

Package ‘BFI’

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Type Package

Title Bayesian Federated Inference

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Description The Bayesian Federated Inference ('BFI') method combines inference results obtained from local data sets in the separate centers. In this version of the package, the 'BFI' methodology is programmed for linear, logistic and survival regression models. For GLMs, see Jonker, Pazira and Coolen (2024) <[doi:10.1002/sim.10072](https://doi.org/10.1002/sim.10072)>; for survival models, see Pazira, Massa, Weijers, Coolen and Jonker (2024) <[doi:10.48550/arXiv.2404.17464](https://doi.org/10.48550/arXiv.2404.17464)>; and for heterogeneous populations, see Jonker, Pazira and Coolen (2024) <[doi:10.48550/arXiv.2402.02898](https://doi.org/10.48550/arXiv.2402.02898)>.

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URL <https://hassanpazira.github.io/BFI/>

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Contents

BFI-package	2
b.diag	3
bfi	4
hazards.fun	13
inv.prior.cov	16
MAP.estimation	20
n.par	28
Nurses	29
summary.bfi	30
surv.simulate	32
trauma	36
Index	37

BFI-package	<i>Bayesian Federated Inference</i>
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Description

The Bayesian Federated Inference method combines inference results from different (medical) centers without sharing the data. In this version of the package, the user can fit models specifying Gaussian, Binomial (Logistic) and Survival families.

Details

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MAP.estimation and bfi are the main functions. All other functions are utility functions.

Some examples are provided in the vignettes accompanying this package in order to show how the package can be applied to real data. The vignettes can be found on the package website at <https://hassanpazira.github.io/BFI/> or within R once the package has been installed, e.g., via vignette("BFI", package = "BFI").

Author(s)

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References

Jonker M.A., Pazira H. and Coolen A.C.C. (2024). *Bayesian federated inference for estimating statistical models based on non-shared multicenter data sets*, *Statistics in Medicine*, 43(12): 2421-2438. <<https://doi.org/10.1002/sim.10072>>

Pazira H., Massa E., Weijers J.A.M., Coolen A.C.C. and Jonker M.A. (2024). *Bayesian Federated Inference for Survival Models*, *arXiv*. <<https://arxiv.org/abs/2404.17464>>

Jonker M.A., Pazira H. and Coolen A.C.C. (2024). *Bayesian Federated Inference for regression models with heterogeneous multi-center populations*, *arXiv*. <<https://arxiv.org/abs/2402.02898>>

b.diag

Create a Block Diagonal Matrix

Description

Construct a block diagonal matrix using multiple given block matrices.

Usage

```
b.diag(..., fill = 0)
```

Arguments

... individual matrices or one list of matrices.
fill non-block-diagonal elements. Default is 0.

Details

Avoid combining matrices and lists for the ... argument.

b.diag() covers the arguments of type "character".

If a *sparse* matrix needed, run the following:

```
library(Matrix); Matrix(b_diag, sparse = TRUE)
```

where b_diag is the matrix returned by b.diag().

Value

b.diag() returns a block diagonal matrix obtained by combining the arguments.

Author(s)

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Examples

```

b.diag(1, matrix(1:3, 3,4), diag(3:2))

b.diag(matrix(1:6, 2), as.character(2))

lists <- list(1, 2:3, diag(4:6), 7, cbind(8,9:12), 13:15)
b.diag(lists)
identical(b.diag(lists), b.diag(lapply(lists, as.matrix)))

b.diag(replicate(3, matrix(round(rnorm(9)), 3, 3), simplify=FALSE))

```

bfi*Bayesian Federated Inference*

Description

bfi function can be used (on the central server) to combine inference results from separate datasets (without combining the data) to approximate what would have been inferred had the datasets been merged. This function can handle linear, logistic and survival regression models.

Usage

```

bfi(theta_hats = NULL,
     A_hats,
     Lambda,
     family = c("gaussian", "binomial", "survival"),
     stratified = FALSE,
     strat_par = NULL,
     center_spec = NULL,
     basehaz = c("weibul", "exp", "gomp", "poly", "pwexp"),
     theta_A_polys = NULL,
     q_ls,
     center_zero_sample = FALSE,
     which_cent_zeros,
     zero_sample_covs,
     refer_cats,
     zero_cats,
     lev_no_ref_zeros)

```

Arguments

theta_hats	a list of L vectors of the maximum a posteriori (MAP) estimates of the model parameters in the L centers. These vectors must have equal dimensions. See ‘Details’.
A_hats	a list of L minus curvature matrices for L centers. These matrices must have equal dimensions. See ‘Details’.

family	a character string representing the family name used for the local centers. Can be abbreviated.
Lambda	a list of $L + 1$ matrices. The k matrix is the chosen inverse variance-covariance matrix of the Gaussian distribution that is used as prior distribution in center k , where $k = 1, 2, \dots, L$. The last matrix is the chosen variance-covariance matrix for the Gaussian prior of the (fictive) combined data set. If <code>stratified = FALSE</code> , all $L + 1$ matrices must have equal dimensions. While, if <code>stratified = TRUE</code> , the first L matrices must have equal dimensions and the last matrix should have a different (greater) dimension than the others. See ‘Details’.
stratified	logical flag for performing the stratified analysis. If <code>stratified = TRUE</code> , the parameter(s) selected in the <code>strat_par</code> argument are allowed to be different across centers, except when the argument <code>center_spec</code> is not NULL. Default is <code>stratified = FALSE</code> . See ‘Details’ and ‘Examples’.
strat_par	a one- or two-element integer vector for indicating the stratification parameter(s). The values 1 and/or 2 are/is used to indicate that the “intercept” and/or “sigma2” are allowed to vary, respectively. This argument is used only when <code>stratified = TRUE</code> and <code>center_spec = NULL</code> . Default is <code>strat_par = NULL</code> , but if <code>stratified = TRUE</code> , <code>strat_par</code> can not be NULL unless there is a center specific variable. For the binomial family the length of the vector should be at most one which refers to “intercept”, and the value of this element should be 1. For gaussian family this vector can be 1 for indicating the “intercept” only, 2 for indicating the “sigma2” only, and <code>c(1, 2)</code> for both “intercept” and “sigma2”. See ‘Details’ and ‘Examples’.
center_spec	a vector of L elements for representing the center specific variable. This argument is used only when <code>stratified = TRUE</code> and <code>strat_par = NULL</code> . Each element represents a specific feature of the corresponding center. There must be only one specific value or attribute for each center. This vector could be a numeric, characteristic or factor vector. Note that, the order of the centers in the vector <code>center_spec</code> must be the same as in the list of the argument <code>theta_hats</code> . The used data type in the argument <code>center_spec</code> must be categorical. Default is <code>center_spec = NULL</code> . See also ‘Details’ and ‘Examples’.
basehaz	a character string representing one of the available baseline hazard functions; exponential (“exp”), Weibull (“weibul”, the default), Gompertz (“gomp”), exponentiated polynomial (“poly”), and piecewise exponential (“pwexp”). It is only used when <code>family = "survival"</code> . Can be abbreviated.
theta_A_polys	a list with L elements so that each element is the array <code>theta_A_ploy</code> (the output of the <code>MAP.estimation</code> function, <code>MAP.estimation()\$theta_A_ploy</code>) for the corresponding center. This argument, <code>theta_A_polys</code> , is only used if <code>family = "survival"</code> and <code>basehaz = "poly"</code> . See ‘Details’.
q_ls	a vector with L elements in which each element is the order (minus 1) of the exponentiated polynomial baseline hazard function for the corresponding center, i.e., each element is the value of <code>q_1</code> (the output of the <code>MAP.estimation</code> function, <code>MAP.estimation()\$q_1</code>). This argument, <code>q_ls</code> , is only used if <code>family = "survival"</code> and <code>basehaz = "poly"</code> . It can also be a scalar which represents the maximum value of the <code>q_1</code> ’s across the centers.

<code>center_zero_sample</code>	logical flag indicating whether the center has a categorical covariate with no observations/individuals in one of the categories. Default is <code>center_zero_sample = FALSE</code> . For more details see ‘References’.
<code>which_cent_zeros</code>	an integer vector representing the center(s) which has one categorical covariate with no individuals in one of the categories. It is used if <code>center_zero_sample = TRUE</code> .
<code>zero_sample_covs</code>	a vector in which each element is a character string representing the categorical covariate that has no samples/observations in one of its categories for the corresponding center. Each element of the vector can be obtained from the output of the <code>MAP.estimation()</code> function for the corresponding center, <code>MAP.estimation()\$zero_sample_cov</code> . It is used when <code>center_zero_sample = TRUE</code> .
<code>refer_cats</code>	a vector in which each element is a character string representing the reference category for the corresponding center. Each element of the vector can be obtained from the output of the <code>MAP.estimation()</code> function for the corresponding center, <code>MAP.estimation()\$refer_cat</code> . This vector is used when <code>center_zero_sample = TRUE</code> .
<code>zero_cats</code>	a vector in which each element is a character string representing the category with no samples/observations for the corresponding center. Each element of the vector can be obtained from the output of the <code>MAP.estimation()</code> function for the corresponding center, i.e., <code>MAP.estimation()\$zero_cat</code> . It is used when <code>center_zero_sample = TRUE</code> .
<code>lev_no_ref_zeros</code>	a list in which the number of elements equals the length of the <code>which_cent_zeros</code> argument. Each element of the list is a vector containing the names of the levels of the categorical covariate that has no samples/observations in one of its categories for the corresponding center. However, the name of the category with no samples and the name of the reference category are excluded from this vector. Each element of the list can be obtained from the output of the <code>MAP.estimation()</code> function, i.e., <code>MAP.estimation()\$lev_no_ref_zero</code> . This argument is used if <code>center_zero_sample = TRUE</code> .

