

# Package ‘latentcor’

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**Type** Package

**Title** Fast Computation of Latent Correlations for Mixed Data

**Version** 2.0.1

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**Description** The first stand-alone R package for computation of latent correlation that takes into account all variable types (continuous/binary/ordinal/zero-inflated), comes with an optimized memory footprint, and is computationally efficient, essentially making latent correlation estimation almost as fast as rank-based correlation estimation.

The estimation is based on latent copula Gaussian models.

For continuous/binary types, see Fan, J., Liu, H., Ning, Y., and Zou, H. (2017).

For ternary type, see Quan X., Booth J.G. and Wells M.T. (2018) <[arXiv:1809.06255](https://arxiv.org/abs/1809.06255)>.

For truncated type or zero-

inflated type, see Yoon G., Carroll R.J. and Gaynanova I. (2020) <[doi:10.1093/biomet/asaa007](https://doi.org/10.1093/biomet/asaa007)>.

For approximation method of computation, see Yoon G., Müller C.L. and Gaynanova I. (2021) <[doi:10.1080/10618600.2021.1882468](https://doi.org/10.1080/10618600.2021.1882468)>. The latter method uses multi-linear interpolation originally implemented in the R package <<https://cran.r-project.org/package=chebpol>>.

**Depends** R (>= 3.0.0)

**Imports** stats, pcaPP, fMultivar, mnormt, Matrix, MASS, heatmaply, ggplot2, plotly, graphics, geometry, doFuture, foreach, future, doRNG, microbenchmark

**License** GPL-3

**Encoding** UTF-8

**RoxygenNote** 7.2.1

**Suggests** rmarkdown, markdown, knitr, testthat (>= 3.0.0), lattice, cubature, plot3D, covr

**VignetteBuilder** knitr

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**NeedsCompilation** yes

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evaluation	<i>Numerical evaluation for different estimation methods.</i>
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### Description

Speed and accuracy comparison of two different estimation methods.

### Usage

```
evaluation(
  genfun,
  estfun_1,
  estfun_2,
  grid_list,
  nrep = 100,
  showplot = FALSE,
  cores = detectCores(),
  ...
)
```

### Arguments

genfun	A data generation function.
estfun_1	A function for first estimation method.
estfun_2	A function for second estimation method.
grid_list	A list for grid points to be evaluated (each element of list is a vector represents ticklabels on a dimension). The number of list elements are the dimension of function inputs.
nrep	Number of replications in simulation.

showplot	Logical indicator. showplot = TRUE generates the heatmaps of output arrays. NULL if showplot = FALSE.
cores	The numbers of cores (threads) of your machine to conduct parallel computing.
...	Other inputs for data generation or estimation functions to be passed through.

## Value

evaluation returns

- meanAE\_1: An array for mean absolute error of first estimation method.
- meanAE\_2: An array for mean absolute error of second estimation method.
- medianAE\_1: An array for median absolute error of first estimation method.
- medianAE\_2: An array for median absolute error of second estimation method.
- maxAE\_1: An array for maximum absolute error of first estimation method.
- maxAE\_2: An array for maximum absolute error of second estimation method.
- meanAE\_diff: An array for mean absolute error of difference between two estimations.
- medianAE\_diff: An array for median absolute error of difference between two estimations.
- maxAE\_diff: An array for maximum absolute error of difference between two estimations.
- mediantime\_1: An array for median time of first estimation method.
- mediantime\_2: An array for median time of second estimation method.
- plot\_meanAE\_1: A plot for mean absolute error of first estimation method.
- plot\_meanAE\_2: A plot for mean absolute error of second estimation method.
- plot\_medianAE\_1: A plot for median absolute error of first estimation method.
- plot\_medianAE\_2: A plot for median absolute error of second estimation method.
- plot\_maxAE\_1: A plot for maximum absolute error of first estimation method.
- plot\_maxAE\_2: A plot for maximum absolute error of second estimation method.
- plot\_meanAE\_diff: A plot for mean absolute error of difference between two estimations.
- plot\_medianAE\_diff: A plot for median absolute error of difference between two estimations.
- plot\_maxAE\_diff: A plot for maximum absolute error of difference between two estimations.
- plot\_mediantime\_1: A plot for median time of first estimation method.
- plot\_mediantime\_2: A plot for median time of second estimation method.

gen\_data

*Mixed type simulation data generator***Description**

Generates data of mixed types from the latent Gaussian copula model.

