Schuster_second_deriv_pi_wrt_kappa_v(i, j, i1, j1, marginal_pi, kappa, v)`

**Arguments**

i	first index of pi
j	second index of pi
i1	first index of v
j1	second index of v
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

---

*Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_2*

*Second derivative of pi[i, j] wrt marginal\_pi[k]^2*

---

**Description**

Second derivative of pi[i, j] wrt marginal\_pi[k]^2

**Usage**

*Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_2(i, j, k, k2, marginal\_pi, kappa, v)*

**Arguments**

i	first index into pi
j	second index into pi
k	index into marginal_pi
k2	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second derivative of pi[i, j] wrt marginal\_pi^2

---

*Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_kappa*

*Second order partial wrt kappa, marginal\_pi*

---

**Description**

Derivative is uniformly 0

**Usage**

*Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_kappa(i, j, k, marginal\_pi, kappa, v)*

**Arguments**

i	first index of pi
j	second index of pi
k	index of marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_v

*Second order partial pi wrt marginal\_pi and v*

**Description**

Second order partial pi wrt marginal\_pi and v

**Usage**

```
Schuster_second_deriv_pi_wrt_marginal_pi_v(
  i,
  j,
  k,
  i1,
  j1,
  marginal_pi,
  kappa,
  v
)
```

**Arguments**

i	first index of pi
j	second index of pi
k	index of marginal_pi
i1	first index of v
j1	second index of v
marginal_pi	expected proportions of each of the categories
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

derivative

---

*Schuster\_second\_deriv\_pi\_wrt\_v\_2*

*Second order partial wrt v^2*

---

**Description**

Derivative is uniformly 0

**Usage**

```
Schuster_second_deriv_pi_wrt_v_2(i, j, i1, j1, i2, j2, marginal_pi, kappa, v)
```

**Arguments**

i	first index of pi
j	second index of pi
i1	first index of first v
j1	second index of first v
i2	first index of second v
j2	second index of second
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

---

Schuster\_solve\_for\_v    *Solves for the last row and diagonal of symmetry matrix v (v-tilde) using constraint equations*

---

**Description**

Solves for the last row and diagonal of symmetry matrix v (v-tilde) using constraint equations

**Usage**

```
Schuster_solve_for_v(marginal_pi, kappa, v)
```

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

revised version of v matrix with last row and diagonal modified

---

---

Schuster\_solve\_for\_v1    *Solves for the last row and diagonal of symmetry matrix v (parameteer v-tilde) using linear algebra formulation from paper.*

---

**Description**

Solves for the last row and diagonal of symmetry matrix v (parameteer v-tilde) using linear algebra formulation from paper.

**Usage**

```
Schuster_solve_for_v1(marginal_pi, kappa, v)
```

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

revised version of v matrix with last row and diagonal modified

---

**Schuster\_symmetric\_rater\_agreement\_model**

*Computes the model that has kappa as a coefficient and symmetry.*

---

**Description**

Schuster, C. (2001). Kappa as a parameter of a symmetry model for rater agreement. Journal of Educational and Behavioral Statistics, 26(3), 331-342.

**Usage**

```
Schuster_symmetric_rater_agreement_model(
  n,
  verbose = FALSE,
  max_iter = 10000,
  criterion = 1e-07,
  min_iter = 1000
)
```

**Arguments**

n	the matrix of observed counts
verbose	logical. should cycle-by-cycle information be printed out
max_iter	integer. maximum number of iterations to perform
criterion	number. maximum change in log(likelihood) to decide convergence
min_iter	integer. minimum number of iterations to perform

**Value**

a list containing marginal\_pi: vector of expected proportions for each category kappa numeric:  
kappa coefficient v: matrix of symmetry parameters chisq: Pearson X^2 g\_squared: likelihood ratio G^2 df: degrees of freedom

---

**Schuster\_update**

*Computes the Newton-Raphson update*

---

**Description**

Computes both gradient and hessian, and then solves the system of equations

**Usage**

```
Schuster_update(n, marginal_pi, kappa, v)
```

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each category
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

the vector of updates

Schuster\_v\_tilde      *Computes the common diagonal term v-tilde.*

**Description**

Computes the common diagonal term v-tilde.

**Usage**

```
Schuster_v_tilde(marginal_pi, kappa, validate = TRUE)
```

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
validate	logical. should the value of pi[r,r] be checked for validity? Default is TRUE

**Value**

v-tilde

social\_status      *Social mobility data with father's occupational social status and son's occupational social status.*

**Description**

Social mobility data with father's occupational social status and son's occupational social status.