Details

`bfi` function implements the BFI approach described in the papers Jonker et. al. (2024a), Pazira et. al. (2024) and Jonker et. al. (2024b) given in the references. The inference results gathered from different (L) centers are combined, and the BFI estimates of the model parameters and curvature matrix evaluated at that point are returned.

The inference result from each center must be obtained using the `MAP.estimation` function separately, and then all of these results (coming from different centers) should be compiled into a list to be used as an input of `bfi()`. The models in the different centers should be defined in exactly the same way; among others, exactly the same covariates should be included in the models. The parameter vectors should be defined exactly the same, so that the L vectors and matrices in the input lists `theta_hat`'s and `A_hat`'s are defined in the same way (e.g., the covariates need to be included in the models in the same order).

Note that the order of the elements in the lists `theta_hats`, `A_hats` and `Lambda`, must be the same with respect to the centers, so that in every list the element at the ℓ position is from the center ℓ . This should also be the case for the vector `center_spec`.

If for the locations `intercept = FALSE`, the stratified analysis is not possible anymore for the binomial family.

If `stratified = FALSE`, both `strat_par` and `center_spec` must be `NULL` (the defaults), while if `stratified = TRUE` only one of the two must be `NULL`.

If `stratified = FALSE` and all the $L + 1$ matrices in `Lambda` are equal, it is sufficient to give a (list of) one matrix only. In both cases of the `stratified` argument (`TRUE` or `FALSE`), if only the first L matrices are equal, the argument `Lambda` can be a list of two matrices, so that the first matrix represents the chosen variance-covariance matrix for local centers and the second one is the chosen matrix for the combined data set. The last matrix of the list in the argument `Lambda` can be built by the function `inv.prior.cov()`.

If the data type used in the argument `center_spec` is continuous, one can use `stratified = TRUE` and `center_spec = NULL`, and set `strat_par` not to `NULL` (i.e., to 1, 2 or both (1, 2)). Indeed, in this case, the stratification parameter(s) given in the argument `strat_par` are assumed to be different across the centers.

When `family = 'survival'` and `basehaz = 'poly'`, the arguments `theta_hats` and `A_hats` should not be provided. Instead, the `theta_A_polys` and `q_ls` arguments should be defined using the local information, specifically `MAP. estimation()$theta_A_poly` and `MAP. estimation()$q_l`, respectively. See the last example in 'Examples'.

Value

`bfi` returns a list containing the following components:

<code>theta_hat</code>	the vector of estimates obtained by combining the inference results from the L centers with the 'BFI' methodology. If an intercept was fitted in every center and <code>stratified = FALSE</code> , there is only one general "intercept" in this vector, while if <code>stratified = TRUE</code> and <code>strat_par = 1</code> , there are L different intercepts in the model, for each center one;
<code>A_hat</code>	minus the curvature (or Hessian) matrix obtained by the 'BFI' method for the combined model. If <code>stratified = TRUE</code> , the dimension of the matrix is always greater than when <code>stratified = FALSE</code> ;
<code>sd</code>	the vector of standard deviation of the estimates in <code>theta_hat</code> obtained from the matrix in <code>A_hat</code> , i.e., the vector equals <code>sqrt(diag(solve(A_hat)))</code> which equals the square root of the elements at the diagonal of the inverse of the <code>A_hat</code> matrix.
<code>family</code>	the family object used;
<code>basehaz</code>	the baseline hazard function used;
<code>stratified</code>	whether a stratified analysis was done or not.;

Author(s)

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References

Jonker M.A., Pazira H. and Coolen A.C.C. (2024a). *Bayesian federated inference for estimating statistical models based on non-shared multicenter data sets*, *Statistics in Medicine*, 43(12): 2421-2438. <<https://doi.org/10.1002/sim.10072>>

Pazira H., Massa E., Weijers J.A.M., Coolen A.C.C. and Jonker M.A. (2024). *Bayesian Federated Inference for Survival Models*, *arXiv*. <<https://arxiv.org/abs/2404.17464>>

Jonker M.A., Pazira H. and Coolen A.C.C. (2024b). *Bayesian Federated Inference for regression models with heterogeneous multi-center populations*, *arXiv*. <<https://arxiv.org/abs/2402.02898>>

See Also

[MAP.estimation](#) and [inv.prior.cov](#)

Examples

```
#####
## Example 1: y ~ Binomial (L = 2 centers) ##
#####

# Setting a seed for reproducibility
set.seed(112358)

#-----#
# Data Simulation for Local Center 1 #
#-----#
n1 <- 30 # sample size of center 1
X1 <- data.frame(x1=rnorm(n1), # continuous variable
                 x2=sample(0:2, n1, replace=TRUE)) # categorical variable
# make dummy variables
X1x2_1 <- ifelse(X1$x2 == '1', 1, 0)
X1x2_2 <- ifelse(X1$x2 == '2', 1, 0)
X1$x2 <- as.factor(X1$x2)
# regression coefficients
beta <- 1:4 # beta[1] is the intercept
# linear predictor:
eta1 <- beta[1] + X1$x1 * beta[2] + X1x2_1 * beta[3] + X1x2_2 * beta[4]
# inverse of the link function ( g^{-1}(\eta) = \mu ):
mu1 <- binomial()$linkinv(eta1)
y1 <- rbinom(n1, 1, mu1)

#-----#
# Data Simulation for Local Center 2 #
#-----#
n2 <- 50 # sample size of center 2
X2 <- data.frame(x1=rnorm(n2), # continuous variable
                 x2=sample(0:2, n2, replace=TRUE)) # categorical variable
# make dummy variables:
X2x2_1 <- ifelse(X2$x2 == '1', 1, 0)
X2x2_2 <- ifelse(X2$x2 == '2', 1, 0)
X2$x2 <- as.factor(X2$x2)
# linear predictor:
```

```

eta2 <- beta[1] + X2$x1 * beta[2] + X2x2_1 * beta[3] + X2x2_2 * beta[4]
# inverse of the link function:
mu2 <- binomial()$linkinv(eta2)
y2 <- rbinom(n2, 1, mu2)

#-----#
# MAP Estimates at Center 1 #
#-----#
# Assume the same inverse covariance matrix (Lambda) for both centers:
Lambda <- inv.prior.cov(X1, lambda = 0.01, family = 'binomial')
fit1 <- MAP.estimate(y1, X1, family = 'binomial', Lambda)
theta_hat1 <- fit1$theta_hat # intercept and coefficient estimates
A_hat1 <- fit1$A_hat # minus the curvature matrix

#-----#
# MAP Estimates at Center 2 #
#-----#
fit2 <- MAP.estimate(y2, X2, family='binomial', Lambda)
theta_hat2 <- fit2$theta_hat
A_hat2 <- fit2$A_hat

#-----#
# BFI at Central Center #
#-----#
theta_hats <- list(theta_hat1, theta_hat2)
A_hats <- list(A_hat1, A_hat2)
bfi <- bfi(theta_hats, A_hats, Lambda, family='binomial')
class(bfi)
summary(bfi, cur_mat=TRUE)

###-----###
### Stratified Analysis ###
###-----###

# By running the following line an error appears because
# when stratified = TRUE, both 'strat_par' and 'center_spec' can not be NULL:
Just4check1 <- try(bfi(theta_hats, A_hats, Lambda, family = 'binomial',
                    stratified = TRUE), TRUE)
class(Just4check1) # By default, both 'strat_par' and 'center_spec' are NULL!

# By running the following line an error appears because when stratified = TRUE,
# last matrix in 'Lambda' should not have the same dim. as the other local matrices:
Just4check2 <- try(bfi(theta_hats, A_hats, Lambda, stratified = TRUE,
                    strat_par = 1), TRUE)
class(Just4check2) # All matrices in Lambda have the same dimension!

# Stratified analysis when 'intercept' varies across two centers:
newLam <- inv.prior.cov(X1, lambda=c(0.1, 0.3), family = 'binomial',
                    stratified = TRUE, strat_par = 1)
bfi <- bfi(theta_hats, A_hats, list(Lambda, newLam), family = 'binomial',
                    stratified=TRUE, strat_par=1)
summary(bfi, cur_mat=TRUE)

