

# Package ‘loewesadditivity’

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**Title** Loewe's Additivity

**Version** 0.1.0

**Description** Estimate model parameters to determine whether two compounds have synergy, antagonism, or Loewe's Additivity.

**License** MIT + file LICENSE

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base_GIA	<i>Estimate GIA according to the base model</i>
----------	---

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### Description

Estimate GIA according to the base model

### Usage

```
base_GIA(model_params, dose_A, dose_B, fn_list = NULL)
```

### Arguments

model_params	named vector of parameters to be used in function. Specifically, the named parameters must be "beta_A", "beta_B", "gamma_A", "gamma_B", "tau_1", and "tau_2". See details for more info.
dose_A	numeric vector of doses (e.g. mg/mL) of dose_A
dose_B	numeric vector of doses (e.g. mg/mL) of dose_B
fn_list	NULL

### Value

estimated GIA for each combination of dose A and dose B

### Details

The equation is given in full as follows. The GIA (%) is given as a function of the model parameters and the doses  $A_i$  and  $B_i$ , respectively. The doses scaled by the respective ED50s  $\beta_A$  and  $\beta_B$  are denoted by  $A_i^*$  and  $B_i^*$ , respectively. The parameters  $\gamma_A$  and  $\gamma_B$  are shape parameters. The parameters  $\tau_1$  and  $\tau_2$  are interaction parameters. Finally,  $\lambda_i$  is a weighted combination of dose A and dose B.

$$GIA_i = 100\%(1 - e^{-\psi_i})$$

$$\psi_i = \log(2)u_i^{\lambda_i}$$

$$u_i = A_i^* + B_i^* + \tau_1 A_i^* B_i^*$$

$$v_i = \lambda_i \gamma_A + (1 - \lambda_i) \gamma_B + \tau_1 \tau_2 \lambda_i (1 - \lambda_i) \gamma_A \gamma_B$$

$$\lambda_i = \frac{A_i^*}{A_i^* + B_i^*}$$

$$A_i^* = A_i / \beta_A$$

$$B_i^* = B_i / \beta_B$$

## Examples

```
model_params <- c("beta_A" = 1, "beta_B" = 2, "gamma_A" = .5,
  "gamma_B" = .6, "tau_1" = 1, "tau_2" = 0)
dose_A <- c(0, 1, 0)
dose_B <- c(0, 0, 1)
base_GIA(model_params, dose_A, dose_B)
```

---

 boot\_GIA

*Helper function for the bootstrap results*


---

## Description

Helper function for the bootstrap results

## Usage

```
boot_GIA(
  par,
  gia_df,
  gia_est,
  n_boot = 100,
  alpha = 0.05,
  GIA_fn = base_GIA,
  S_fn = calc_S_base,
  fn_list = NULL,
  verbose = FALSE
)
```

## Arguments

par	named vector of parameters, that correspond to those used in 'GIA_fn'.
gia_df	data frame with the following columns <ul style="list-style-type: none"> <li>dose_Adose A mg/mL</li> <li>dose_Bdose B mg/mL</li> <li>GIAGIA</li> </ul>
gia_est	estimated values of GIA (these will be used as the 'truth')
n_boot	number of boot straps to use to estimate confidence intervals of the parameters, GIA estimates, and values of S. The default is 100. If n_boot = 0, then no bootstraps will be run and only the point estimates will be returned.

alpha	value of alpha. Default is .05
GIA_fn	function to calculate the GIA from dose_A and dose_B combinations and given set of parameters. Default is base_GIA
S_fn	Function to calculate S. Default is calc_S_base
fn_list	additional arguments to pass to GIA_fn
verbose	logical indicating whether we should print where we are in the process. Default is FALSE.

**Value**

a list with the following elements

- params\_esta data frame of dimension # of params x 4 where each row in the data frame is a parameter and where the columns are the mean, lower, alpha/2 quantile, and upper, 100 - alpha/2 quantile
- S\_est a data frame of one row x 4 where we provide the mean, lower, and upper estimates
- GIA\_est the original data with additional columns of the mean, lower, and upper estimates for each dose combination

---

calc_S	<i>Calculate S generally</i>
--------	------------------------------

---

**Description**

Calculate S generally

**Usage**

```
calc_S(best_pars, S_fn = calc_S_base, fn_list = NULL)
```

**Arguments**

best_pars	named vector of parameters. "tau_1" must be a name. As must "tau_2" and "gamma_A" and "gamma_B"
S_fn	function to calculate
fn_list	NULL