**Usage**

```
gen_data(
  n = 100,
  types = c("ter", "con"),
  rhos = 0.5,
  copulas = "no",
  XP = NULL,
  showplot = FALSE
)
```

**Arguments**

n	A positive integer indicating the sample size. The default value is 100.
types	A vector indicating the type of each variable, could be "con" (continuous), "bin" (binary), "tru" (truncated) or "ter" (ternary). The number of variables is determined based on the length of types, that is $p = \text{length}(\text{types})$ . The default value is <code>c("ter", "con")</code> which creates two variables: the first one is ternary, the second one is continuous.
rhos	A vector with lower-triangular elements of desired correlation matrix, e.g. <code>rhos = c(.3, .5, .7)</code> means the correlation matrix is <code>matrix(c(1, .3, .5, .3, 1, .7, .5, .7, 1), 3, 3)</code> . If only a scalar is supplied ( <code>length(rhos) = 1</code> ), then equi-correlation matrix is assumed with all pairwise correlations being equal to rhos. The default value is 0.5 which means correlations between any two variables are 0.5.
copulas	A vector indicating the copula transformation $f$ for each of the $p$ variables, e.g. $U = f(Z)$ . Each element can take value "no" ( $f$ is identity), "expo" (exponential transformation) or "cube" (cubic transformation). If the vector has length 1, then the same transformation is applied to all $p$ variables. The default value is "no": no copula transformation for any of the variables.
XP	A list of length $p$ indicating proportion of zeros (for binary and truncated), and proportions of zeros and ones (for ternary) for each of the variables. For continuous variable, NA should be supplied. If NULL, the following values are automatically generated as elements of XP list for the corresponding data types: For continuous variable, the corresponding value is NA; for binary or truncated variable, the corresponding value is a number between 0 and 1 representing the proportion of zeros, the default value is 0.5; for ternary variable, the corresponding value is a pair of numbers between 0 and 1, the first number indicates the the proportion of zeros, the second number indicates the proportion of ones. The

sum of a pair of numbers should be between 0 and 1, the default value is  $c(0.3, 0.5)$ .

showplot Logical indicator. If TRUE, generates the plot of the data when number of variables  $p$  is no more than 3. The default value is FALSE.

### Value

gen\_data returns a list containing

- X: Generated data matrix (n by p) of observed variables.
- plotX: Visualization of the data matrix X. Histogram if  $p=1$ . 2D Scatter plot if  $p=2$ . 3D scatter plot if  $p=3$ . Returns NULL if showplot = FALSE.

### References

Fan J., Liu H., Ning Y. and Zou H. (2017) "High dimensional semiparametric latent graphical model for mixed data" [doi:10.1111/rssb.12168](https://doi.org/10.1111/rssb.12168).

Yoon G., Carroll R.J. and Gaynanova I. (2020) "Sparse semiparametric canonical correlation analysis for data of mixed types" [doi:10.1093/biomet/asaa007](https://doi.org/10.1093/biomet/asaa007).