```

```
#####
## Example 2: y ~ Gaussian (L = 3 centers) ##
#####

# Setting a seed for reproducibility
set.seed(112358)

p <- 3 # number of coefficients without 'intercept'
theta <- c(1, rep(2, p), 1.5) # reg. coef.s (theta[1] is 'intercept') & 'sigma2' = 1.5

#-----#
# Data Simulation for Local Center 1 #
#-----#
n1 <- 30 # sample size of center 1
X1 <- data.frame(matrix(rnorm(n1 * p), n1, p)) # continuous variables
# linear predictor:
eta1 <- theta[1] + as.matrix(X1)
# inverse of the link function ( g^{-1}(\eta) = \mu ):
mu1 <- gaussian()$linkinv(eta1)
y1 <- rnorm(n1, mu1, sd = sqrt(theta[5]))

#-----#
# Data Simulation for Local Center 2 #
#-----#
n2 <- 40 # sample size of center 2
X2 <- data.frame(matrix(rnorm(n2 * p), n2, p)) # continuous variables
# linear predictor:
eta2 <- theta[1] + as.matrix(X2)
# inverse of the link function:
mu2 <- gaussian()$linkinv(eta2)
y2 <- rnorm(n2, mu2, sd = sqrt(theta[5]))

#-----#
# Data Simulation for Local Center 3 #
#-----#
n3 <- 50 # sample size of center 3
X3 <- data.frame(matrix(rnorm(n3 * p), n3, p)) # continuous variables
# linear predictor:
eta3 <- theta[1] + as.matrix(X3)
# inverse of the link function:
mu3 <- gaussian()$linkinv(eta3)
y3 <- rnorm(n3, mu3, sd = sqrt(theta[5]))

#-----#
# Inverse Covariance Matrix #
#-----#
# Creating the inverse covariance matrix for the Gaussian prior distribution:
Lambda <- inv.prior.cov(X1, lambda = 0.05, family='gaussian') # the same for both centers

#-----#
# MAP Estimates at Center 1 #
#-----#
```

```

fit1      <- MAP.estimation(y1, X1, family = 'gaussian', Lambda)
theta_hat1 <- fit1$theta_hat # intercept and coefficient estimates
A_hat1    <- fit1$A_hat      # minus the curvature matrix

#-----#
# MAP Estimates at Center 2 #
#-----#
fit2      <- MAP.estimation(y2, X2, family = 'gaussian', Lambda)
theta_hat2 <- fit2$theta_hat
A_hat2    <- fit2$A_hat

#-----#
# MAP Estimates at Center 3 #
#-----#
fit3      <- MAP.estimation(y3, X3, family = 'gaussian', Lambda)
theta_hat3 <- fit3$theta_hat
A_hat3    <- fit3$A_hat

#-----#
# BFI at Central Center #
#-----#
A_hats    <- list(A_hat1, A_hat2, A_hat3)
theta_hats <- list(theta_hat1, theta_hat2, theta_hat3)
bfi       <- bfi(theta_hats, A_hats, Lambda, family = 'gaussian')
summary(bfi, cur_mat=TRUE)

###-----###
### Stratified Analysis ###
###-----###

# Stratified analysis when 'intercept' varies across two centers:
newLam1 <- inv.prior.cov(X1, lambda = c(0.1,0.3), family = 'gaussian',
                        stratified = TRUE, strat_par = 1, L=3)
# 'newLam1' is used the prior for combined data and
# 'Lambda' is used the prior for locals
list_newLam1 <- list(Lambda, newLam1)
bfi1 <- bfi(theta_hats, A_hats, list_newLam1, family = 'gaussian',
            stratified = TRUE, strat_par = 1)
summary(bfi1, cur_mat = TRUE)

# Stratified analysis when 'sigma2' varies across two centers:
newLam2 <- inv.prior.cov(X1, lambda = c(0.1,0.3), family = 'gaussian',
                        stratified = TRUE, strat_par = 2, L = 3)
# 'newLam2' is used the prior for combined data and 'Lambda' is used the prior for locals
list_newLam2 <- list(Lambda, newLam2)
bfi2 <- bfi(theta_hats, A_hats, list_newLam2, family = 'gaussian',
            stratified = TRUE, strat_par=2)
summary(bfi2, cur_mat = TRUE)

# Stratified analysis when 'intercept' and 'sigma2' vary across 2 centers:
newLam3 <- inv.prior.cov(X1, lambda = c(0.1,0.2,0.3), family = 'gaussian',
                        stratified = TRUE, strat_par = c(1, 2), L = 3)
# 'newLam3' is used the prior for combined data and 'Lambda' is used the prior for locals

```

```

list_newLam3 <- list(Lambda, newLam3)
bfi3 <- bfi(theta_hats, A_hats, list_newLam3, family = 'gaussian',
            stratified = TRUE, strat_par = 1:2)
summary(bfi3, cur_mat = TRUE)

###-----###
### Center Specific Covariates ###
###-----###

# Assume the first and third centers have the same center-specific covariate value
# of '3', while this value for the second center is '1', i.e., center_spec = c(3,1,3)
newLam4 <- inv.prior.cov(X1, lambda=c(0.1, 0.2, 0.3), family='gaussian',
                        stratified=TRUE, center_spec = c(3,1,3), L=3)
# 'newLam4' is used the prior for combined data and 'Lambda' is used the prior for locals
l_newLam4 <- list(Lambda, newLam4)
bfi4 <- bfi(theta_hats, A_hats, l_newLam4, family = 'gaussian',
            stratified = TRUE, center_spec = c(3,1,3))
summary(bfi4, cur_mat = TRUE)

#####
## Example 3: Survival family (L = 2 centers) ##
#####

# Setting a seed for reproducibility
set.seed(112358)

p <- 3
theta <- c(1:4, 5, 6) # regression coefficients (1:4) & omega's (5:6)

#-----#
# Simulating Survival data for Local Center 1 #
#-----#
n1 <- 30
X1 <- data.frame(matrix(rnorm(n1 * p), n1, p)) # continuous (normal) variables
# Simulating survival data ('time' and 'status') from 'Weibull' with
# a predefined censoring rate of 0.3:
y1 <- surv.simulate(Z = list(X1), beta = theta[1:p], a = theta[5], b = theta[6],
                    u1 = 0.1, cen_rate = 0.3, gen_data_from = "weibul")$D[[1]][, 1:2]
Lambda <- inv.prior.cov(X1, lambda = c(0.1, 1), family = "survival", basehaz = "poly")
fit1 <- MAP.estimation(y1, X1, family = 'survival', Lambda = Lambda, basehaz = "poly")
theta_hat1 <- fit1$theta_hat # coefficient estimates
A_hat1 <- fit1$A_hat # minus the curvature matrix
summary(fit1, cur_mat=TRUE)

#-----#
# Simulating Survival data for Local Center 2 #
#-----#
n2 <- 30
X2 <- data.frame(matrix(rnorm(n2 * p), n2, p)) # continuous (normal) variables
# Survival simulated data from 'Weibull' with a predefined censoring rate of 0.3:
y2 <- surv.simulate(Z = list(X2), beta = theta[1:p], a = theta[5], b = theta[6], u1 = 0.1,
                    cen_rate = 0.3, gen_data_from = "weibul")$D[[1]][, 1:2]

```

```

fit2 <- MAP.estimation(y2, X2, family = 'survival', Lambda = Lambda, basehaz = "poly")
theta_hat2 <- fit2$theta_hat
A_hat2 <- fit2$A_hat
summary(fit2, cur_mat=TRUE)

#-----#
# BFI at Central Center #
#-----#
# When family = 'survival' and basehaz = "poly", only 'theta_A_polys'
# should be defined instead of 'theta_hats' and 'A_hats':
theta_A_hats <- list(fit1$theta_A_poly, fit2$theta_A_poly)
qls <- c(fit1$q_l, fit2$q_l)
bfi <- bfi(Lambda = Lambda, family = 'survival', theta_A_polys = theta_A_hats,
           basehaz = "poly", q_ls = qls)
summary(bfi, cur_mat=TRUE)

```

hazards.fun	<i>Compute the estimated (baseline/cumulative) hazard and (baseline) survival functions</i>
-------------	---

Description

For a given vector of times, `hazards.fun` computes the estimated baseline hazard, cumulative baseline hazard, hazard, baseline survival, and survival functions. It can be used for prediction on a new sample.

Usage

```

hazards.fun(time,
            z = NULL,
            p,
            theta_hat,
            basehaz = c("weibul", "exp", "gomp", "poly", "pwexp"),
            q_max,
            timax)

```

Arguments

time	the vector containing the time values for which the hazard rate is computed. If the argument <code>z</code> is not <code>NULL</code> , then the length of the argument <code>time</code> should be the number of columns of <code>z</code> , which is p .
z	a new observation vector of length p . If <code>z = NULL</code> (the default), then the relative risk ($z^T \beta$) is considered a vector of 1 with length n .
p	the number of coefficients. It is taken equal to the number of elements of the argument <code>z</code> , if <code>z</code> is not <code>NULL</code> .

theta_hat	a vector contains the values of the estimated parameters. The first p values represent the coefficient parameters (β), while the remaining values pertain to the parameters of the baseline hazard function (ω).
basehaz	a character string representing one of the available baseline hazard functions; exponential ("exp"), Weibull ("weibul", the default), Gompertz ("gomp"), exponentiated polynomial ("poly"), and piecewise exponential ("pwerp"). Can be abbreviated.
q_max	a value represents the order of the exponentiated polynomial baseline hazard function. This argument should only be used when basehaz = "poly". In the case of multiple centers, the maximum value of the orders should be used. <code>ql.LRT()</code> can be used for obtaining of the order of each center.
timax	a value represents the minimum (or maximum) value of the maximum times observed in the different centers. This argument should only be used when basehaz = "pwerp".

Details

`hazards.fun` computes the estimated baseline hazard, cumulative baseline hazard, hazard, baseline survival, and survival functions at different time points specified in the argument `time`.

The function `hazards.fun()` can be used for prediction purposes with new sample. The arguments `time` and `z` should be provided for the new data.

Value

`hazards.fun` returns a list containing the following components:

bhazard	the vector of estimates of the baseline hazard function at the time points given by the argument <code>time</code> ;
cbhazard	the vector of estimates of the cumulative baseline hazard function at the time points specified in the argument <code>time</code> ;
bsurvival	the vector of estimates of the baseline survival function at the time points given by the argument <code>time</code> ;
hazard	the vector of estimates of the hazard function at the time points given by the argument <code>time</code> ;
chazard	the vector of estimates of the cumulative hazard function at the time points specified in the argument <code>time</code> ;
survival	the vector of estimates of the survival function at the time points given by the argument <code>time</code> .