**Value**

Hewlett's S for the given model

**Examples**

```
best_pars <- c("tau_1" = 0,
              "tau_2" = 1,
              "gamma_A" = 1,
              "gamma_B" = 1)
calc_S_base(best_pars) # should be 1
```

---

calc_S_base	<i>Calculate S from given tau_1 for base model</i>
-------------	--

---

**Description**

Calculate S from given tau\_1 for base model

**Usage**

```
calc_S_base(best_pars, fn_list = NULL)
```

**Arguments**

best_pars	named vector of parameters. "tau_1" must be a name. As must "tau_2" and "gamma_A" and "gamma_B"
fn_list	NULL

**Value**

Hewlett's S for the base model.

**Examples**

```
best_pars <- c("tau_1" = 0,  
              "tau_2" = 1,  
              "gamma_A" = 1,  
              "gamma_B" = 1)  
calc_S_base(best_pars) # should be 1
```

---

cyrpa_ripr	<i>CyRPA and RIPR</i>
------------	-----------------------

---

**Description**

The data is the raw data for a combination dose of CyRPA and RIPR.

**well** one of iRBC (the max), uRBC (the min), RPMI (??), or comb (which is short for combination)

**RIPR** dose of RIPR in mg/mL

**CyRPA** dose of CyRPA in mg/mL

**expyrepxz** the results from experiment x, sub item y, repetition z

**Usage**

```
cyrpa_ripr
```

**Format**

An object of class `data.frame` with 38 rows and 15 columns.

**Examples**

```
data("cyrpa_ripr")
head(cyrpa_ripr)
```

---

design_experiment	<i>Helper function to generate code to run an experiment</i>
-------------------	--

---

**Description**

Helper function to generate code to run an experiment

**Usage**

```
design_experiment(
  levels_A = c(0, 1 * 2^(-4:2)),
  levels_B = c(0, 2 * 2^(-4:2)),
  par = c(beta_A = 1, beta_B = 2, gamma_A = 0.5, gamma_B = 0.5, tau_1 = 3, tau_2 = 0.05),
  n_rep = 1,
  n_sims = 100,
  noise_par = c(a0 = 3, a1 = 0.01)
)
```

**Arguments**

levels_A	levels of A used in the combination
levels_B	levels of B used in the combination
par	named vector of model parameters
n_rep	number of total repetitions of experiment
n_sims	number of simulations to run
noise_par	named vector with 'a0' and 'a1' which are used to generate noise for the GIA.

**Details**

prints out code to copy and paste into R to simulate the expected coverage of your experiment under your designed hypothesis

---

design_grid	<i>Function to design an experimental grid of combinations</i>
-------------	--

---

**Description**

Function to design an experimental grid of combinations

**Usage**

```
design_grid(
  levels_A = c(0, 1 * 2^(-4:2)),
  levels_B = c(0, 2 * 2^(-4:2)),
  n_rep = 1
)
```

**Arguments**

levels_A	levels of A used in the combination
levels_B	levels of B used in the combination
n_rep	number of total repetitions of experiment

**Value**

data frame with columns dose\_A, dose\_B, and GIA for all possible combinations

---

estimate_GIA	<i>Take in dose A and dose B combinations and estimate GIA</i>
--------------	--

---

**Description**

Take in dose A and dose B combinations and estimate GIA

**Usage**

```
estimate_GIA(model_params, dose_A, dose_B, fn = base_GIA, fn_list = NULL)
```

**Arguments**

model_params	named vector of parameters to be used in function
dose_A	numeric vector of doses (e.g. mg/mL) of dose_A
dose_B	numeric vector of doses (e.g. mg/mL) of dose_B
fn	the function used to calculate GIA. The default is base_GIA. See ?base_GIA for more details.
fn_list	additional parameters to pass to the function to estimate GIA

**Value**

vector of the same size of dose\_A and dose\_B where each entry is the estimated GIA for the combination of dose A and dose B

**Examples**

```
model_params <- c("beta_A" = 1, "beta_B" = 2, "gamma_A" = .5,
  "gamma_B" = .6, "tau_1" = 1, "tau_2" = 0)
dose_A <- c(0, 1, 0)
dose_B <- c(0, 0, 1)
estimate_GIA(model_params, dose_A, dose_B)
```

---

estimate_params	<i>Estimate the parameters for a given data set and model</i>
-----------------	---