### Examples

```
# Generate single continuous variable with exponential transformation (always greater than 0)
# and show histogram.
simdata = gen_data(n = 100, copulas = "expo", types = "con", showplot = FALSE)
X = simdata$X; plotX = simdata$plotX
# Generate a pair of variables (ternary and continuous) with default proportions
# and without copula transformation.
simdata = gen_data()
X = simdata$X
# Generate 3 variables (binary, ternary and truncated)
# corresponding copulas for each variables are "no" (no transformation),
# "cube" (cube transformation) and "cube" (cube transformation).
# binary variable has 30% of zeros, ternary variable has 20% of zeros
# and 40% of ones, truncated variable has 50% of zeros.
# Then show the 3D scatter plot (data points project on either 0 or 1 on Axis X1;
# on 0, 1 or 2 on Axis X2; on positive domain on Axis X3)
simdata = gen_data(n = 100, rhos = c(.3, .4, .5), copulas = c("no", "cube", "cube"),
  types = c("bin", "ter", "tru"), XP = list(.3, c(.2, .4), .5), showplot = TRUE)
X = simdata$X; plotX = simdata$plotX
# Check the proportion of zeros for the binary variable.
sum(simdata$X[, 1] == 0)
# Check the proportion of zeros and ones for the ternary variable.
sum(simdata$X[, 2] == 0); sum(simdata$X[, 2] == 1)
# Check the proportion of zeros for the truncated variable.
sum(simdata$X[, 3] == 0)
```

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get_types	<i>Automatically determine types of each variable (continuous/binary/ternary/truncated) in a data matrix.</i>
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### Description

Automatically determine types of each variable (continuous/binary/ternary/truncated) in a data matrix.

### Usage

```
get_types(X, tru_prop = 0.05)
```

### Arguments

X	A numeric data matrix (n by p), where n is number of samples, and p is number of variables. Missing values (NA) are allowed.
tru_prop	A scalar between 0 and 1 indicating the minimal proportion of zeros that should be present in a variable to be treated as "tru" (truncated type or zero-inflated) rather than as "con" (continuous type). The default value is 0.05 (any variable with more than 5% of zero values among n samples is treated as truncated or zero-inflated)

### Value

get\_types returns

- types: A vector of length p indicating the type of each of the p variables in X. Each element is one of "con" (continuous), "bin" (binary), "ter" (ternary) or "tru" (truncated).

### Examples

```
X = gen_data(types = c("ter", "con"))$X
get_types(X)
```

---

interpolant	<i>Evaluate an interpolant in a point</i>
-------------	---

---

### Description

An interpolant is a function returned by [ipol](#) which has prespecified values in some points, and which fills in between with some reasonable values.

**Arguments**

x	The argument of the function. A function of more than one variable takes a vector. x can also be a matrix of column vectors.
threads	The number of threads to use for evaluation. All interpolants created by <code>ipol</code> are parallelized. If given a matrix argument x, the vectors can be evaluated in parallel.
...	Other parameters. Currently used for simplex linear interpolants with the logical argument <code>blend=c("linear", "cubic", "sigmoid")</code> where a blending function can be chosen.

**Value**

A numeric. If more than one point was evaluated, a vector.

**Author(s)**

Simen Gaure

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interpolation	<i>Parallel version of multilinear interpolation generator for function approximation</i>
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**Description**

Parallel version of multilinear interpolation generator for function approximation

The primary method is `ipol` which dispatches to some other method. All the generated [interpolants](#) accept as an argument a matrix of column vectors. The generated functions also accept an argument `threads=getOption('ipol.threads')` to utilize more than one CPU if a matrix of column vectors is evaluated. The option `ipol.threads` is initialized from the environment variable `IPOL_THREADS` upon loading of the package. It defaults to 1.

**Usage**

```
interpolation(evalfun, grid_list, cores = detectCores(), int = FALSE, ...)
```

**Arguments**

evalfun	The objective function to be approximated.
grid_list	A list for grid points (each element of list is a vector represents ticklabels on a dimension). The number of list elements are the dimension of function inputs.
cores	The numbers of cores (threads) of your machine to conduct parallel computing.
int	Logical indicator. <code>int = TRUE</code> interpolant value multiplied by $10^7$ then convert to interger to save memory. Original interpolant if <code>int = FALSE</code> .
...	Other inputs for objective functions to be passed through.