Author(s)

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References

Pazira H., Massa E., Weijers J.A.M., Coolen A.C.C. and Jonker M.A. (2024). *Bayesian Federated Inference for Survival Models*, *arXiv*. <<https://arxiv.org/abs/2404.17464>>

See Also[MAP.estimation](#)**Examples**

```

# Setting a seed for reproducibility
set.seed(1123)

##-----
## Simulating Survival data
##-----

n <- 40
p <- 7
Original_data <- data.frame(matrix(rnorm((n+1) * p), (n+1), p))
X <- Original_data[1:n,]
X_new <- Original_data[(n+1),]
# Simulating survival data from Exponential distribution
# with a predefined censoring rate of 0.2:
Orig_y <- surv.simulate(Z = Original_data, beta = rep(1,p), a = exp(1),
                        cen_rate = 0.2, gen_data_from = "exp")$D[[1]][,1:2]
y <- Orig_y[1:n,]
y_new <- Orig_y[(n+1),]
time_points <- seq(0, max(y$time), length.out=20)

#-----
# Weibull baseline hazard
#-----

Lambda <- inv.prior.cov(X, lambda = c(0.5, 1), family = 'survival', basehaz = 'weibul')
fit_weib <- MAP.estimation(y, X, family = 'survival', Lambda = Lambda,
                          basehaz = "weibul")

# relative risk is 1:
hazards.fun(time = time_points, p = p, theta_hat = fit_weib$theta_hat,
            basehaz = "weibul")

#-----
# Gompertz baseline hazard
#-----
fit_gomp <- MAP.estimation(y, X, family = 'survival', Lambda = Lambda,
                          basehaz = "gomp")

# different time points
hazards.fun(time=1:max(y*2), p = p, theta_hat = fit_gomp$theta_hat,
            basehaz = "gomp")

##-----
## Prediction for a new sample
##-----

## Exponentiated polynomial (poly) baseline hazard:
Lambda <- inv.prior.cov(X, lambda = c(0.5, 1), family = 'survival', basehaz = "poly")

```

```

fit_poly <- MAP. estimation(y, X, family = 'survival', Lambda = Lambda,
                        basehaz = "poly")
hazards.fun(time = y_new$time, z = X_new, theta_hat = fit_poly$theta_hat,
            basehaz = "poly", q_max = fit_poly$q_l)

## Piecewise Exponential (pwexp) baseline hazard:
Lambda <- inv.prior.cov(X, lambda = c(0.5, 1), family = 'survival', basehaz = "pwexp")
fit_pw <- MAP. estimation(y, X, family='survival', Lambda=Lambda, basehaz="pwexp",
                        min_max_times = max(y))
hazards.fun(time = y_new$time, z = X_new, theta_hat = fit_pw$theta_hat,
            basehaz = "pwexp", timax = max(y))

```

 inv.prior.cov

Creates an inverse covariance matrix for a Gaussian prior

Description

inv.prior.cov constructs a diagonal inverse covariance matrix for the Gaussian prior distribution based on the design matrix of covariates. This construction accounts for the number of regression parameters, especially when dealing with categorical covariates. For a linear model, it also includes an additional row and column to represent the variance of the measurement error. In the case of a survival model, it considers the parameters of the baseline hazard function as well.

Usage

```

inv.prior.cov(X,
             lambda = 1,
             L = 2,
             family = c("gaussian", "binomial", "survival"),
             intercept = TRUE,
             stratified = FALSE,
             strat_par = NULL,
             center_spec = NULL,
             basehaz = c("weibul", "exp", "gomp", "poly", "pwexp"),
             max_order = 2,
             n_intervals = 4)

```

Arguments

X	design matrix of dimension $n \times p$, where n is the number of samples observed, and p is the number of predictors/variables so excluding the intercept.
lambda	the vector used as the diagonal of the (inverse covariance) matrix that will be created by inv.prior.cov(). The length of the vector depends on the number of columns of X, type of the covariates (continuous/dichotomous or categorical), family, whether an intercept is included in the model, and whether stratified analysis is desired. When stratified = FALSE, lambda could be

	a single positive number (if all values in the vector are equal), a vector of two elements (the first is used for regression parameters including “intercept” and the second for the “sigma2” in the gaussian family or for the baseline hazard parameters in the survival case), or a vector of length equal to the number of model parameters. However, the length of lambda is different when stratified = TRUE, see ‘Details’ for more information. Default is lambda = 1.
L	the number of centers. This argument is used only when stratified = TRUE. Default is L = 2. See ‘Details’ and ‘Examples’.
family	a description of the error distribution. This is a character string naming a family of the model. In the current version of the package, the family of model can be “gaussian” (with identity link function), “binomial” (with logit link function), or “survival”. Can be abbreviated. By default the gaussian family is used. In case of a linear regression model, family = “gaussian”, there is an extra model parameter for the variance of measurement error. While in the case of survival model, family = “survival”, the number of the model parameters depend on the choice of baseline hazard functions, see ‘Details’ for more information.
intercept	logical flag for having an intercept. It does not used when family = “survival”. By changing the intercept the dimension of the inverse covariance matrix changes. If intercept = TRUE (the default), the output matrix created by inv.prior.cov() has one row and one column related to intercept, while if intercept = FALSE, the resulting matrix does not have the row and column called intercept.
stratified	logical flag for performing the stratified analysis. If stratified = TRUE, the parameter(s) selected in the strat_par argument are allowed to be different across centers. This argument should only be used when designing the inverse covariance matrix for the (fictive) combined data, i.e., the last matrix for the Lambda argument in bfi(). If inv.prior.cov() is used for the analysis in the local centers (to built the L first matrices for the Lambda argument in bfi()), this argument should be FALSE, even if the BFI analysis is stratified. It does not used when family = “survival”. Default is stratified = FALSE. See ‘Details’ and ‘Examples’.
strat_par	a one- or two-element integer vector for indicating the stratification parameter(s). The values 1 and/or 2 are/is used to indicate that the “intercept” and/or “sigma2” are allowed to vary, respectively. This argument is used only when stratified = TRUE. Default is strat_par = NULL, but if stratified = TRUE, strat_par can not be NULL. For the binomial family the length of the vector should be one which refers to “intercept”, and the value of this element should be 1. For gaussian this vector can be 1 for indicating the “intercept” only, 2 for indicating the “sigma2” only, and c(1, 2) for both “intercept” and “sigma2”. See ‘Examples’.
center_spec	a vector of L elements for representing the center specific variable. This argument is used only when stratified = TRUE and strat_par = NULL. Each element represents a specific feature of the corresponding center. There must be only one specific value or attribute for each center. This vector could be a numeric, characteristic or factor vector. Note that, the order of the centers in the vector center_spec must be the same as in the list of the argument theta_hats

	in the function <code>bfi()</code> . The used data type in the argument <code>center_spec</code> must be categorical. Default is <code>center_spec = NULL</code> . See also ‘Details’ and ‘Examples’.
<code>basehaz</code>	a character string representing one of the available baseline hazard functions; exponential (<code>"exp"</code>), Weibull (<code>"weibull"</code> , the default), Gompertz (<code>"gomp"</code>), exponentiated polynomial (<code>"poly"</code>), and piecewise constant exponential (<code>"pwexp"</code>). Can be abbreviated. It is only used when <code>family = "survival"</code> .
<code>max_order</code>	an integer representing the maximum value of <code>q_l</code> , which is the order/degree minus 1 of the exponentiated polynomial baseline hazard function. This argument is only used when <code>family = "survival"</code> and <code>basehaz = "poly"</code> . Default is 2.
<code>n_intervals</code>	an integer representing the number of intervals in the piecewise exponential baseline hazard function. This argument is only used when <code>family = "survival"</code> and <code>basehaz = "pwexp"</code> . Default is 4.

Details

`inv.prior.cov` creates a diagonal matrix with the vector `lambda` as its diagonal. The argument `stratified = TRUE` should only be used to construct a matrix for the prior density in case of stratification in the fictive combined data. Never be used for the construction of the matrix for analysis in the centers.

When `stratified = FALSE`, the length of the vector `lambda` depends on the covariate matrix `X`, `family`, `basehaz`, and whether an “intercept” is included in the model. For example, if the design matrix `X` has p columns with continuous or dichotomous covariates, `family = gaussian`, and `intercept = TRUE`, then `lambda` should have $p+2$ elements. In this case, if in `X` there is a categorical covariate with $q > 2$ categories, then the length of `lambda` increases with $q - 2$.

All values of `lambda` should be non-negative as they represent the inverse of the variance of the Gaussian prior. This argument is considered as the inverse of the variance of the prior distribution for: (β_0, β) if `family = "binomial"` and `intercept = TRUE`; $(\beta_0, \beta, \sigma^2)$ if `family = "gaussian"` and `intercept = TRUE`; and (β, ω) if `family = "survival"`.

If all values in the vector `lambda` equal, one value is enough to be given as entry. If `lambda` is a scalar, the function `inv.prior.cov` sets each value at the diagonal equal to `lambda`. When `lambda` is two dimensional: if `family = "binomial"`, the first and second values are used for the inverse of the variance of the prior distribution for the intercept (β_0) and regression parameters (β) , respectively; If `family = "gaussian"`, the first and second values are used for the inverse of the variance of the prior distribution for the regression parameters including the intercept (β_0, β) and variance of the measurement error (σ^2) , respectively; If `family = "survival"`, the first and second values are used for the inverse of the variance of the prior distribution for the regression parameters (β) and baseline hazard parameters (ω) , respectively.

If `stratified = TRUE` the length of the vector `lambda` should be equal to the number of parameters in the combined model.

If `intercept = FALSE`, for the binomial family the stratified analysis is not possible therefore `stratified` can not be `TRUE`.

If `stratified = FALSE`, both `strat_par` and `center_spec` must be `NULL` (the defaults), while if `stratified = TRUE` only one of the two must be `NULL`.

The output of `inv.prior.cov()` can be used in the main functions `MAP.estimation()` and `bfi()`.