**Usage**

```
social_status
```

**Format**

```
## 'social_status' A matrix with 7 rows and 7 columns
```

**Source**

Goodman, L. A. (1979). Simple models for the analysis of association in cross-classifications having ordered categories. *Journal of the American Statistical Association*, 74(367), 537-552.

**social\_status2**

*Social mobility data with father's occupational social status and son's occupational social status. \* categories instead of 7 in social status..*

**Description**

Social mobility data with father's occupational social status and son's occupational social status. \* categories instead of 7 in social status..

**Usage**

```
social_status2
```

**Format**

```
## 'social_status2' A matrix with 8 rows and 8 columns
```

**Source**

Goodman, L. A. (1979). Simple models for the analysis of association in cross-classifications having ordered categories. *Journal of the American Statistical Association*, 74(367), 537-552.

**Stuart\_marginal\_homogeneity**

*Computes Stuart's Q test of marginal homogeneity.*

**Description**

Stuart, A. (1955). A test for homogeneity of the marginal distributions in a two-way classification. *Biometrika*, 42(3/4), 412-416.

**Usage**

```
Stuart_marginal_homogeneity(n)
```

**Arguments**

n	matrix of observed counts
---	---------------------------

**Value**

a list containing q: value of q test-statistic df: degrees of freedom p: upper tail p-value of q

**Examples**

```
Stuart_marginal_homogeneity(vision_data)
```

---

taste	<i>Taste ratings</i>
-------	----------------------

---

**Description**

Taste ratings

**Usage**

```
taste
```

**Format**

## ‘taste’ A matrix with 5 rows and 5 columns.

**Source**

McCullagh, P. (1980, p. 119). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142.

---

teachers	<i>Teachers ratings of their students intelligence.</i>
----------	---

---

**Description**

Interrater agreement data for two teachers asked to rate the intelligence of their students.

**Usage**

```
teachers
```

**Format**

## ‘teachers’ A matrix with 4 rows and 4 columns. Higher scores correspond to higher estimated intelligence.

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 36). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

<code>teaching_style</code>	<i>Style of teachers rated by supervisors</i>
-----------------------------	---

---

### Description

Ratings of style of teaching by supervisors. 1 indicates Authoritarian, 2 indicates Democratic, 3 indicates Permissive.

### Usage

```
teaching_style
```

### Format

An object of class `matrix` (inherits from `array`) with 3 rows and 3 columns.

### Details

@format ## 'teaching\_style' A matrix with 3 rows and 3 columns.

@source Agresti, A. (1989). An agreement model with kappa as parameter. *Statistics & Probability Letters*, 7, 271-273.

---

<code>tonsils</code>	<i>Relationship between size of child's tonsils and their status as a carrier of a disease.</i>
----------------------	---

---

### Description

Relationship between size of child's tonsils and their status as a carrier of a disease.

### Usage

```
tonsils
```

### Format

## 'tonsils' A matrix with 2 rows and 3 columns. Rows are disease status and columns are ratings of tonsil size.

### Source

McCullagh, P. (1980). Regression models for ordinal data. *Journal of the Royal Statistical Society, Series B*, 42(2), 109-142.

---

**tv**

*Interrater agreement of two journalists' evaluation of proposed TV programs.*

---

**Description**

Ratings go from low to high probability of the show's success.

**Usage**

tv

**Format**

## 'tv' A matrix of 6 rows and 6 columns.

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 56). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

**uniform\_association\_fHat**

*Computes expected counts for uniform association model*

---

**Description**

Computes expected counts for uniform association model

**Usage**

uniform\_association\_fHat(alpha, beta, theta)

**Arguments**

alpha	row effects
beta	column effects
theta	association parameter

**Value**

matrix of model-based expected counts

**uniform\_association\_update\_theta***Updates estimate of theta value of the uniform association model***Description**

Updates estimate of theta value of the uniform association model

**Usage**

```
uniform_association_update_theta(theta, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

theta	current estimate of theta
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical. Should the cells of the main diagonal be excluded from the computations? Default is FALSE, include all cells.

**Value**

updated estimate of theta parameter

**var\_kappa***Computes the sampling variance of kappa.***Description**

Formulas are from the paper by Fleiss,J. L., Cohen, J., & Everitt, B. S. (1969). Large sample standard errors of kappa and weighted kappa. Two results are returned in a list. var\_kappa0 is the null case and would be used for testing the hypothesis that kappa = 0. The second is var\_kappa and is for the non-null case, such as constructing CI for estimated kappa. Note that both are in the variance metric. Take the square root to get the standard error.

**Usage**

