

Package ‘bayeslm’

October 12, 2022

Type Package

Title Efficient Sampling for Gaussian Linear Regression with Arbitrary Priors

Version 1.0.1

Date 2022-6-25

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Description Efficient sampling for Gaussian linear regression with arbitrary priors, Hahn, He and Lopes (2018) <[arXiv:1806.05738](https://arxiv.org/abs/1806.05738)>.

License LGPL (>= 2)

Imports Rcpp (>= 0.12.7), stats, graphics, grDevices, coda, methods, RcppParallel

SystemRequirements GNU make

Depends R (>= 2.10)

URL <https://github.com/JingyuHe/bayeslm>

NeedsCompilation yes

LinkingTo Rcpp, RcppArmadillo, RcppParallel

Suggests rmarkdown, knitr

VignetteBuilder knitr

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Repository CRAN

Date/Publication 2022-06-27 22:50:02 UTC

R topics documented:

bayeslm-package	2
bayeslm	2
hs_gibbs	6

plot.MCMC	7
predict.bayeslm.fit	8
summary.bayeslm.fit	9
summary.MCMC	10

Index	12
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bayeslm-package	<i>Efficient sampling for Gaussian linear regression with arbitrary priors</i>
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Description

The elliptical slice sampler for Bayesian linear regression with shrinkage priors such as horseshoe, Laplace prior, ridge prior.

Author(s)

P. Richard Hahn, Jingyu He and Hedibert Lopes

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References

Hahn, P. Richard, Jingyu He, and Hedibert Lopes. *Efficient sampling for Gaussian linear regression with arbitrary priors* (2017).

See Also

bayeslm

bayeslm	<i>Efficient sampling for Gaussian linear model with arbitrary priors</i>
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Description

This package implements an efficient sampler for Gaussian Bayesian linear regression. The package uses elliptical slice sampler instead of regular Gibbs sampler. The function has several built-in priors and user can also provide their own prior function (written as a R function).

Usage

```
## Default S3 method:
bayeslm(Y, X = FALSE, prior = "horseshoe", penalize = NULL,
block_vec = NULL, sigma = NULL, s2 = 1, kap2 = 1, N = 20000L, burnin = 0L,
thinning = 1L, vglobal = 1, sampling_vglobal = TRUE, verb = FALSE, irect = TRUE,
standardize = TRUE, singular = FALSE, scale_sigma_prior = TRUE, prior_mean = NULL,
prob_vec = NULL, cc = NULL, lambda = NULL, ...)

## S3 method for class 'formula'
bayeslm(formula, data = list(), Y = FALSE, X = FALSE,
prior = "horseshoe", penalize = NULL, block_vec = NULL, sigma = NULL,
s2 = 1, kap2 = 1, N = 20000L, burnin = 0L, thinning = 1L, vglobal = 1,
sampling_vglobal = TRUE, verb = FALSE, standardize = TRUE, singular = FALSE,
scale_sigma_prior = TRUE, prior_mean = NULL,
prob_vec = NULL, cc = NULL, lambda = NULL, ...)
```

Arguments

formula	formula of the model to fit.
data	an optional data frame containing the variables in the model. By default the variables are taken from the environment which bayeslm is called from.
Y	data.frame, matrix, or vector of inputs Y. Response variable.
X	data.frame, matrix, or vector of inputs X. Regressors.
prior	Indicating shrinkage prior to use. "horseshoe" for approximate horseshoe prior (default), "laplace" for laplace prior, "ridge" for ridge prior, "sharkfin" for "sharkfin" prior and "nonlocal" for nonlocal prior.
block_vec	A vector indicating number of regressors in each block. Sum of all entries should be the same as number of regressors. The default value is block_vec = rep(1, p), put every regressor in its own block (slice-within-Gibbs sampler)
penalize	A vector indicating shrink regressors or not. It's length should be the same as number of regressors. 1 indicates shrink corresponding coefficient, 0 indicates no shrinkage. The default value is rep(1, p), shrink all coefficients
sigma	Initial value of residual standard error. The default value is half of standard error of Y.
s2, kap2	Parameter of prior over sigma, an inverse gamma prior with rate s2 and shape s2.
N	Number of posterior samples (after burn-in).
burnin	Number of burn-in samples. If burnin > 0, the function will draw N + burnin samples and return the last N samples only.
thinning	Number of thinnings. thinning = 1 means no thinning.
vglobal	Initial value of global shrinkage parameter. Default value is 1
sampling_vglobal	Bool, if TRUE, sampling the global shrinkage parameter by random walk Metropolis Hastings on log scale, otherwise always stay at the initial value vglobal.