Value

inv.prior.cov returns a diagonal matrix. The dimension of the matrix depends on the number of columns of X, type of the covariates (continuous/dichotomous or categorical), intercept, family, and basehaz.

Author(s)

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References

- Jonker M.A., Pazira H. and Coolen A.C.C. (2024). *Bayesian federated inference for estimating statistical models based on non-shared multicenter data sets*, *Statistics in Medicine*, 43(12): 2421-2438. <<https://doi.org/10.1002/sim.10072>>
- Pazira H., Massa E., Weijers J.A.M., Coolen A.C.C. and Jonker M.A. (2024). *Bayesian Federated Inference for Survival Models*, *arXiv*. <<https://arxiv.org/abs/2404.17464>>
- Jonker M.A., Pazira H. and Coolen A.C.C. (2024b). *Bayesian Federated Inference for regression models with heterogeneous multi-center populations*, *arXiv*. <<https://arxiv.org/abs/2402.02898>>

See Also

[MAP.estimation](#)

Examples

```
#-----
# Data Simulation
#-----
X <- data.frame(x1=rnorm(50),                # standard normal variable
               x2=sample(0:2, 50, replace=TRUE), # categorical variable
               x3=sample(0:1, 50, replace=TRUE)) # dichotomous variable
X$x2 <- as.factor(X$x2)
X$x3 <- as.factor(X$x3)

# The (inverse) variance value (lambda=0.05) is assumed to be
# the same for Gaussian prior of all parameters (for non-stratified)

#-----
# Inverse Covariance Matrix for the Gaussian prior
#-----
# y ~ Binomial with 'intercept'
inv.prior.cov(X, lambda = 0.05, family = 'binomial')
# returns a 5-by-5 matrix

# y ~ Binomial without 'intercept'
inv.prior.cov(X, lambda = 0.05, family = "binomial", intercept = FALSE)
# a 4-by-4 matrix

# y ~ Gaussian with 'intercept'
```

```

inv.prior.cov(X, lambda = 0.05, family = 'gaussian')
# returns a 6-by-6 matrix

# Survival family with 'weibul' baseline hazard
inv.prior.cov(X, lambda = c(0.05, 0.1), family = 'survival')
# returns a 6-by-6 matrix

# Survival family with 'pwexp' baseline hazard (4 intervals)
inv.prior.cov(X, lambda = 0.05, family = 'survival', basehaz = "pwexp")
# returns a 8-by-8 matrix

# Survival family with 'poly' baseline hazard
inv.prior.cov(X, lambda = c(0.05, 0.1), family = 'survival', basehaz = "poly")
# returns a 7-by-7 matrix

#-----
# Stratified analysis
#-----
# y ~ Binomial when 'intercept' varies across 3 centers:
inv.prior.cov(X, lambda = c(.2, 1), family = 'binomial', stratified = TRUE,
              strat_par = 1, L = 3)

# y ~ Gaussian when 'intercept' and 'sigma2' vary across 2 centers; y ~ Gaussian
inv.prior.cov(X, lambda = c(1, 2, 3), family = "gaussian", stratified = TRUE,
              strat_par = c(1, 2))

# y ~ Gaussian when 'sigma2' varies across 2 centers (with 'intercept')
inv.prior.cov(X, lambda = c(1, 2, 3), family='gaussian', stratified = TRUE,
              strat_par = 2)

# y ~ Gaussian when 'sigma2' varies across 2 centers (without 'intercept')
inv.prior.cov(X, lambda = c(2, 3), family = "gaussian", intercept = FALSE,
              stratified=TRUE, strat_par = 2)

#-----
# Center specific covariate
#-----
# center specific covariate has K = 2 categories across 4 centers; y ~ Binomial
inv.prior.cov(X, lambda = c(0.1:2), family = 'binomial', stratified = TRUE,
              center_spec = c("Iran", "Netherlands", "Netherlands", "Iran"), L=4)

# center specific covariate has K = 3 categories across 5 centers; y ~ Gaussian
inv.prior.cov(X, lambda = c(0.5:3), family = 'gaussian', stratified = TRUE,
              center_spec = c("Medium", "Big", "Small", "Big", "Small"), L = 5)

# center specific covariate has K = 4 categories across 5 centers; y ~ Gaussian
inv.prior.cov(X, lambda = 1, family = 'gaussian', stratified = TRUE,
              center_spec = c(3,1:4), L=5)

```

Description

MAP. estimation function is used (in local centers) to compute Maximum A Posterior (MAP) estimators of the parameters for Generalized Linear Models (GLM) and Survival models.

Usage

```
MAP. estimation(y,
               X,
               family = c("gaussian", "binomial", "survival"),
               Lambda,
               intercept = TRUE,
               initial = NULL,
               basehaz = c("weibul", "exp", "gomp", "poly", "pwexp"),
               alpha = 0.1,
               max_order = 2,
               n_intervals = 4,
               min_max_times,
               center_zero_sample = FALSE,
               zero_sample_cov,
               refer_cat,
               zero_cat,
               control = list())
```

Arguments

- | | |
|--------|---|
| y | response vector. If the "binomial" family is used, this argument is a vector with entries 0 (failure) or 1 (success). Alternatively, for this family, the response can be a matrix where the first column is the number of "successes" and the second column is the number of "failures". For the "survival" family, the response is a matrix where the first column is the survival time, named "time", and the second column is the censoring indicator, named "status", with 0 indicating censoring time and 1 indicating event time. |
| X | design matrix of dimension $n \times p$, where p is the number of covariates or predictors. Note that the order of the covariates must be the same across the centers; otherwise, the output estimates of bfi() will be incorrect. |
| family | a description of the error distribution. This is a character string naming a family of the model. In the current version of the package, the family of model can be "gaussian" (with identity link function), "binomial" (with logit link function), or "survival". Can be abbreviated. By default the gaussian family is used. In case of a linear regression model, family = "gaussian", there is an extra model parameter for the variance of measurement error. While in the case of survival model, family = "survival", the number of the model parameters depend on the choice of baseline hazard functions, see 'Details' for more information. |
| Lambda | the inverse variance-covariance matrix of the Gaussian distribution that is used as prior distribution for the model parameters. The dimension of the matrix depends on the number of columns of X, type of the covariates (continuous / |

dichotomous or categorical), family, and whether an intercept is included (if applicable). However, Lambda can be easily created by `inv.prior.cov()`. See [inv.prior.cov](#) for more information.

intercept	logical flag for fitting an intercept. If <code>intercept=TRUE</code> (the default), the intercept is fitted, i.e., it is included in the model, and if <code>intercept=FALSE</code> it is set to zero, i.e., it's not in the model. This argument is not used if <code>family = "survival"</code> .
initial	a vector specifying initial values for the parameters to be optimized over. The length of <code>initial</code> is equal to the number of model parameters and thus, is equal to the number of rows or columns of Lambda. Since the 'L-BFGS-B' method is used in the algorithm, these values should always be finite. Default is a vector of zeros, except for the survival family with the poly function, where it is a vector with the first p elements as zeros for coefficients (β) and -0.5 for the remaining parameters (ω). For the gaussian family, the last element of the <code>initial</code> vector could also be considered negative, because the Gaussian prior was applied to $\log(\sigma^2)$.
basehaz	a character string representing one of the available baseline hazard functions; exponential ("exp"), Weibull ("weibul", the default), Gompertz ("gomp"), exponentiated polynomial ("poly"), and piecewise constant exponential ("pwexp"). Can be abbreviated. It is only used when <code>family = "survival"</code> . If local sample size is large and the shape of the baseline hazard function is completely unknown, the "exponentiated polynomial" and "piecewise exponential" hazard functions would be preferred above the lower dimensional alternatives. However, if the local samples size is low, one should be careful using the "piecewise exponential" hazard function with many intervals.
alpha	a significance level used in the chi-squared distribution (with one degree of freedom and $1-\alpha$ representing the upper quantile) to conduct a likelihood ratio test for obtaining the order of the exponentiated polynomial baseline hazard function. It is only used when <code>family = "survival"</code> and <code>basehaz = "poly"</code> . Default is 0.1. See 'Details'.
max_order	an integer representing the maximum value of <code>q_1</code> , which is the order/degree minus 1 of the exponentiated polynomial baseline hazard function. This argument is only used when <code>family = "survival"</code> and <code>basehaz = "poly"</code> . Default is 2.
n_intervals	an integer representing the number of intervals in the piecewise exponential baseline hazard function. This argument is only used when <code>family = "survival"</code> and <code>basehaz = "pwexp"</code> . Default is 4.
min_max_times	a scalar representing the minimum of the maximum event times observed in the centers. The value of this argument should be defined by the central server (which has access to the maximum event times of all the centers) and is only used when <code>family = "survival"</code> and <code>basehaz = "pwexp"</code> .
center_zero_sample	logical flag indicating whether the center has a categorical covariate with no observations/individuals in one of the categories. Default is <code>center_zero_sample = FALSE</code> .

zero_sample_cov	either a character string or an integer representing the categorical covariate that has no samples/observations in one of its categories. This covariate should have at least two categories, one of which is the reference. It is used when center_zero_sample = TRUE.
refer_cat	a character string representing the reference category. The category with no observations (the argument zero_cat) cannot be used as the reference in the argument refer_cat. It is used when center_zero_sample = TRUE.
zero_cat	a character string representing the category with no samples/observations. It is used when center_zero_sample = TRUE.
control	a list of control parameters. See ‘Details’.