```
var_kappa(n)
```

**Arguments**

n	matrix of observe counts
---	--------------------------

**Value**

a list containing; var\_kappa0: variance for the null case var\_kappa: variance for the non-null case.

`var_weighted_kappa`      *Computes the sampling variance of weighted kappa.*

### Description

Formulas are from the paper by Fleiss,J. L., Cohen, J., & Everitt, B. S. (1969). Large sample standard errors of kappa and weighted kappa. Two results are returned in a list. `var_kappa0` is the null case and would be used for testing the hypothesis that  $\kappa = 0$ . The second is `var_kappa` and is for the non-null case, such as constructing CI for estimated kappa. Note that both are in the variance metric. Take the square root to get the standard error.

### Usage

```
var_weighted_kappa(n, w)
```

### Arguments

<code>n</code>	matrix of observe counts
<code>w</code>	matrix of penalty weights

### Value

a list containing; `var_kappa0`: variance for the null case `var_kappa`: variance for the non-null case.

`vision_data`      *Visual acuity of women factory workers.*

### Description

Measurements of unaided visual acuity for women working at the Royal Ordnance factories 1943-1946. Rows are right eye, columns are left eye. 1 indicates best vision, 4 is poorest.

### Usage

```
vision_data
```

### Format

```
## 'visual_data' A matrix with 4 rows and 4 columns.
```

### Source

Stuart, A. (1953). The estimation and comparison of strengths of association in contingency tables. *Biometrika*, 40(1/2), 105-110.

---

vision_data_men	<i>Visual acuity of men factory workers.</i>
-----------------	--

---

**Description**

Measurements of unaided visual acuity for men working at the Royal Ordnance factories 1943-1946. Rows are right eye, columns are left eye. 1 indicates best vision, 4 is poorest.

**Usage**

```
vision_data_men
```

**Format**

```
## 'visual_data_men' A matrix with 4 rows and 4 columns.
```

**Source**

Stuart, A. (1953). The estimation and comparison of strengths of association in contingency tables. *Biometrika*, 40(1/2), 105-110.

---

von_Eye_diagonal	<i>Fits the diagonal effects model, where each category has its own parameter delta[k].</i>
------------------	---

---

**Description**

Fits the diagonal effects model, where each category has its own parameter delta[k].

**Usage**

```
von_Eye_diagonal(n)
```

**Arguments**

n	the matrix of observed counts
---	-------------------------------

**Value**

a list containing beta: the regression parameters. delta parameters are the final elements of beta  
g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

**von\_Eye\_diagonal\_linear\_by\_linear**

*Fits the diagonal effects model, where each category has its own parameter  $\delta[k]$ , while also incorporating a linear-by-linear term.*

**Description**

Fits the diagonal effects model, where each category has its own parameter  $\delta[k]$ , while also incorporating a linear-by-linear term.

**Usage**

```
von_Eye_diagonal_linear_by_linear(n, center = TRUE)
```

**Arguments**

n	the matrix of observed counts
center	should the linear-by-linear components be centered to have mean 0? Default is TRUE

**Value**

a list containing beta: the regression parameters. delta parameters come after rows and columns and finally the linear-by-linear term g\_squared:  $G^2$  fit measure chisq:  $\chi^2$  fit measure df: degrees of freedom expected: matrix of expected frequencies

**von\_Eye\_equal\_weighted\_diagonal**

*Fits the equal weighted diagonal model, where the diagonals all have an additional parameter  $\delta$ , with the constraint that  $\delta$  is equal across all categories.*

**Description**

Fits the equal weighted diagonal model, where the diagonals all have an additional parameter  $\delta$ , with the constraint that  $\delta$  is equal across all categories.

**Usage**

```
von_Eye_equal_weighted_diagonal(n)
```

**Arguments**

n	the matrix of observed counts
---	-------------------------------

**Value**

a list containing beta: the regression parameters g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

**von\_Eye\_equal\_weight\_diagonal\_linear**

*Fits the diagonal effects model, where there is a single delta parameter for all categories, while also incorporating a linear-by-linear term.*

**Description**

Fits the diagonal effects model, where there is a single delta parameter for all categories, while also incorporating a linear-by-linear term.

**Usage**