verb	Bool, if TRUE, print out sampling progress.
icept	Bool, if the inputs are matrix X and Y, and icept = TRUE, the function will estimate intercept. Default value is TRUE. If the input is formula $Y \sim X$, option icept is useless, control intercept by formula $Y \sim X$ or $Y \sim X - 1$.
standardize	Bool, if TRUE, standardize X and Y before sampling.
singular	Bool, if TRUE, take it as a rank-deficient case such as $n < p$ or $X'X$ is singular. See section 2.3.2 of the paper for details.
scale_sigma_prior	Bool, if TRUE, the prior of regression coefficient β is scaled by residual standard error σ .
prior_mean	vector, specify prior mean of nonlocal prior for each regressor. It should have length p (no intercept) or p + 1 (intercept). The default value is 1.5 for all regressors.
prob_vec	vector, specify prior mean of sharkfin prior for each regressor. It should have length p (no intercept) or p + 1 (intercept). The default value is 0.25 for all regressors.
cc	Only works when singular == TRUE, precision parameter of ridge adjustment. It should be a vector with length \$p\$. If it is NULL, it will be set as rep(10, p).
lambda	The shrinkage parameter for Laplace prior only.
...	optional parameters to be passed to the low level function bayeslm.default.

Details

For details of the approach, please see Hahn, He and Lopes (2017)

Value

loops	A vector of number of elliptical slice sampler loops for each posterior sample.
sigma	A vector of posterior samples of residual standard error.
vglobal	A vector of posterior samples of the global shrinkage parameter.
beta	A matrix of posterior samples of coefficients.
fitted.values	Fitted values of the regression model. Take posterior mean of coefficients with 20% burnin samples.
residuals	Residuals of the regression model, equals $y - \text{fitted.values}$.

Note

horseshoe is essentially call function bayeslm with prior = "horseshoe". Same for sharkfin, ridge, blasso, nonlocal.

Author(s)

Jingyu He <jingyu.he@chicagobooth.edu>

References

Hahn, P. Richard, Jingyu He, and Hedibert Lopes. *Efficient sampling for Gaussian linear regression with arbitrary priors*. (2017).

Examples

```
p = 20
n = 100

kappa = 1.25
beta_true = c(c(1,2,3),rnorm(p-3,0,0.01))
sig_true = kappa*sqrt(sum(beta_true^2))

x = matrix(rnorm(p*n),n,p)
y = x %*% beta_true + sig_true * rnorm(n)

x = as.matrix(x)
y = as.matrix(y)
data = data.frame(x = x, y = y)

block_vec = rep(1, p) # slice-within-Gibbs sampler, put every coefficient in its own block

fitOLS = lm(y~x-1)

# call the function using formulas
fita = bayeslm(y ~ x, prior = 'horseshoe',
              block_vec = block_vec, N = 10000, burnin = 2000)
# summary the results
summary(fita)
summary(fita$beta)

# put the first two coefficients in one elliptical sampling block
block_vec2 = c(2, rep(1, p-2))
fitb = bayeslm(y ~ x, data = data, prior = 'horseshoe',
              block_vec = block_vec2, N = 10000, burnin = 2000)

# comparing several different priors

fit1 = bayeslm(y,x,prior = 'horseshoe', icept = FALSE,
              block_vec = block_vec, N = 10000, burnin=2000)
beta_est1 = colMeans(fit1$beta)

fit2 = bayeslm(y,x,prior = 'laplace', icept = FALSE,
              block_vec = block_vec, N = 10000, burnin=2000)
beta_est2 = colMeans(fit2$beta)

fit3 = bayeslm(y,x,prior = 'ridge', icept = FALSE,
              block_vec = block_vec, N = 10000, burnin=2000)
```

```

beta_est3 = colMeans(fit3$beta)

fit4 = bayeslm(y,x,prior = 'sharkfin', icept = FALSE,
              block_vec = block_vec, N = 10000, burnin=2000)
beta_est4 = colMeans(fit4$beta)

fit5 = bayeslm(y,x,prior = 'nonlocal', icept = FALSE,
              block_vec = block_vec, N = 10000, burnin=2000)
beta_est5 = colMeans(fit5$beta)

plot(NULL,xlim=range(beta_true),ylim=range(beta_true),
     xlab = "beta true", ylab = "estimation")
points(beta_true,beta_est1,pch=20)
points(beta_true,fitOLS$coef,col='red')
points(beta_true,beta_est2,pch=20,col='cyan')
points(beta_true,beta_est3,pch=20,col='orange')
points(beta_true,beta_est4,pch=20,col='pink')
points(beta_true,beta_est5,pch=20,col='lightgreen')

legend("topleft", c("OLS", "horseshoe", "laplace", "ridge", "sharkfin",
                  "nonlocal"), col = c("red", "black", "cyan", "orange",
                  "pink", "lightgreen"), pch = rep(1, 6))

abline(0,1,col='red')

rmseOLS = sqrt(sum((fitOLS$coef-beta_true)^2))
rmse1 = sqrt(sum((beta_est1-beta_true)^2))
rmse2 = sqrt(sum((beta_est2-beta_true)^2))
rmse3 = sqrt(sum((beta_est3-beta_true)^2))
rmse4 = sqrt(sum((beta_est4-beta_true)^2))
rmse5 = sqrt(sum((beta_est5-beta_true)^2))

print(cbind(ols = rmseOLS, hs = rmse1,laplace = rmse2,
            ridge = rmse3,sharkfin = rmse4,nonlocal = rmse5))