Details

MAP. estimation function finds the Maximum A Posteriori (MAP) estimates of the model parameters by maximizing the log-posterior density with respect to the parameters, i.e., the estimates equal the values for which the log-posterior density is maximal (the posterior mode). In other words, MAP. estimation() optimizes the log-posterior density with respect to the parameter vector to obtain its MAP estimates. In addition to the model parameters (i.e., coefficients (β) and variance error (σ_e^2) for gaussian or the parameters of the baseline hazard (ω) for survival), the curvature matrix (Hessian of the log-posterior) is estimated around the mode.

The MAP. estimation function returns an object of class ‘bfi’. Therefore, summary() can be used for the object returned by MAP. estimation().

For the case where family = “survival” and basehaz = “poly”, we assume that in all centers the q_ℓ ’s are equal. However, the order of the estimated polynomials may vary across the centers so that each center can have different number of parameters, say $q_\ell+1$. After obtaining the estimates within the local centers (by using MAP. estimation()) and having all estimates in the central server, we choose the order of the polynomial approximation for the combined data to be the maximum of the orders of the local polynomial functions, i.e., $\max\{q_1, \dots, q_L\}$, to approximate the global baseline hazard (exponentiated polynomial) function more accurately. This is because the higher-order polynomial approximation can capture more complex features and details in the combined data. Using the higher-order approximation ensures that we account for the higher-order moments and features present in the data while maintaining accuracy. As a result, all potential cases are stored in the theta_A_poly argument to be used in bfi() by the central server. For further information on the survival family, refer to the ‘References’ section.

To solve unconstrained and bound-constrained optimization problems, the MAP. estimation function utilizes an optimization algorithm called Limited-memory Broyden-Fletcher-Goldfarb-Shanno with Bound Constraints (L-BFGS-B), Byrd et. al. (1995). The L-BFGS-B algorithm is a limited-memory “quasi-Newton” method that iteratively updates the parameter estimates by approximating the inverse Hessian matrix using gradient information from the history of previous iterations. This approach allows the algorithm to approximate the curvature of the posterior distribution and efficiently search for the optimal solution, which makes it computationally efficient for problems with a large number of variables.

By default, the algorithm uses a relative change in the objective function as the convergence criterion. When the change in the objective function between iterations falls below a certain threshold (‘factr’) the algorithm is considered to have converged. The convergence can be checked with the argument convergence in the output. See ‘Value’.

In case of convergence issue, it may be necessary to investigate and adjust optimization parameters to facilitate convergence. It can be done using the `initial` and `control` arguments. By the argument `initial` the initial points of the iterative optimization algorithm can be changed, and the argument `control` is a list that can supply any of the following components:

- `maxit`: is the maximum number of iterations. Default is 150;
- `factr`: controls the convergence of the 'L-BFGS-B' method. Convergence occurs when the reduction in the objective is within this factor of the machine tolerance. Default for `factr` is $1e7$, which gives a tolerance of about $1e-9$. The exact tolerance can be checked by multiplying this value by `.Machine$double.eps`;
- `pgtol`: helps to control the convergence of the 'L-BFGS-B' method. It is a tolerance on the projected gradient in the current search direction, i.e., the iteration will stop when the maximum component of the projected gradient is less than or equal to `pgtol`, where `pgtol` ≥ 0 . Default is zero, when the check is suppressed;
- `trace`: is a non-negative integer. If positive, tracing information on the progress of the optimization is produced. Higher values may produce more tracing information: for the method 'L-BFGS-B' there are six levels of tracing. To understand exactly what these do see the source code of `optim` function in the [stats](#) package;
- `REPORT`: is the frequency of reports for the 'L-BFGS-B' method if '`control$trace`' is positive. Default is every 10 iterations;
- `lmm`: is an integer giving the number of BFGS updates retained in the 'L-BFGS-B' method. Default is 5.

Value

`MAP. estimation` returns a list containing the following components:

- | | |
|------------------------|--|
| <code>theta_hat</code> | the vector corresponding to the maximum a posteriori (MAP) estimates of the parameters. For the gaussian family, the last element of this vector is σ^2 ; |
| <code>A_hat</code> | minus the curvature (or Hessian) matrix around the point <code>theta_hat</code> . The dimension of the matrix is the same as the argument <code>Lambda</code> ; |
| <code>sd</code> | the vector of standard deviation of the MAP estimates in <code>theta_hat</code> , that is <code>sqrt(diag(solve(A_hat)))</code> ; |
| <code>Lambda</code> | the inverse variance-covariance matrix of the Gaussian distribution that is used as prior distribution for the parameters. It's exactly the same as the argument <code>Lambda</code> ; |
| <code>formula</code> | the formula applied; |
| <code>names</code> | the names of the model parameters; |
| <code>n</code> | sample size; |
| <code>np</code> | the number of coefficients; |
| <code>q_1</code> | the order/degree minus 1 of the exponentiated polynomial baseline hazard function determined for the current center by the likelihood ratio test. This output argument, <code>q_1</code> , is only shown when <code>family = "survival"</code> and <code>basehaz = "poly"</code> , and will be used in the function <code>bfi()</code> ; |

theta_A_poly	an array where the first component is a matrix with columns representing the MAP estimates of the parameters for different q_l 's, i.e., $q_l, q_{l+1}, \dots, \text{max_order}$. The other components are minus the curvature matrices for different q_l 's, i.e., $q_l, q_{l+1}, \dots, \text{max_order}$. Therefore, the first non-NA curvature matrix is equal to the output argument A_hat. This output argument, theta_A_poly, is only shown if family = "survival" and basehaz = "poly", and will be used in the function bfi();
lev_no_ref_zer	a vector containing the names of the levels of the categorical covariate that has no samples/observations in one of its categories. The name of the category with no samples and the name of the reference category are excluded from this vector. This argument is shown when family = "survival" and basehaz = "poly", and will be used in the function bfi();
zero_sample_cov	the categorical covariate that has no samples/observations in one of its categories. It is shown when center_zero_sample = TRUE, and can be used in the function bfi();
refer_cat	the reference category. It is shown when center_zero_sample = TRUE, and can be used in the function bfi();
zero_cat	the category with no samples/observations. It is shown when center_zero_sample = TRUE, and can be used in the function bfi();
value	the value of minus the log-likelihood posterior density evaluated at theta_hat;
family	the family used;
basehaz	the baseline hazard function used;
intercept	logical flag used to fit an intercept if TRUE, or set to zero if FALSE;
convergence	an integer value used to encode the warnings and the errors related to the algorithm used to fit the model. The values returned are: <ul style="list-style-type: none"> 0 algorithm has converged; 1 maximum number of iterations ('maxit') has been reached; 2 Warning from the 'L-BFGS-B' method. See the message after this value;
control	the list of control parameters used to compute the MAP estimates.

Author(s)

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References

Jonker M.A., Pazira H. and Coolen A.C.C. (2024). *Bayesian federated inference for estimating statistical models based on non-shared multicenter data sets*, *Statistics in Medicine*, 43(12): 2421-2438. <<https://doi.org/10.1002/sim.10072>>

Pazira H., Massa E., Weijers J.A.M., Coolen A.C.C. and Jonker M.A. (2024). *Bayesian Federated Inference for Survival Models*, *arXiv*. <<https://arxiv.org/abs/2404.17464>>

Jonker M.A., Pazira H. and Coolen A.C.C. (2024b). *Bayesian Federated Inference for regression models with heterogeneous multi-center populations*, *arXiv*. <<https://arxiv.org/abs/2402.02898>>

Byrd R.H., Lu P., Nocedal J. and Zhu C. (1995). *A limited memory algorithm for bound constrained optimization*. SIAM Journal on Scientific Computing, 16, 1190-1208. <<https://doi.org/10.1137/0916069>>

See Also

[bfi](#), [inv.prior.cov](#) and [summary.bfi](#)

Examples

```
###-----###
### y ~ Gaussian ###
###-----###

# Setting a seed for reproducibility
set.seed(11235)

# model parameters: coefficients and sigma2 = 1.5
theta <- c(1, 2, 2, 2, 1.5)

#-----
# Data Simulation
#-----
n <- 30 # sample size
p <- 3 # number of coefficients without intercept
X <- data.frame(matrix(rnorm(n * p), n, p)) # continuous variables
# linear predictor:
eta <- theta[1] + theta[2] * X$X1 + theta[3] * X$X2 + theta[4] * X$X3
# inverse of the link function (  $g^{-1}(\eta) = \mu$  ):
mu <- gaussian()$linkinv(eta)
y <- rnorm(n, mu, sd = sqrt(theta[5]))

# Load the BFI package
library(BFI)

#-----
# MAP estimations for theta and curvature matrix
#-----
# MAP estimates with 'intercept'
Lambda <- inv.prior.cov(X, lambda = c(0.1, 1), family = "gaussian")
(fit <- MAP. estimation(y, X, family = "gaussian", Lambda))
class(fit)
summary(fit, cur_mat = TRUE)

# MAP estimates without 'intercept'
Lambda <- inv.prior.cov(X, lambda = c(0.1, 1), family = 'gaussian', intercept = FALSE)
(fit1 <- MAP. estimation(y, X, family = 'gaussian', Lambda, intercept = FALSE))
summary(fit1, cur_mat = TRUE)

###-----###
### Survival family ###
###-----###
```

```

# Setting a seed for reproducibility
set.seed(112358)

#-----
# Simulating Survival data
#-----
n <- 40
beta <- 1:4
p <- length(beta)
X <- data.frame(matrix(rnorm(n * p), n, p)) # continuous (normal) variables

## Simulating survival data from Weibull with a predefined censoring rate of 0.3
y <- surv.simulate(Z = list(X), beta = beta, a = 5, b = exp(1.8), u1 = 0.1,
                  cen_rate = 0.3, gen_data_from = "weibul")$D[[1]][, 1:2]

##
## MAP estimations with "weibul" function
##
Lambda <- inv.prior.cov(X, lambda = c(0.1, 1), family = 'survival', basehaz = "weibul")
fit2 <- MAP. estimation(y, X, family = 'survival', Lambda = Lambda, basehaz = "weibul")
fit2
fit2$theta_hat

##
## MAP estimations with "poly" function
##
Lambda <- inv.prior.cov(X, lambda = c(0.1, 1), family = 'survival', basehaz = 'poly')
fit3 <- MAP. estimation(y, X, family = "survival", Lambda = Lambda, basehaz = "poly")
# Degree of the exponentiated polynomial baseline hazard
fit3$q_l + 1
# theta_hat for (beta_1, ..., beta_p, omega_0, ..., omega_{q_l})
fit3$theta_A_poly[,1][,fit3$q_l+1] # equal to fit3$theta_hat
# A_hat
fit3$theta_A_poly[, ,fit3$q_l+2] # equal to fit3$A_hat
summary(fit3, cur_mat = TRUE)

##
## MAP estimations with "pwexp" function with 3 intervals
##
# Assume we have 4 centers
Lambda <- inv.prior.cov(X, lambda = c(0.1, 1), family = 'survival',
                      basehaz = 'pwexp', n_intervals = 3)
# For this baseline hazard ("pwexp"), we need to know
# maximum survival times of the 3 other centers:
max_times <- c(max(rexp(30)), max(rexp(50)), max(rexp(70)))
# Minimum of the maximum values of the survival times of all 4 centers is:
min_max_times <- min(max(y$time), max_times)
fit4 <- MAP. estimation(y, X, family = "survival", Lambda = Lambda, basehaz = "pwexp",
                      n_intervals = 3, min_max_times=max(y$time))
summary(fit4, cur_mat = TRUE)