```
von_Eye_equal_weight_diagonal_linear(n, center = TRUE)
```

**Arguments**

- |        |  |
|--------|--|
| n      | the matrix of observed counts  |
| center | should the linear-by-linear components be centered to have mean 0? Default is TRUE |

**Value**

a list containing beta: the regression parameters. delta parameters come after rows and columns and finally the linear-by-linear term g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

**von\_Eye\_linear\_by\_linear**

*Fits the basic independent rows and columns model incorporating a linear-by-linear term.*

**Description**

Fits the basic independent rows and columns model incorporating a linear-by-linear term.

**Usage**

```
von_Eye_linear_by_linear(n, center = TRUE)
```

**Arguments**

- n matrix of observed counts  
 center should the linear-by-linear components be centered to have mean 0? Default is TRUE

**Value**

a list containing beta: the regression parameters. The linear-by-linear parameter is last g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

**von\_Eye\_main\_effect** *Fits the base model with only independent row and column effects.*

**Description**

Fits the base model with only independent row and column effects.

**Usage**

```
von_Eye_main_effect(n)
```

**Arguments**

- n the matrix of observed counts

**Value**

a list containing beta: the regression parameters g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

**von\_Eye\_weight\_by\_response\_category\_design**

*Creates design matrix for weight be response category model.*

**Description**

The model specifies main effects for row and column, and a parameter for the agreement (diagonal) cells. This takes a design matrix for that model and applies domain-specific weights to the agreement parameters.

**Usage**

```
von_Eye_weight_by_response_category_design(n, x, w, n_raters = 2)
```

**Arguments**

- n** the matrix of cell counts  
**x** the original design matrix.  
**w** the vector of weights to apply to the agreement cells. Should have same number of entries as the number of diagonal elements (number of rows & of columns)  
**n\_raters** number of raters. Currently only 2 (the default) are supported. This is an extension point for future work.

**Value**

new design matrix with weights applied to the agreement cells.

---

**weighted\_cov**

*Computes the weighted covariance*

---

**Description**

Computes covariance between x and y using case weights in w

**Usage**

```
weighted_cov(x, y, w, use_df = TRUE)
```

**Arguments**

- x** Numeric vector. First variable  
**y** Numeric vector. Second variable  
**w** Numeric vector. case weights  
**use\_df** Logical. should the divisor be sum of weights - 1 (TRUE) or N - 1 (FALSE)

**Value**

the weighted covariance between x and y

---

**weighted\_kappa***Computes Cohen's 1968 weighted kappa coefficient*

---

**Description**

Computes Cohen's 1968 weighted kappa coefficient

**Usage**

```
weighted_kappa(n, w = diag(rep(1, nrow(n))), quadratic = FALSE)
```

**Arguments**

n	matrix of observed counts
w	matrix of weights. Defaults to identity matrix
quadratic	logical. Should quadratic weights be used? Default is FALSE. If TRUE, quadratic weights are used. These override the values in w. If FALSE, weights in w are used

**Value**

value of weighted kappa

---

---

**weighted\_var***Computes the weighted variance*

---

**Description**

Computes variance between x and y using case weights in w

**Usage**

```
weighted_var(x, w, use_df = TRUE)
```

**Arguments**

x	Numeric vector. First variable
w	Numeric vector. Case weights
use_df	Logical. Should the divisor be sum of weights - 1 (TRUE) or N - 1 (FALSE)

**Value**

the weighted covariance between x and y

---

winnipeg_data	<i>Agreement between two clinicians on presence of multiple sclerosis based on file.</i>
---------------	--

---

**Description**

See companion new\_orleans\_data.

**Usage**