**Details**

The interpolants are ordinary R-objects and can be saved with `save()` and loaded later with `load()` or serialized/unserialized with other tools, just like any R-object. However, they contain calls to functions in the package, and while the author will make efforts to ensure that generated interpolants are compatible with future versions of **ipol**, I can issue no such absolute guarantee.

**Value**

`interpolation` returns

- `value`: A list of of length `p` corresponding to each variable. Returns NA for continuous variable; proportion of zeros for binary/truncated variables; the cumulative proportions of zeros and ones (e.g. first value is proportion of zeros, second value is proportion of zeros and ones) for ternary variable.
- `interpolant`: An interpolant function generated by `chebpol::chebpol` for interpolation.

**See Also**

[ipol](#), [interpolant](#)

**Examples**

```
## Not run: grid_list = list(seq(-0.5, 0.5, by = 0.5), seq(-0.5, 0.5, by = 0.5))
objfun = function(x, y) {x^2 + sqrt(y)}
evalfun = function(X) {objfun(X[1], X[2])}
value = interpolation(evalfun = evalfun, grid_list = grid_list)$value
interpolant = interpolation(evalfun = evalfun, grid_list = grid_list)$interpolant
## End(Not run)
```

---

`ipol`

*Create an interpolating function from given values. Several interpolation methods are supported.*

---

**Description**

Create an interpolating function from given values. Several interpolation methods are supported.

**Usage**

```
ipol(val, grid = NULL, ...)
```

**Arguments**

`val` array or function. Function values on a grid.

`grid` list. Each element is a vector of ordered grid-points for a dimension.

`...` Further arguments to the function, if `is.function(val)`. And some extra arguments for interpolant creation described in section `Details`.



**Value**

A function(`x`, `threads=getOption('chebpol.threads')`) defined on a hypercube, an [interpolant](#) for the given function. The argument `x` can be a matrix of column vectors which are evaluated in parallel in a number of threads. The function yields values for arguments outside the hypercube as well, though it will typically be a poor approximation. `threads` is an integer specifying the number of parallel threads which should be used when evaluating a matrix of column vectors.

**Author(s)**

Simen Gaure

**Examples**

```
## evenly spaced grid-points
su <- seq(0,1,length.out=10)
## irregularly spaced grid-points
s <- su^3
## create approximation on the irregularly spaced grid
m11 <- ipol(exp(s), grid=list(s))
## test it, since exp is convex, the linear approximation lies above
## the exp between the grid points
m11(su) - exp(su)

## multi dimensional approximation
f <- function(x) 10/(1+25*mean(x^2))
# a 3-dimensional 10x10x10 grid, first and third coordinate are non-uniform
grid <- list(s, su, sort(1-s))

# make multilinear spline.
m12 <- ipol(array(apply(expand.grid(grid), 1, f), c(10, 10, 10)), grid=grid)
# make 7 points in R3 to test them on
m <- matrix(runif(3*7),3)
rbind(true=apply(m,2,f), ml=m12(m))
```

---

latentcor

*Estimate latent correlation for mixed types.*

---

**Description**

Estimation of latent correlation matrix from observed data of (possibly) mixed types (continuous/binary/truncated/ternary) based on the latent Gaussian copula model. Missing values (NA) are allowed. The estimation is based on pairwise complete observations.