```

n.par

The Number of Predictors, Coefficients, and Observations

Description

n.par returns the number of regression parameters, covariates and observations present in X based on the selected family.

Usage

```
n.par(X, family = c("gaussian", "binomial", "survival"))
```

Arguments

X	design matrix of dimension $n \times p$, where n is the number of samples observed, and p is the number of predictors/covariables. It could be a matrix or a list of matrices.
family	a description of the error distribution used to specify the model. This should be a character string, either "gaussian", "binomial", or "survival". Can be abbreviated. By default the gaussian family is used.

Details

orig.names and covar.names are the same if the all covariates in X are continuous. However, if there are at least one categorical variable in X with more than two categories, they are different.

Value

n.par returns a list containing the following components:

n.reg.par	the number of regression parameters;
n.covar	the number of covariates;
n.sample	the number of samples/observations;
orig.names	the original names of the variables (without including the names of dummy variables);
covar.names	the names of the variables (together with the names of any dummy variables, if applicable).

Author(s)

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Examples

```

#-----
# family = "gaussian"
#-----

X0 <- data.frame(x1 = rnorm(50),                # standard normal variable
                x2 = sample(0:2, 50, replace=TRUE), # categorical variable
                x3 = sample(0:1, 50, replace=TRUE)) # dichotomous variable
n.par(X0) # without dummy variables
X0$x2 <- as.factor(X0$x2)
X0$x3 <- as.factor(X0$x3)
n.par(X0) # with dummy variables

X1 <- data.frame(Intercept = rep(1,30),
                x1 = rnorm(30),                # continuous variable
                x2 = sample(0:2, 30, replace=TRUE)) # categorical variable
n.par(X1) # without dummy variables
X1$x2 <- as.factor(X1$x2)
n.par(X1) # without dummy variables

# a list of two data sets:
X01 <- list(X0, X1)
n.par(X01)

```

Nurses

Nurses' stress in different hospitals

Description

This dataset comprises three-level simulated data extracted for a hypothetical study investigating stress levels within hospital settings. The dataset focuses on nurses working in specific wards within various hospitals. It includes several variables, such as nurse age (measured in years), nurse experience (measured in years), nurse gender (0 for male, 1 for female), ward type (0 for general care, 1 for special care), and hospital size (0 for small, 1 for medium, 2 for large). The dataset in the package is obtained from the original dataset by leaving out some of the unused columns.

Usage

```
data(Nurses)
```

Source

<https://multilevel-analysis.sites.uu.nl/datasets/>

References

Hox, J., Moerbeek, M., and van de Schoot, R. (2010). *Multilevel Analysis: Techniques and Applications*, Second Edition (2nd ed.). Routledge. <<https://doi.org/10.4324/9780203852279>>

summary.bfi

*Summarizing BFI Fits***Description**

Summary method for an object with class 'bfi' created by the `MAP.estimate` and `bfi` functions.

Usage

```
## S3 method for class 'bfi'
summary(object,
        cur_mat = FALSE,
        digits = max(3, getOption("digits") - 3),
        ...)
```

Arguments

<code>object</code>	fitted bfi object.
<code>cur_mat</code>	logical; if TRUE, minus the curvature matrix around the estimated parameters is returned and printed. Default is FALSE.
<code>digits</code>	significant digits in printout.
<code>...</code>	additional arguments affecting the summary produced.

Details

`summary.bfi()` gives information about the MAP estimates of parameters of the model. It can be used for the bfi objects built by the `MAP.estimate` and `bfi` functions.

The output of the summary method shows the details of the model, i.e. formula, family and link function used to specify the generalized linear model, followed by information about the estimates, standard deviations and credible intervals. Information about the log-likelihood posterior and convergence status are also provided.

By default, `summary.bfi` function does not return (minus) the curvature matrix, but the user can use `cur_mat = TRUE` to print it.

Value

`summary.bfi` returns an object of class `summary.bfi`, a list with the following components:

<code>theta_hat</code>	the component from <code>object</code> . The last element of this vector is the estimate of the dispersion parameter (<code>sigma2</code>) if <code>family = "gaussian"</code> . See the MAP.estimate and bfi functions.
<code>A_hat</code>	the component from <code>object</code> . See the MAP.estimate and bfi functions.
<code>sd</code>	the component from <code>object</code> . If <code>family = "gaussian"</code> , the last element of this vector is the square root of the estimated dispersion. See the MAP.estimate and bfi functions.

Lambda	the component from object. See the MAP.estimate function.
formula	the component from object. See the MAP.estimate function.
n	the component from object. See the MAP.estimate function.
np	the component from object. See the MAP.estimate function.
family	the component from object. See the MAP.estimate function.
intercept	the component from object. See the MAP.estimate function.
convergence	the component from object. See the MAP.estimate function.
control	the component from object. See the MAP.estimate function.
stratified	the component from object. See the bfi function.
estimate	the estimated regression coefficients, i.e., without the estimate sigma2.
logLikPost	the value of the log-likelihood posterior density evaluated at estimates (theta_hat).
link	the link function only for GLMs, not for the survival family. By default the gaussian family with identity link function and the binomial family with logit link function are used.
dispersion	the estimated variance of the random error, i.e., sigma2. The dispersion is taken as 1 for the binomial family.
CI	a 95% credible interval of the MAP estimates of the parameters.

Author(s)

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See Also

[MAP.estimate](#) and [bfi](#)

Examples

```
#-----
# y ~ Gaussian
#-----
# model assumption:
theta <- c(1, 2, 3, 4, 1.5) # coefficients and sigma2 = 1.5

#-----
# Data Simulation
#-----
n      <- 40
X      <- data.frame(x1=rnorm(n),                # continuous variable
                    x2=sample(1:3, n, replace=TRUE)) # categorical variable
Xx2_1  <- ifelse(X$x2 == '2', 1, 0)
Xx2_2  <- ifelse(X$x2 == '3', 1, 0)
X$x2   <- as.factor(X$x2)
eta    <- theta[1] + theta[2] * X$x1 + theta[3] * Xx2_1 + theta[4] * Xx2_2
mu     <- gaussian()$linkinv(eta)
y      <- rnorm(n, mu, sd = sqrt(theta[5]))
```

```

#-----
# MAP estimations
#-----
Lambda <- inv.prior.cov(X, lambda = c(0.1, 0.5), family = "gaussian")
fit <- MAP.estimate(y, X, family = "gaussian", Lambda)
class(fit)

#-----
# Summary of MAP estimates
#-----
summary(fit)
sumfit <- summary(fit, cur_mat = TRUE)
sumfit$estimate
sumfit$logLikPost
sumfit$dispersion
sumfit$CI
class(sumfit)

```

surv.simulate	<i>Generate survival data with predefined censoring rates for proportional hazards models</i>
---------------	---

Description

surv.simulate simulates one or multiple (right-censored) survival datasets for proportional hazards models by simultaneously incorporating a baseline hazard function from three different survival distributions (exponential, Weibull and Gompertz), a random censoring time generated from a uniform distribution with an known/unknown upper limit, and a set of baseline covariates. When the upper limit of the uniform censoring time distribution is unknown, surv.simulate can be used separately to obtain the upper limit with a predefined censoring rate.