```
winnipeg_data
```

**Format**

## ‘winnipeg\_data’ A matrix with 4 rows and 4 columns Ratings range from definite presence of disease to definite absence.

**Source**

???

# Index

- \* datasets
  - budget\_actual, 18
  - budget\_expected, 19
  - coal\_g, 32
  - depression, 33
  - dogs, 34
  - dreams, 34
  - dumping, 35
  - esophageal\_cancer, 35
  - family\_income, 37
  - gender\_vision, 37
  - homicide\_black\_black, 52
  - homicide\_black\_white, 52
  - homicide\_white\_black, 53
  - homicide\_white\_white, 53
  - hypothalamus\_1, 54
  - hypothalamus\_2, 54
  - interference\_12, 55
  - interference\_control\_1, 55
  - interference\_control\_2, 56
  - mental\_health, 155
  - movies, 168
  - new\_orleans\_data, 169
  - occupational\_status, 170
  - paranoia, 170
  - radiology, 171
  - social\_status, 189
  - social\_status2, 190
  - taste, 191
  - teachers, 191
  - teaching\_style, 192
  - tonsils, 192
  - tv, 193
  - vision\_data, 195
  - vision\_data\_men, 196
  - winnipeg\_data, 202
- Agresti\_bisection, 10
- Agresti\_compute\_lambda, 10
- Agresti\_compute\_pi, 11
- Agresti\_create\_design\_matrix, 11
- Agresti\_equation\_1, 12
- Agresti\_equation\_2, 12
- Agresti\_equation\_3, 13
- Agresti\_extract\_delta, 13
- Agresti\_f, 14
- Agresti\_kappa\_agreement, 14
- Agresti\_simple\_diagonals\_parameter\_quasi\_symmetry, 15
- Agresti\_starting\_values, 15
- Agresti\_w\_diff, 16
- Agresti\_weighted\_tau, 16
- Bhapkar\_marginal\_homogeneity, 17
- Bhapkar\_quasi\_symmetry, 17
- Bowker\_symmetry, 18
- budget\_actual, 18
- budget\_expected, 19
- Clayton\_marginal\_location, 19
- Clayton\_stratified\_marginal\_location, 20
- Clayton\_summarize, 21
- Clayton\_summarize\_stratified, 21
- Clayton\_two\_way\_association, 22
- Cliff\_as\_d\_matrix, 22
- Cliff\_compute\_d, 23
- Cliff\_counts\_2, 23
- Cliff\_counts\_3, 24
- Cliff\_counts\_4, 24
- Cliff\_counts\_5, 25
- Cliff\_counts\_6, 25
- Cliff\_dependent, 26
- Cliff\_dependent\_compute\_cov, 26
- Cliff\_dependent\_compute\_cov\_from\_d, 27
- Cliff\_dependent\_compute\_from\_matrix, 27
- Cliff\_dependent\_compute\_from\_table, 28
- Cliff\_dependent\_compute\_paired\_d, 29
- Cliff\_independent, 30

Cliff\_independent\_from\_matrix, 30  
 Cliff\_independent\_from\_table, 31  
 Cliff\_independent\_weighted, 31  
 Cliff\_weighted\_d\_matrix, 32  
 coal\_g, 32  
 constant\_of\_integration, 33  
 depression, 33  
 dogs, 34  
 dreams, 34  
 dumping, 35  
 esophageal\_cancer, 35  
 expand, 36  
 expit, 36  
 family\_income, 37  
 gender\_vision, 37  
 Goodman\_constrained\_diagonals\_parameter\_symmetry, 38  
 Goodman\_diagonals\_parameter\_symmetry, 38  
 Goodman\_fixed\_parameter, 39  
 Goodman\_ml, 40  
 Goodman\_model\_i, 41  
 Goodman\_model\_i\_star, 43  
 Goodman\_model\_ii, 42  
 Goodman\_model\_ii\_star, 43  
 Goodman\_null\_association, 44  
 Goodman\_pi, 45  
 Goodman\_pi\_matrix, 46  
 Goodman\_symmetric\_association\_model, 46  
 Goodman\_uniform\_association, 47  
 handle\_max\_i\_i, 47  
 handle\_max\_i\_k, 48  
 handle\_max\_k\_k2, 49  
 handle\_one\_maximum, 49  
 handle\_tied\_below\_maximum, 50  
 handle\_tied\_maximum, 50  
 handle\_untied\_below\_maximum, 51  
 homicide\_black\_black, 52  
 homicide\_black\_white, 52  
 homicide\_white\_black, 53  
 homicide\_white\_white, 53  
 hypothalamus\_1, 54  
 hypothalamus\_2, 54  
 interference\_12, 55  
 interference\_control\_1, 55  