---

**Description**

Estimate the parameters for a given data set and model

**Usage**

```
estimate_params(
  data,
  init_params = c(beta_A = 0.25, beta_B = 0.25, gamma_A = 0.5, gamma_B = 0.5, tau_1 = 0,
    tau_2 = 0),
  n_boot = 100,
  GIA_fn = base_GIA,
  S_fn = calc_S_base,
  fn_list = NULL,
  alpha = 0.05,
  verbose = FALSE
)
```

**Arguments**

data	data frame with the following columns <ul style="list-style-type: none"> <li>• dose_Adose A mg/mL</li> <li>• dose_Bdose B mg/mL</li> <li>• GIAGIA</li> </ul>
init_params	named vector of parameters, that correspond to those used in 'GIA_fn'. These will be used as the initial guesses. A default is provided.
n_boot	number of boot straps to use to estimate confidence intervals of the parameters, GIA estimates, and values of S. The default is 100. If n_boot = 0, then no bootstraps will be run and only the point estimates will be returned.
GIA_fn	function to calculate the GIA from dose_A and dose_B combinations and given set of parameters. Default is base_GIA



S_fn	Function to calculate S. Default is calc_S_base
fn_list	additional arguments to pass to GIA_fn
alpha	alpha level used to produce CIs. The bootstrap will use a two-tailed method. The default is .05 to produce a 95% CI
verbose	logical indicating whether we should print where we are in the process. Default is FALSE.

## Value

a list with the following elements

- params\_esta data frame of dimension # of params x 4 where each row in the data frame is a parameter and where the columns are the mean, lower, alpha/2 quantile, and upper, 100 - alpha/2 quantile
- S\_est a data frame of one row x 4 where we provide the mean, lower, and upper estimates
- GIA\_est the original data with additional columns of the mean, lower, and upper estimates for each dose combination
- SSE Sum of Square Error for the model under the best (mean) parameters

## Examples

```
df <- loewesadditivity::cyrpa_ripr
df$dose_A <- df$CyRPA
df$dose_B <- df$RIPR
data <- fortify_gia_data(df)
model_params <- c("beta_A" = .5, "beta_B" = .5,
                 "gamma_A" = .5, "gamma_B" = .5,
                 "tau_1" = 0, "tau_2" = 0)

n_boot <- 10
GIA_fn <- base_GIA
S_fn <- calc_S_base
fn_list <- NULL
alpha <- .05
verbose <- FALSE
out <- estimate_params(data = data,
                      init_params = model_params,
                      n_boot = n_boot,
                      GIA_fn = GIA_fn,
                      S_fn = S_fn,
                      fn_list = fn_list,
                      alpha = alpha,
                      verbose = verbose)
names(out)
```

---

fortify_gia_data	<i>Put GIA measurements into a dplyr format</i>
------------------	---

---

**Description**

Put GIA measurements into a dplyr format

**Usage**

```
fortify_gia_data(data)
```

**Arguments**

<b>data</b>	data frame of GIA measurements
<b>well</b>	one of "IRBC", "uRBC", "RPMI", or "comb"
<b>dose_A</b>	dose of A in mg/mL
<b>dose_B</b>	dose of B in mg/mL
<b>exp(X)(Y)rep(Z)</b>	where X = 1 or 2, Y = a or b, and Z = 1, 2, or 3

**Value**

long data frame with columns well, dose\_A, dose\_B, plate, exp\_num (experiment number), plate (a or b), rep\_num (repetition number), gia\_mean, and average iRBC and uRBC

**Examples**

```
df <- loewesadditivity::rh5_ama1ron2
df$dose_A <- df$RH5
df$dose_B <- df$AMA1RON2
fortified_df <- fortify_gia_data(df)
head(fortified_df)
```

---

get_ed_line	<i>Helper function to get the ED50 line</i>
-------------	---

---

**Description**

Helper function to get the ED50 line

**Usage**

```
get_ed_line(
  grid_width = 50,
  par,
  GIA_fn = base_GIA,
  fn_list = NULL,
  ed_val = 50
)
```

**Arguments**

grid_width	number of levels to find points at
par	named vector of parameters
GIA_fn	function to calculate GIA
fn_list	additional parameters to pass to GIA_fn
ed_val	Which line to compute. Default is 50

**Value**

data frame with the following columns

**dose\_A** dose of A (unscaled)

**dose\_B** dose of B (unscaled)

**GIA** value of GIA %

---

make_grid	<i>Make a grid of points</i>
-----------	------------------------------

---

**Description**

Make a grid of points

**Usage**

```
make_grid(n = 40, par, Amax = 2, Bmax = 2, n_reps = 1)
```

**Arguments**

n	number of levels on each side (Total grid is $n^2$ ). Default is 40
par	named vector of model parameters
Amax	max amount of number of ED50s. Default is 2
Bmax	max amount of number of ED50s. Default is 2.
n_reps	number of replicates to repeat entire grid/experiment. Default is 1.