Usage

```

surv.simulate(L = 1, Z, beta, a, b, u1 = 0, u2, cen_rate,
             gen_data_from = c("exp", "weibul", "gomp"),
             only_u2 = FALSE, n.rep = 100, Trace = FALSE)

```

Arguments

L	the number of datasets to be generated. Default is L = 1.
Z	a list of L design matrices of dimension $n_\ell \times p$, where n_ℓ is the number of samples observed for the ℓ^{th} dataset and p is the number of covariables. When L = 1, Z can be a matrix.
beta	the vector of the (true) coefficients values, with a length of p (the number of covariates).

a	scale parameter, which should be non-negative. See ‘Details’ for the form of the cumulative hazard that can be used.
b	shape/location parameter, which should be non-negative. It is not used when <code>gen_data_from = “exp”</code> . See ‘Details’ for the form of the cumulative hazard that can be used.
u1	a known non-negative lower limit of the uniform distribution for generating random censoring time. Default is <code>u1 = 0</code> . If <code>cen_rate</code> is not equal to 0, then <code>u1</code> does not need to be defined.
u2	an non-negative upper limit of the uniform random censoring time distribution. The upper limit can be unknown (<code>u2 = NULL</code> , the default), or predefined. When this argument is assumed to be unknown, <code>u2 = NULL</code> , it is calculated by the algorithm within <code>surv.simulate()</code> . However, if the argument <code>u2</code> is known, the censoring rate cannot be predefined (meaning there is no control over it) and is calculated based on the generated dataset. See ‘Details’ and ‘References’.
cen_rate	a value representing the proportion of observations in the simulated survival data that are censored. The range of this argument is from 0 to 1. When the upper limit is known, <code>cen_rate</code> can nor be predefined. If there is no censoring (<code>cen_rate = 0</code>), the lower (<code>u1</code>) and upper (<code>u2</code>) limits of the uniform distribution do not need to be specified.
gen_data_from	a description of the distribution from which the time to event is generated. This is a character string and can be <code>exponential (“exp”)</code> , <code>Weibull (“weibul”)</code> , or <code>Gompertz (“gomp”)</code> . Can be abbreviated. By default, the exponential distribution is used.
only_u2	logical flag for calculating only the upper limit of the uniform censoring time distribution. If <code>only_u2 = TRUE</code> , the dataset(s) are not generated. If <code>only_u2 = TRUE</code> , the arguments <code>Z</code> and <code>u2</code> do not need to be specified, and <code>cen_rate</code> should not be set to 0. Default is <code>only_u2 = FALSE</code> .
n.rep	a scalar specifying the number of iterations. This argument is exclusively used in the case of the Gompertz distribution. Default is 100.
Trace	logical flag indicating whether the output of the desired <code>u2</code> and the censoring proportion for different datasets should be produced for each iteration. It works <code>gen_data_from = “gomp”</code> .

Details

`surv.simulate` function generates L simulated right-censored survival datasets from exponential, Weibull, or Gompertz distributions, incorporating the covariates, Z , distributed according to a multivariate normal distribution, with censoring time generated from a uniform distribution `Uniform(u1, u2)`, where `u1` is known but `u2` can be either known or unknown.

`surv.simulate()` can also be used to calculate the unknown upper limit of the uniform distribution, `u2`, with a predefined censoring rate. To do this, set `u2 = NULL` and `only_u2 = TRUE`. In this case, the datasets are not generated; only `u2` is.

`surv.simulate()` uses a root-finding algorithm to select the censoring parameter that achieves predefined censoring rates in the simulated survival data.

When `gen_data_from = “exp”`:

- the cumulative baseline hazard function is considered as $\Lambda_0 = at$,
- the event time for the ℓ^{th} dataset, T_ℓ , is computed by $-\log(u) \exp(-Z_\ell \boldsymbol{\beta})/a$, where u follows a standard uniform distribution;

For `gen_data_from = "weibul"`:

- the cumulative hazard function is as $\Lambda_0 = at^b$,
- the event time is computed by $T_\ell = (-\log(u) \exp(-Z_\ell \boldsymbol{\beta})/a)^{1/b}$, where u follows a standard uniform distribution;

For `gen_data_from = "gomp"`:

- the cumulative hazard function is as $\Lambda_0 = a(\exp(bt) - 1)/b$,
- the event time is computed by $T_\ell = \log(1 - \log(u) \exp(-Z_\ell \boldsymbol{\beta})b/a)/b$, where u follows a standard uniform distribution;

Finally the survival time is obtained by $\tilde{T}_\ell = \min\{T_\ell, C_\ell\}$.

The function will be updated for `gen_data_from = "gomp"`.

Value

`surv.simulate` returns a list containing the following components:

D	a list of L data frames, with dimension $n_\ell \times (p + 2)$. The first and second columns, named <code>time</code> and <code>status</code> , contain the simulated survival time and the censoring indicator, respectively, where 0 means censored and 1 means uncensored;
<code>censor_propor</code>	the vector of censoring proportions in the simulated datasets D, containing L elements;
<code>u1</code>	the lower limit of the uniform distribution used to generate random censoring times with a predefined censoring rate. Sometimes this output is less than the value entered by the user, as it is adjusted to achieve the desired amount of censoring rate;
<code>u2</code>	the upper limit of the uniform distribution used to generate random censoring times. If <code>u2 = NULL</code> , this output will be the estimated upper limit necessary to achieve the desired censoring rate across the L datasets.

Author(s)

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References

Pazira H., Massa E., Weijers J.A.M., Coolen A.C.C. and Jonker M.A. (2024). *Bayesian Federated Inference for Survival Models*, *arXiv*. <<https://arxiv.org/abs/2404.17464>>

See Also

[MAP.estimation](#)

Examples

```

# Setting a seed for reproducibility
set.seed(1123)

#-----
# Simulating Survival data
#-----
N   <- c(7, 10, 13) # the sample sizes of 3 datasets
beta <- 1:4
p   <- length(beta)
L   <- 3

# Define a function to generate multivariate normal samples
mvrnorm_new <- function(n, mu, Sigma) {
  pp <- length(mu)
  e <- matrix(rnorm(n * pp), nrow = n)
  return(crossprod(t(e), chol(Sigma)) + matrix(mu, n, pp, byrow = TRUE))
}
Z <- list()
for (z in seq_len(L)) {
  Z[[z]] <- mvrnorm_new(n = N[z], mu = rep(0, p),
                       Sigma = diag(rep(1, p),p))
  colnames(Z[[z]]) <- paste0("Z_",seq_len(ncol(Z[[z]])))
}

# One simulated dataset from exponential distribution with no censoring:
surv_data <- surv.simulate(Z = Z[[1]], beta = beta, a = exp(-.9),
                          cen_rate = 0, gen_data_from = "exp")
surv_data
surv_data$D[[1]][,1:2] # The simulated survival data

# Calculate only 'u2' with a predefined censoring rate of 0.4:
u2_new <- surv.simulate(Z = Z[1:2], beta = beta, a = exp(-.9),
                      b = exp(1.8), u1 = 0.1, only_u2 = TRUE,
                      cen_rate = 0.4, gen_data_from = "weibul")$u2
u2_new

# Two simulated datasets with a known 'u2':
# Using 'u2_new' to help control over censoring rate (was chosen 0.4)
surv.simulate(Z = Z[1:2], beta = beta, a = exp(-.9), b = exp(1.8),
             u1 = 0.05, u2 = u2_new, gen_data_from = "weibul")

# Three simulated datasets from 'weibul' with an unknown 'u2':
surv.simulate(Z = Z, beta = beta, a = exp(-1), b = exp(1),
             u1 = 0.01, cen_rate = 0.3, gen_data_from = "weibul")

# Two simulated datasets from 'gomp' with unknown 'u2' and censoring rate of 0.3:
surv.simulate(Z = Z[2:3], beta = beta, a = exp(1), b = exp(2), u1 = 0.1,
             cen_rate = 0.3, gen_data_from = "gomp", Trace = TRUE)

```

trauma

Trauma patients from different hospitals

Description

This data set consists of data of 371 trauma patients from three hospitals. The binary variable mortality is used as an outcome, and variables age, sex, the Injury Severity Score (ISS, ranging from 1 (low) to 75 (high)) and the Glasgow Coma Scale (GCS, which expresses the level of consciousness, ranging from 3 (low) to 15 (high)) are used as covariates. There are three types of hospitals: peripheral hospital without a neuro-surgical unit (Status = 1), peripheral hospital with a neuro-surgical unit (Status = 2), and academic medical center (Status = 3). Originally, the data come from a multi center study collected with a different aim. For educational purposes minor changes have been made, see the references below.

Usage

data(trauma)

References

- Jonker M.A., Pazira H. and Coolen A.C.C. (2024). *Bayesian federated inference for estimating statistical models based on non-shared multicenter data sets*, *Statistics in Medicine*, 43(12): 2421-2438. <<https://doi.org/10.1002/sim.10072>>
- Draaisma J.M.Th, de Haan A.F.J., Goris R.J.A. (1989). *Preventable Trauma Deaths in the Netherlands - A prospective Multicentre Study*, *The journal of Trauma*, Vol. 29(11), 1552-1557.

Index

- * **array**
 - b.diag, 3
 - inv.prior.cov, 16
 - * **bayesian**
 - bfi, 4
 - MAP.estimation, 21
 - * **datagen**
 - surv.simulate, 32
 - * **datasets**
 - Nurses, 29
 - trauma, 36
 - * **federated**
 - bfi, 4
 - * **models**
 - bfi, 4
 - MAP.estimation, 21
 - summary.bfi, 30
 - * **nonparametric**
 - bfi, 4
 - MAP.estimation, 21
 - * **optimize**
 - MAP.estimation, 21
 - * **package**
 - BFI-package, 2
 - * **regression**
 - bfi, 4
 - MAP.estimation, 21
 - n.par, 28
 - summary.bfi, 30
 - * **survival**
 - bfi, 4
 - hazards.fun, 13
 - MAP.estimation, 21
 - summary.bfi, 30
 - surv.simulate, 32
- b.diag, 3
bfi, 4, 26, 30, 31
BFI-package, 2
hazards.fun, 13
inv.prior.cov, 8, 16, 22, 26
MAP.estimation, 8, 15, 19, 20, 30, 31, 34
n.par, 28
Nurses, 29
stats, 24
summary(summary.bfi), 30
summary.bfi, 26, 30
surv.simulate, 32
trauma, 36