 interference\_control\_2, 56  
 Ireland\_marginal\_homogeneity, 56  
 Ireland\_mdls, 57  
 Ireland\_normalize\_for\_truncation, 57  
 Ireland\_quasi\_symmetry, 58  
 Ireland\_quasi\_symmetry\_model, 58  
 Ireland\_symmetry, 59  
 is\_invertible, 60  
 is\_missing\_or\_infinite, 60  
 kappa, 61  
 likelihood\_ratio\_chisq, 61  
 loadRData, 62  
 log\_likelihood, 63  
 log\_linear\_add\_all\_diagonals, 63  
 log\_linear\_append\_column, 64  
 log\_linear\_create\_coefficient\_names, 65  
 log\_linear\_create\_linear\_by\_linear, 65  
 log\_Linear\_create\_log\_n, 66  
 log\_linear\_equal\_weight\_agreement\_design, 66  
 log\_linear\_fit, 67  
 log\_linear\_main\_effect\_design, 68  
 log\_linear\_matrix\_to\_vector, 68  
 log\_linear\_quasi\_symmetry\_model\_design, 69  
 log\_linear\_remove\_column, 69  
 log\_linear\_symmetry\_design, 70  
 logit, 62  
 McCullagh\_compute\_c\_plus, 72  
 McCullagh\_compute\_condition, 70  
 McCullagh\_compute\_cumulative\_sums, 71  
 McCullagh\_compute\_cumulatives, 71  
 McCullagh\_compute\_df, 72  
 McCullagh\_compute\_gamma, 73  
 McCullagh\_compute\_gamma\_from\_phi, 73  
 McCullagh\_compute\_gamma\_plus\_1\_from\_phi, 74  
 McCullagh\_compute\_generalized\_cumulatives, 74  
 McCullagh\_compute\_generalized\_pi, 75  
 McCullagh\_compute\_lambda, 75  
 McCullagh\_compute\_log\_l, 76  
 McCullagh\_compute\_Nij, 76

McCullagh\_compute\_omega, 77  
McCullagh\_compute\_phi, 77  
McCullagh\_compute\_phi\_matrix, 78  
McCullagh\_compute\_pi, 78  
McCullagh\_compute\_pi\_from\_beta, 79  
McCullagh\_compute\_pi\_from\_gamma, 79  
McCullagh\_compute\_regression\_weights,  
    80  
McCullagh\_compute\_s\_plus, 80  
McCullagh\_compute\_update, 81  
McCullagh\_compute\_z, 81  
McCullagh\_conditional\_symmetry, 82  
McCullagh\_conditional\_symmetry\_compute\_s,  
    82  
McCullagh\_conditional\_symmetry\_initialize\_phi,  
    83  
McCullagh\_conditional\_symmetry\_maximize\_phi, 83  
McCullagh\_conditional\_symmetry\_maximize\_theta,  
    84  
McCullagh\_conditional\_symmetry\_pi, 84  
McCullagh\_derivative\_condition\_wrt\_psi,  
    85  
McCullagh\_derivative\_gamma\_plus\_1\_wrt\_phi,  
    85  
McCullagh\_derivative\_gamma\_wrt\_phi, 86  
McCullagh\_derivative\_gamma\_wrt\_y, 86  
McCullagh\_derivative\_lagrangian\_wrt\_delta,  
    87  
McCullagh\_derivative\_lagrangian\_wrt\_delta\_vec,  
    87  
McCullagh\_derivative\_lagrangian\_wrt\_psi,  
    88  
McCullagh\_derivative\_log\_l\_wrt\_alpha,  
    89  
McCullagh\_derivative\_log\_l\_wrt\_beta,  
    89  
McCullagh\_derivative\_log\_l\_wrt\_c, 90  
McCullagh\_derivative\_log\_l\_wrt\_delta,  
    90  
McCullagh\_derivative\_log\_l\_wrt\_delta\_vec,  
    91  
McCullagh\_derivative\_log\_l\_wrt\_params,  
    92  
McCullagh\_derivative\_log\_l\_wrt\_phi, 92  
McCullagh\_derivative\_log\_l\_wrt\_psi, 93  
McCullagh\_derivative\_omega\_wrt\_alpha,  
    93  
McCullagh\_derivative\_omega\_wrt\_c, 94  
McCullagh\_derivative\_omega\_wrt\_delta,  
    94  
McCullagh\_derivative\_omega\_wrt\_delta\_vec,  
    95  
McCullagh\_derivative\_omega\_wrt\_psi, 95  
McCullagh\_derivative\_phi\_wrt\_gamma, 96  
McCullagh\_derivative\_pi\_wrt\_alpha, 99  
McCullagh\_derivative\_pi\_wrt\_c, 100  
McCullagh\_derivative\_pi\_wrt\_delta, 101  
McCullagh\_derivative\_pi\_wrt\_delta\_vec,  
    101  
McCullagh\_derivative\_pi\_wrt\_psi, 102  
McCullagh\_derivative\_pij\_wrt\_alpha, 96  