**Value**

data frame with the following columns

**dose\_A** unscaled dose of A

**dose\_B** unscaled dose o B

**rep** replicate number

## Examples

```
n <- 40
par <- c("beta_A" = 1, "beta_B" = 2)
out <- make_grid(n = 2, par = par)
exp_out <- data.frame(dose_A = c(0, 2, 0, 2),
                     dose_B = c(0, 0, 4, 4),
                     rep = 1)
```

---

plot\_curves

*Plot the surface and observations*

---

## Description

Plot the surface and observations

## Usage

```
plot_curves(
  est_list,
  dose_A = "Dose A",
  dose_B = "Dose B",
  title = "Curves of Dose Combos",
  subtitle = "",
  base_size = 14
)
```

## Arguments

est_list	output from estimate_params
dose_A	to pass to ggplot
dose_B	to pass to ggplot
title	to pass to ggplot
subtitle	to pass to ggplot
base_size	to pass to ggplot

## Value

ggplot object

## Examples

```
df <- loewesadditivity::cyrpa_ripr
df$dose_A <- df$CyRPA
df$dose_B <- df$RIPR
data <- fortify_gia_data(df)
model_params <- c("beta_A" = .5, "beta_B" = .5,
```

```

      "gamma_A" = .5, "gamma_B" = .5,
      "tau_1" = 0, "tau_2" = 0)
n_boot <- 10
GIA_fn <- base_GIA
S_fn <- calc_S_base
fn_list <- NULL
alpha <- .05
verbose <- FALSE
out <- estimate_params(data = data,
  init_params = model_params,
  n_boot = n_boot,
  GIA_fn = GIA_fn,
  S_fn = S_fn,
  fn_list = fn_list,
  alpha = alpha,
  verbose = verbose)
plots <- plot_curves(out, dose_A = "CyRPA",
  dose_B = "RIPR")

```

---

plot\_isobologram      *Plot the estimated isobologram*

---

## Description

Plot the estimated isobologram

## Usage

```

plot_isobologram(
  est_list,
  dose_A = "Dose A",
  dose_B = "Dose B",
  GIA_fn = base_GIA,
  fn_list = NULL,
  title = "Isobologram Dose Combos",
  subtitle = "",
  base_size = 14
)

```

## Arguments

est_list	output from estimate_params
dose_A	to pass to ggplot
dose_B	to pass to ggplot
GIA_fn	function to calculate GIA
fn_list	additional arguments to pass to GIA fn

title           to pass to ggplot  
 subtitle       to pass to ggplot  
 base\_size       to pass to ggplot

### Value

ggplot object

### Examples

```

df <- loewesadditivity::cyrpa_ripr
df$dose_A <- df$CyRPA
df$dose_B <- df$RIPR
data <- fortify_gia_data(df)
model_params <- c("beta_A" = .5, "beta_B" = .5,
                  "gamma_A" = .5, "gamma_B" = .5,
                  "tau_1" = 0, "tau_2" = 0)

n_boot <- 10
GIA_fn <- base_GIA
S_fn <- calc_S_base
fn_list <- NULL
alpha <- .05
verbose <- FALSE
out <- estimate_params(data = data,
  init_params = model_params,
  n_boot = n_boot,
  GIA_fn = GIA_fn,
  S_fn = S_fn,
  fn_list = fn_list,
  alpha = alpha,
  verbose = verbose)
plot_curves(out, dose_A = "CyRPA",
  dose_B = "RIPR")

```

---

plot\_surface

*Plot the surface and observations*

---

### Description

Plot the surface and observations

### Usage

```

plot_surface(
  est_list,
  GIA_fn = base_GIA,
  fn_list = NULL,
  xlab = "Dose A",

```



---

 rh5\_ama1ron2

*RH5 and AMAIRON2*


---

**Description**

The data is the raw data for a combination dose of RH5 and AMAIRON2. The data was collected by PEOPLE and on DATE on this GRANT.