```

hs_gibbs

Gibbs sampler of horseshoe regression

Description

Standard Gibbs sampler of horseshoe regression.

Usage

```
hs_gibbs(Y, X, nsamps, a, b, scale_sigma_prior)
```

Arguments

Y	Response of regression.
X	Matrix of regressors.
nsamps	Number of posterior samples.
a	Parameter of inverse Gamma prior on σ .
b	Parameter of inverse Gamma prior on σ .
scale_sigma_prior	Bool, if TRUE, use prior scaled by σ .

Details

This function implements standard Gibbs sampler of horseshoe regression. The prior is $y \mid \beta, \sigma^2, X \sim MVN(X\beta, \sigma^2 I)$ $\beta_i \mid \tau, \lambda_i, \sigma \sim N(0, \lambda_i^2 \tau^2 \sigma^2)$ $\sigma^2 \sim IG(a, b)$ $\tau \sim C^+(0, 1)$ $\lambda_i \sim C^+(0, 1)$

Author(s)

Jingyu He

See Also

[summary.mcmc](#)

Examples

```
x = matrix(rnorm(1000), 100, 10)
y = x %*% rnorm(10) + rnorm(100)
fit=hs_gibbs(y, x, 1000, 1, 1, TRUE)
summary(fit)
```

plot.MCMC

Plot posterior summary

Description

plot.MCMC is an S3 method to plot empirical distribution of posterior draws. The input is a MCMC matrix

Usage

```
## S3 method for class 'MCMC'
plot(x, names, burnin=trunc(.1*nrow(X)), tvalues, TRACEPLOT=TRUE, DEN=TRUE, INT=TRUE,
      CHECK_NDRAWS=TRUE, ... )
```

Arguments

x	A MCMC class matrix of posterior draws, such as bayeslm\beta.
names	an optional character vector of names for the columns of X.
burnin	Number of draws to burn-in (default value is $0.1 * nrow(X)$).
tvalues	vector of true values.
TRACEPLOT	logical, TRUE provide sequence plots of draws and acfs (default: TRUE)
DEN	logical, TRUE use density scale on histograms (default: TRUE)
INT	logical, TRUE put various intervals and points on graph (default: TRUE)
CHECK_NDRAWS	logical, TRUE check that there are at least 100 draws (default: TRUE)
...	optional arguments for generic function.

Details

This function is modified from package bayesm by Peter Rossi. It plots summary of posterior draws.

Author(s)

Peter Rossi, Anderson School, UCLA, <perossichi@gmail.com>.

See Also

[summary.bayeslm.fit](#)

Examples

```
x = matrix(rnorm(1000), 100, 10)
y = x %*% rnorm(10) + rnorm(100)
fit=bayeslm(y~x)
plot(fit$beta)
```

predict.bayeslm.fit *Predict new data*

Description

predict.bayeslm.fit is an S3 method to predict response on new data.

Usage

```
## S3 method for class 'bayeslm.fit'
predict(object,data,burnin,X,...)
```


Arguments

object	object is output of bayeslm function.
data	A data frame or list of new data to predict.
burnin	number of draws to burn-in (default value is $0.1 * nrow(X)$).
X	If call bayeslm with matrices input x and y but not formula, pass new matrix to predict here. See example for details.
...	optional arguments for generic function.

Details

Make prediction on new data set, users are allowed to adjust number of burn-in samples.