**Usage**

```
latentcor(
  X,
  types = NULL,
  method = c("approx", "original"),
  use.nearPD = TRUE,
  nu = 0.001,
  tol = 1e-08,
  ratio = 0.9,
  showplot = FALSE
)
```

**Arguments**

<code>X</code>	A numeric matrix or numeric data frame (n by p), where n is number of samples, and p is number of variables. Missing values (NA) are allowed, in which case the estimation is based on pairwise complete observations.
<code>types</code>	A vector of length p indicating the type of each of the p variables in X. Each element must be one of "con" (continuous), "bin" (binary), "ter" (ternary) or "tru" (truncated). If the vector has length 1, then all p variables are assumed to be of the same type that is supplied. The default value is NULL, and the variable types are determined automatically using function <code>get_types</code> . As automatic determination of variable types takes extra time, it is recommended to supply the types explicitly when they are known in advance.
<code>method</code>	The calculation method for latent correlations. Either "original" or "approx". If <code>method = "approx"</code> , multilinear approximation method is used, which is much faster than the original method, see Yoon et al. (2021) for timing comparisons for various variable types. If <code>method = "original"</code> , optimization of the bridge inverse function is used. The default is "approx".
<code>use.nearPD</code>	Logical indicator. <code>use.nearPD = TRUE</code> gets nearest positive definite matrix for the estimated latent correlation matrix with shrinkage adjustment by nu. Output R is the same as <code>Rpointwise</code> if <code>use.nearPD = FALSE</code> . Default value is TRUE.
<code>nu</code>	Shrinkage parameter for the correlation matrix, must be between 0 and 1. Guarantees that the minimal eigenvalue of returned correlation matrix is greater or equal to nu. When <code>nu = 0</code> , no shrinkage is performed, the returned correlation matrix will be semi-positive definite but not necessarily strictly positive definite. When <code>nu = 1</code> , the identity matrix is returned (not recommended). The default (recommended) value is 0.001.
<code>tol</code>	When <code>method = "original"</code> , specifies the desired accuracy of the bridge function inversion via uniroot optimization and is passed to <code>optimize</code> . The default value is 1e-8. When <code>method = "approx"</code> , this parameter is ignored.
<code>ratio</code>	When <code>method = "approx"</code> , specifies the boundary value for multilinear interpolation, must be between 0 and 1. When <code>ratio = 0</code> , no linear interpolation is performed (the slowest execution) which is equivalent to <code>method = "original"</code> . When <code>ratio = 1</code> , linear interpolation is always performed (the fastest execution) but may lead to high approximation errors. The default (recommended) value is

0.9 which controls the approximation error and has fast execution, see Yoon et al. (2021) for details. When `method = "original"`, this parameter is ignored.

`showplot` Logical indicator. `showplot = TRUE` generates a ggplot object `plotR` with the heatmap of latent correlation matrix `R`. `plotR = NULL` if `showplot = FALSE`. Default value is `FALSE`.

## Details

The function estimates latent correlation by calculating inverse bridge function (Fan et al., 2017) evaluated at the value of sample Kendall's tau ( $\hat{\tau}$ ). The bridge function `F` connects Kendall's tau to latent correlation `r` so that  $F(r) = E(\hat{\tau})$ . The form of function `F` depends on the variable types (continuous/binary/truncated/ternary), but is exact. The exact form of inverse is not available, so has to be evaluated numerically for each pair of variables leading to `Rpointwise`.

When `method = "original"`, the inversion is done numerically by solving

$$\text{minimize}_r (F(r) - \hat{\tau})^2$$

using `optimize`. The parameter `tol` is used to control the accuracy of the solution.

When `method = "approx"`, the inversion is done approximately by interpolating previously calculated and stored values of  $F^{-1}(\hat{\tau})$ . This is significantly faster than the original method (Yoon et al., 2021) for binary/ternary/truncated cases, however the approximation errors may be non-negligible on some regions of the space. The parameter `ratio` controls the region where the interpolation is performed with default recommended value of 0.9 giving a good balance of accuracy and computational speed. Increasing the value of `ratio` may improve speed (but possibly sacrifice the accuracy), whereas decreasing the value of `ratio` may improve accuracy (but possibly sacrifice the speed). See Yoon et al. 2021 and vignette for more details.