**Usage**

```
rh5_ama1ron2
```

**Format**

a 38 x 15 data set where the columns are of the following format

**well** one of iRBC (the max), uRBC (the min), RPMI (??), or comb (which is short for combination)

**AMAIRON2** dose of AMAIRON2 in mg/mL

**RH5** dose of RH5 in mg/mL

**expxyrepz** the results from experiment x, sub item y, repetition z

**Examples**

```
data("rh5_ama1ron2")
head(rh5_ama1ron2)
```

---

 rh5\_rh4

*RH5 and RH4*


---

**Description**

The data is the raw data for a combination dose of RH5 and RH4. The data was originally published in Williams et al. (2018).

**Usage**

```
rh5_rh4
```

**Format**

a 48 x 3 data set where the columns are of the following format

**RH4** dose of RH4 in mg/mL

**RH5** dose of RH5 in mg/mL

**GIA** Percent Growth inhibition assay averaged over two experiments



**Examples**

```
data("rh5_rh4")
head(rh5_rh4)
```

---

simulate_coverage	<i>Simulate a GIA model with an assumed error structure</i>
-------------------	---

---

**Description**

Simulate a GIA model with an assumed error structure

**Usage**

```
simulate_coverage(
  n_sims = 10,
  n_boot = 100,
  verbose = TRUE,
  experimental_grid,
  model_par,
  alpha = 0.05,
  noise_par = c(a0 = 2, a1 = 0.01),
  GIA_fn = base_GIA,
  S_fn = calc_S_base,
  fn_list = NULL
)
```

**Arguments**

n_sims	number of coverage simulations
n_boot	number of bootstraps to use in each simulation
verbose	logical indicating whether we should use print statements. Default is TRUE
experimental_grid	data frame with columns 'dose_A' and 'dose_B'
model_par	named vector of parameters corresponding to those used in GIA_fn()
alpha	alpha level used to produce confidence intervals for each bootstrap
noise_par	named vector for the noise parameter. Must have names "a0" and "a1". See ?base_gia for more details.
GIA_fn	function used to calculate GIA. Default is base_GIA().
S_fn	function to calculate S
fn_list	additional parameters to pass to GIA_fn

**Value**

list with the following entries

**interaction\_cov** This is the percent of times 0 was in the  $(1-\alpha)\%$  confidence interval for the interaction term "tau\_1" from the simulated results

**params\_cov** This is the percent of times the true model parameter (those from model\_par) lies in the (marginal) 95% confidence interval for that model parameter.

**tau\_pos** This is the percent of times the  $(1-\alpha)\%$  CI of "tau\_1" was completely above 0.

**tau\_neg** This is the percent of times  $(1-\alpha)\%$  CI of "tau\_1" is completely below zero

**Examples**

```
df <- loewesadditivity::cyrpa_ripr
df$dose_A <- df$CyRPA
df$dose_B <- df$RIPR
data <- fortify_gia_data(df)
model_params <- c("beta_A" = .247, "beta_B" = .224,
                 "gamma_A" = .734, "gamma_B" = .806,
                 "tau_1" = .28, "tau_2" = -.28)
experimental_grid <- make_grid(par = model_params,
                              n = 5)

n_boot <- 100
n_sims <- 10
GIA_fn <- base_GIA
S_fn <- calc_S_base
fn_list <- NULL
alpha <- .05
verbose <- TRUE
## NOT RUN
##out <- simulate_coverage(n_sims = n_sims,
  ##                               n_boot = n_boot,
  ##                               verbose = TRUE,
  ##                               experimental_grid = experimental_grid,
  ##                               model_par = model_params,
  ##                               alpha = .05,
  ##                               noise_par = c("a0" = 3, "a1" = .01),
  ##                               GIA_fn = base_GIA,
  ##                               fn_list = NULL)
##out
```

---

SSE\_GIA

*Calculate the Sum of Squared Error*

---

**Description**

Calculate the Sum of Squared Error

**Usage**

```
SSE_GIA(par, data, GIA_fn = base_GIA, fn_list = NULL)
```

**Arguments**

par	named vector of parameters
data	<ul style="list-style-type: none"><li>• dose_Adose A mg/mL</li><li>• dose_Bdose B mg/mL</li><li>• GIAGIA</li></ul>
GIA_fn	function to calculate GIA
fn_list	additional arguments to pass GIA_fn

**Value**

sum of square error between observed and estimated

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