McCullagh\_derivative\_pij\_wrt\_c, 97  
McCullagh\_derivative\_pij\_wrt\_delta, 98  
McCullagh\_derivative\_pij\_wrt\_delta\_vec,  
    98  
McCullagh\_derivative\_pij\_wrt\_psi, 99  
McCullagh\_extract\_weights, 102  
McCullagh\_fit\_location\_regression\_model,  
    103  
McCullagh\_generalized\_palindromic\_symmetry,  
    104  
McCullagh\_generalized\_pij\_qij, 105  
McCullagh\_generate\_names, 105  
McCullagh\_get\_statistics, 106  
McCullagh\_gradient\_log\_l, 106  
McCullagh\_hessian\_log\_l, 107  
McCullagh\_initialize\_beta, 107  
McCullagh\_initialize\_delta, 108  
McCullagh\_initialize\_delta\_vec, 108  
McCullagh\_initialize\_psi, 109  
McCullagh\_initialize\_x, 109  
McCullagh\_is\_in\_constraint\_set, 110  
McCullagh\_is\_pi\_invalid, 110  
McCullagh\_log\_L, 112  
McCullagh\_logistic\_model, 111  
McCullagh\_logits, 111  
McCullagh\_maximize\_q\_symmetry, 112  
McCullagh\_newton\_raphson\_update, 113  
McCullagh\_palindromic\_symmetry, 114  
McCullagh\_penalized, 114  
McCullagh\_pij\_qij, 115  
McCullagh\_proportional\_hazards, 116  
McCullagh\_q\_symmetry\_initialize\_alpha,  
    117  
McCullagh\_q\_symmetry\_initialize\_phi,

117	134
McCullagh_q_symmetry_pi, 118	McCullagh_second_order_omega_wrt_delta_2, 135
McCullagh_quasi_symmetry, 116	McCullagh_second_order_omega_wrt_delta_alpha, 135
McCullagh_second_order_lagrangian_wrt_psi_2, McCullagh_second_order_omega_wrt_delta_alpha, 118	McCullagh_second_order_omega_wrt_delta_c, 136
McCullagh_second_order_lagrangian_wrt_psi_alpha, 119	McCullagh_second_order_omega_wrt_delta_vec_2, 137
McCullagh_second_order_lagrangian_wrt_psi_delta, 120	McCullagh_second_order_omega_wrt_delta_vec_alpha, 137
McCullagh_second_order_lagrangian_wrt_psi_delta, 121	McCullagh_second_order_omega_wrt_delta_vec_c, 138
McCullagh_second_order_log_l_wrt_alpha_2, 122	McCullagh_second_order_omega_wrt_psi_2, 139
McCullagh_second_order_log_l_wrt_alpha_c, 122	McCullagh_second_order_omega_wrt_psi_alpha, 140
McCullagh_second_order_log_l_wrt_beta_2, 123	McCullagh_second_order_omega_wrt_psi_c, 141
McCullagh_second_order_log_l_wrt_c_2, 124	McCullagh_second_order_omega_wrt_psi_delta, 141
McCullagh_second_order_log_l_wrt_delta_2, 124	McCullagh_second_order_pi_wrt_alpha_2, 143
McCullagh_second_order_log_l_wrt_delta_alpha, McCullagh_second_order_omega_wrt_psi_delta_vec, 125	McCullagh_second_order_pi_wrt_alpha_c, 144
McCullagh_second_order_log_l_wrt_delta_c, 126	McCullagh_second_order_pi_wrt_c_2, 144
McCullagh_second_order_log_l_wrt_delta_vec_2, McCullagh_second_order_pi_wrt_delta_2, 126	McCullagh_second_order_pi_wrt_delta_c, 145
McCullagh_second_order_log_l_wrt_delta_vec_alpha, 127	McCullagh_second_order_pi_wrt_delta_alpha, 145
McCullagh_second_order_log_l_wrt_delta_vec_c, 128	McCullagh_second_order_pi_wrt_delta_c, 146
McCullagh_second_order_log_l_wrt_parms, 128	McCullagh_second_order_pi_wrt_delta_vec_2, 147
McCullagh_second_order_log_l_wrt_psi_2, 129	McCullagh_second_order_pi_wrt_delta_vec_alpha, 148
McCullagh_second_order_log_l_wrt_psi_alpha, 130	McCullagh_second_order_pi_wrt_delta_vec_c, 149
McCullagh_second_order_log_l_wrt_psi_c, 131	McCullagh_second_order_pi_wrt_psi_2, 149
McCullagh_second_order_log_l_wrt_psi_delta, 131	McCullagh_second_order_pi_wrt_psi_alpha, 150
McCullagh_second_order_log_l_wrt_psi_delta_vec, 132	McCullagh_second_order_pi_wrt_psi_c, 151