In case the pointwise estimator `Rpointwise` has negative eigenvalues, it is projected onto the space of positive semi-definite matrices using `nearPD`. The parameter `nu` further allows to perform additional shrinkage towards identity matrix (desirable in cases where the number of variables `p` is very large) as

$$R = (1 - \nu)\tilde{R} + \nu I,$$

where  $\tilde{R}$  is `Rpointwise` after projection by `nearPD`.

## Value

`latentcor` returns

- `zratios`: A list of length `p` corresponding to each variable. Returns `NA` for continuous variable; proportion of zeros for binary/truncated variables; the cumulative proportions of zeros and ones (e.g. first value is proportion of zeros, second value is proportion of zeros and ones) for ternary variable.
- `K`: (`p x p`) Kendall Tau (Tau-a) Matrix for `X`
- `R`: (`p x p`) Estimated latent correlation matrix for `X`
- `Rpointwise`: (`p x p`) Point-wise estimates of latent correlations for `X`. This matrix is not guaranteed to be semi-positive definite. This is the original estimated latent correlation matrix without adjustment for positive-definiteness.
- `plotR`: Heatmap plot of latent correlation matrix `R`, `NULL` if `showplot = FALSE`

## References

Fan J., Liu H., Ning Y. and Zou H. (2017) "High dimensional semiparametric latent graphical model for mixed data" [doi:10.1111/rssb.12168](https://doi.org/10.1111/rssb.12168).

Yoon G., Carroll R.J. and Gaynanova I. (2020) "Sparse semiparametric canonical correlation analysis for data of mixed types" [doi:10.1093/biomet/asaa007](https://doi.org/10.1093/biomet/asaa007).

Yoon G., Müller C.L., Gaynanova I. (2021) "Fast computation of latent correlations" [doi:10.1080/10618600.2021.1882468](https://doi.org/10.1080/10618600.2021.1882468).

## Examples

```
# Example 1 - truncated data type, same type for all variables
# Generate data
X = gen_data(n = 300, types = rep("tru", 5))$X
# Estimate latent correlation matrix with original method and check the timing
start_time = proc.time()
R_org = latentcor(X = X, types = "tru", method = "original")$R
proc.time() - start_time
# Estimate latent correlation matrix with approximation method and check the timing
start_time = proc.time()
R_approx = latentcor(X = X, types = "tru", method = "approx")$R
proc.time() - start_time
# Heatmap for latent correlation matrix.
Heatmap_R_approx = latentcor(X = X, types = "tru", method = "approx",
                             showplot = TRUE)$plotR

# Example 2 - ternary/continuous case
X = gen_data()$X
# Estimate latent correlation matrix with original method
R_nc_org = latentcor(X = X, types = c("ter", "con"), method = "original")$R
# Estimate latent correlation matrix with approximation method
R_nc_approx = latentcor(X = X, types = c("ter", "con"), method = "approx")$R
```

---

r\_ml\_wrapper

*Port function to call multilinear interpolants for continuous developers.*

---

## Description

Port function to call multilinear interpolants for continuous developers.

## Usage

```
r_ml_wrapper(K, zratio1, zratio2, comb)
```

**Arguments**

K	Kendall's tau, can be provided as a number or a vector for interpolation in batch.
zratio1	zratio for first variable. NA for continuous variables, zeros proportions for binary, truncated variables. For ternary variables, a vector of proportion of zeros as first element, proportions of zeros and ones as second element. It can be provided as a vector (matrix) for interpolation in batch. See vignettes for detail.
zratio2	zratio for second variable. NA for continuous variables, zeros proportions for binary, truncated variables. For ternary variables, a vector of proportion of zeros as first element, proportions of zeros and ones as second element. It can be provided as a vector (matrix) for interpolation in batch. See vignettes for detail.
comb	Numeric code for types: "10" for binary/continuous; "11" for binary/binary; "20" for truncated/continuous; "21" for truncated/binary; "22" for truncated/truncated; "30" for ternary/continuous; "31" for ternary/binary; "32" for ternary/truncated; "33" for ternary/ternary.

**Value**

A number or vector of interpolation results.

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