Author(s)

Jingyu He

Examples

```
x = matrix(rnorm(1000), 100, 10)
y = x %*% rnorm(10) + rnorm(100)
data = list(x = x, y = y)

# Train the model with formula input
fit1 = bayeslm(y ~ x, data = data)
# predict
pred1 = predict(fit1, data)

# Train the model with matrices input
fit2 = bayeslm(Y = y, X = x)
pred2 = predict(fit2, X = x)
```

summary.bayeslm.fit *Summarize fitted object of bayeslm*

Description

summary.bayeslm.fit is an S3 method to summarize returned object of function bayeslm. The input should be bayeslm.fit object.

Usage

```
## S3 method for class 'bayeslm.fit'
summary(object, names, burnin=NULL, quantiles=FALSE, trailer=TRUE, ...)
```

Arguments

object	object is a fitted object, returned by function bayeslm.
names	an optional character vector of names for all the coefficients.
burnin	number of draws to burn-in (if it is NULL, will set default value as $0.2 * nrow(object\$beta)$)
quantiles	logical for should quantiles be displayed (def: FALSE)
trailer	logical for should a trailer be displayed (def: TRUE)
...	optional arguments for generic function

Details

This function summarize returned object of function bayeslm. It prints mean, std Dev, effective sample size (computed by function effectiveSize in package coda) coefficients posterior samples. If quantiles=TRUE, quantiles of marginal distributions in the columns of X are displayed.

The function also returns significance level, defined by whether the symmetric posterior quantile-based credible interval excludes zero. For example, a regression coefficient with one * has 0.025 quantile and 0.975 quantile with the same sign. Similarly, '***' denotes 0.0005 and 0.9995, '**' denotes 0.005 and 0.995, '*' denotes 0.025 and 0.975, '.' denotes 0.05 and 0.95 quantiles with the same sign.

Author(s)

Jingyu He

See Also

[summary.mcmc](#)

Examples

```
x = matrix(rnorm(1000), 100, 10)
y = x %*% rnorm(10) + rnorm(100)
fit=bayeslm(y~x)
summary(fit)
```

summary.MCMC

Summarize posterior draws

Description

summary.MCMC is an S3 method to summarize posterior draws of the model. The input should be a matrix of draws.

Usage

```
## S3 method for class 'MCMC'
summary(object, names, burnin=trunc(.1*nrow(X)), quantiles=FALSE, trailer=TRUE, ...)
```

Arguments

object	object is a matrix of draws, usually an object of class MCMC. It's same as X .
names	an optional character vector of names for the columns of X .
burnin	number of draws to burn-in (default value is $0.1 * nrow(X)$).
quantiles	logical for should quantiles be displayed (def: FALSE).
trailer	logical for should a trailer be displayed (def: TRUE).
...	optional arguments for generic function.

Details

This function is modified from package `bayesm` by Peter Rossi. It summarize object MCMC. Mean, Std Dev, effective sample size (computed by function `effectiveSize` in package `coda`) are displayed. If `quantiles=TRUE`, quantiles of marginal distributions in the columns of X are displayed.

The function also returns significance level, defined by whether the symmetric posterior quantile-based credible interval excludes zero. For example, a regression coefficient with one `*` has 0.025 quantile and 0.975 quantile with the same sign. Similarly, `***` denotes 0.0005 and 0.9995, `**` denotes 0.005 and 0.995, `*` denotes 0.025 and 0.975, `.` denotes 0.05 and 0.95 quantiles with the same sign.

Author(s)

Peter Rossi, Anderson School, UCLA, <perossichi@gmail.com>.

See Also

[summary.bayeslm.fit](#)

Examples

```
x = matrix(rnorm(1000), 100, 10)
y = x %*% rnorm(10) + rnorm(100)
fit=bayeslm(y~x)
summary(fit$beta)
```

Index

- * **linear regression**
 - bayeslm, [2](#)
- * **package**
 - bayeslm-package, [2](#)
- * **sumamry**
 - summary.MCMC, [10](#)
- * **summary**
 - plot.MCMC, [7](#)
 - summary.bayeslm.fit, [9](#)
- * **univar**
 - hs_gibbs, [6](#)
 - predict.bayeslm.fit, [8](#)

bayeslm, [2](#)
bayeslm-package, [2](#)

hs_gibbs, [6](#)

plot.MCMC, [7](#)
predict.bayeslm.fit, [8](#)

summary.bayeslm.fit, [8](#), [9](#), [11](#)
summary.MCMC, [10](#)
summary.mcmc, [7](#), [10](#)