McCullagh_second_order_omega_wrt_alpha_2, 133	McCullagh_second_order_pi_wrt_psi_delta, 152
McCullagh_second_order_omega_wrt_alpha_c, 133	
McCullagh_second_order_omega_wrt_c_2,	

McCullagh\_second\_order\_pi\_wrt\_psi\_delta\_vec, 152  
McCullagh\_update\_parameters, 153  
McCullagh\_v\_inverse, 154  
mental\_health, 155  
model\_i\_column\_theta, 161  
model\_i\_effects, 161  
model\_i\_fHat, 162  
model\_i\_normalize\_fHat, 162  
model\_i\_row\_column\_odds\_ratios, 163  
model\_i\_row\_theta, 163  
model\_i\_star\_effects, 164  
model\_i\_star\_fHat, 165  
model\_i\_star\_update\_theta, 165  
model\_i\_starting\_values, 164  
model\_i\_update\_alpha, 166  
model\_i\_update\_beta, 166  
model\_i\_update\_delta, 167  
model\_i\_update\_gamma, 167  
model\_i\_zeta, 168  
model\_ii\_effects, 155  
model\_ii\_fHat, 156  
model\_ii\_ksi, 156  
model\_ii\_star\_effects, 157  
model\_ii\_star\_fHat, 158  
model\_ii\_star\_update\_phi, 158  
model\_ii\_starting\_values, 157  
model\_ii\_update\_alpha, 159  
model\_ii\_update\_beta, 159  
model\_ii\_update\_rho, 160  
model\_ii\_update\_sigma, 160  
movies, 168  
new\_orleans\_data, 169  
null\_association\_fHat, 169  
occupational\_status, 170  
paranoia, 170  
pearson\_chisq, 171  
radiology, 171  
Schuster\_compute\_df, 172  
Schuster\_compute\_pi, 172  
Schuster\_compute\_starting\_values, 173  
Schuster\_derivative\_log\_l\_wrt\_kappa, 173  
Schuster\_derivative\_log\_l\_wrt\_marginal\_pi, 174  
Schuster\_derivative\_log\_l\_wrt\_v, 174  
Schuster\_derivative\_pi\_wrt\_kappa, 175  
Schuster\_derivative\_pi\_wrt\_marginal\_pi, 175  
Schuster\_derivative\_pi\_wrt\_v, 176  
Schuster\_derivative\_v\_wrt\_v, 177  
Schuster\_enforce\_constraints\_on\_v, 177  
Schuster\_gradient, 178  
Schuster\_hessian, 178  
Schuster\_is\_pi\_valid, 179  
Schuster\_newton\_raphson, 179  
Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_2, 180  
Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_v, 180  
Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_2, 181  
Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_kappa, 181  
Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_v, 182  
Schuster\_second\_deriv\_log\_l\_wrt\_v\_2, 182  
Schuster\_second\_deriv\_pi\_wrt\_kappa\_2, 183  
Schuster\_second\_deriv\_pi\_wrt\_kappa\_v, 183  
Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_2, 184  
Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_kappa, 184  
Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_v, 185  
Schuster\_second\_deriv\_pi\_wrt\_v\_2, 186  
Schuster\_solve\_for\_v, 187  
Schuster\_solve\_for\_v1, 187  
Schuster\_symmetric\_rater\_agreement\_model, 188  
Schuster\_update, 188  
Schuster\_v\_tilde, 189  
social\_status, 189  
social\_status2, 190  
Stuart\_marginal\_homogeneity, 190  
taste, 191  
teachers, 191  
teaching\_style, 192  
tonsils, 192  
tv, 193

uniform\_association\_fHat, 193  
uniform\_association\_update\_theta, 194  
  
var\_kappa, 194  
var\_weighted\_kappa, 195  
vision\_data, 195  
vision\_data\_men, 196  
von\_Eye\_diagonal, 196  
von\_Eye\_diagonal\_linear\_by\_linear, 197  
von\_Eye\_equal\_weight\_diagonal\_linear,  
    198  
von\_Eye\_equal\_weighted\_diagonal, 197  
von\_Eye\_linear\_by\_linear, 198  
von\_Eye\_main\_effect, 199  
von\_Eye\_weight\_by\_response\_category\_design,  
    199  
  
weighted\_cov, 200  
weighted\_kappa, 201  
weighted\_var, 201  
winnipeg\_data, 202