

# Package ‘TSCI’

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**Title** Tools for Causal Inference with Possibly Invalid Instrumental Variables

**Version** 3.0.4

**Description** Two stage curvature identification with machine learning for causal inference in settings when instrumental variable regression is not suitable because of potentially invalid instrumental variables. Based on Guo and Buehlmann (2022) ``Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables" <[arXiv:2203.12808](https://arxiv.org/abs/2203.12808)>. The vignette is available in Carl, Emmenegger, Bühlmann and Guo (2023) ``TSCI: two stage curvature identification for causal inference with invalid instruments" <[arXiv:2304.00513](https://arxiv.org/abs/2304.00513)>.

**URL** <https://github.com/dlcarl/TSCI>

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coef.tsci	<i>Extract Model Coefficients of TSCI Fits.</i>
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### Description

Extract Model Coefficients of TSCI Fits.

### Usage

```
## S3 method for class 'tsci'
coef(object, parm = NULL, ...)
```

### Arguments

object	an object of class 'tsci'.
parm	a specification for which treatment effect estimates should be returned. Either a vector of numbers or a vector of names or 'all'. If missing, the treatment effect estimate by violation space selection is returned. If 'all', the treatment effect estimates for all violation space candidates are returned.
...	arguments to be passed to or from other methods.

### Value

Coefficients extracted from the model object object.

---

confint.tsci                      *Confidence Intervals of Treatment Effect Estimates for TSCI Fits.*

---

**Description**

Confidence Intervals of Treatment Effect Estimates for TSCI Fits.

**Usage**

```
## S3 method for class 'tsci'
confint(object, parm = NULL, level = 0.95, ...)
```

**Arguments**

object	an object of class 'tsci'.
parm	a specification of the parameters for which confidence intervals should be calculated. Either a vector of numbers or a vector of names or 'all'. If missing, the confidence interval of treatment effect estimate by violation space selection is returned. If 'all', the confidence intervals for all violation space candidates are returned.
level	the confidence level required.
...	additional argument(s) for methods.

**Value**

a matrix containing the confidence intervals.

---

create\_interactions            *Interactions as Violation Space Candidates*

---

**Description**

Interactions as Violation Space Candidates

**Usage**

```
create_interactions(Z, X = NULL)
```

**Arguments**

Z	observations of the instrumental variable(s). Either a numeric vector of length n or a numeric matrix with dimension n by s.
X	observations of baseline covariate(s) for which interactions with the instrumental variable(s) should be part of the violation space candidates. Either a numeric vector of length n or a numeric matrix with dimension n by p or NULL (if only interactions between the instrumental variables itself should be part of the violation space candidates).

**Value**

A list. The first element contains the observations of the instrumental variable(s)  $Z$ . The second element contains all interactions between the instrumental variable(s) and the baseline covariate(s)  $X$ .

**Examples**

```
Z <- matrix(rnorm(100 * 3), nrow = 100, ncol = 3)
X <- matrix(rnorm(100 * 3), nrow = 100, ncol = 3)
vio_space <- create_interactions(Z = Z, X = X)
```

---

create\_monomials      *Monomials as Violation Space Candidates*

---

**Description**

Monomials as Violation Space Candidates

**Usage**

```
create_monomials(Z, degree, type = c("monomials_main", "monomials_full"))
```

**Arguments**

$Z$	observations of the instrumental variable(s). Either a numeric vector of length $n$ or a numeric matrix with dimension $n$ by $s$ .
degree	The degree up to which monomials should be created. Either a single positive integer or a vector of length $s$ containing positive integers.
type	One out of <code>monomials_main</code> or <code>monomials_full</code> . <code>monomials_main</code> creates the monomials for the polynomials of each instrumental variable up to degree <code>degree</code> . <code>monomials_full</code> creates the monomials for the polynomials of a combination of all instrumental variables up to degree <code>degree</code> . Default is <code>monomials_full</code> .

**Details**

assuming there are 3 instrumental variables  $Z_1$ ,  $Z_2$ , and  $Z_3$  and `degree = c(d1, d2, d3)` with  $d_1 < d_2 < d_3$ , `monomials_main` creates the monomials of the polynomials  $(Z_1 + 1)^{d_1}$ ,  $(Z_2 + 1)^{d_2}$ ,  $(Z_3 + 1)^{d_3}$  without the constants and `monomials_full` creates the monomials  $(Z_1 + Z_2 + Z_3)$ ,  $(Z_1 + Z_2 + Z_3)^2$ , ...,  $(Z_1 + Z_2 + Z_3)^{d_3}$  without the constants and excluding monomials that are products of  $Z_1^d$  or  $Z_2^d$  with  $d > d_1$  resp.  $d > d_2$ . Thus `type = monomials_main` does not include interactions between the instrumental variables.

**Value**

A list. Each element is a matrix consisting of the monomials to be added to the next violation space candidate.

**Examples**

```
Z <- matrix(rnorm(100 * 3), nrow = 100, ncol = 3)
vio_space <- create_monomials(Z = Z, degree = 4, type = "monomials_full")
```

---

```
print.summary.tsci      Print Content of summary.tsci Object.
```

---

**Description**

Print Content of summary.tsci Object.

**Usage**

```
## S3 method for class 'summary.tsci'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

x	an object of class 'summary.tsci'.
digits	number of significant digits to display.
...	arguments to be passed to or from other methods.

---

```
print.tsci              Print Content of tsci Object.
```

---

**Description**

Print Content of tsci Object.

**Usage**

```
## S3 method for class 'tsci'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

x	an object of class 'tsci'.
digits	number of significant digits to display.
...	arguments to be passed to or from other methods.

summary.tsci

*Summarizing Two Stage Curvature Identification Fits***Description**

Summarizing Two Stage Curvature Identification Fits

**Usage**

```
## S3 method for class 'tsci'
summary(object, extended_output = FALSE, ...)
```

**Arguments**

object            an object of class 'tsci'.  
 extended\_output        logical. If TRUE are more detailed summary is returned.  
 ...                arguments to be passed to or from other methods.

**Value**

an object of class 'summary.tsci' containing the following elements:

coefficient a data frame with columns for the estimated treatment coefficient, its standard error, confidence interval and (two-sided) p-value.

invalidity a vector containing the number of times the instrumental variable(s) were considered valid, invalid or too weak to perform the test.

viospace\_selection a data frame with columns for the number of times each of the violation space candidate was selected by comparison, the conservative method and as the largest violation space candidate for which the instrumental variable was considered to be strong enough.

treatment\_model a data frame with information about the method used to fit the treatment model.

sample\_size\_A1 the number of observations in the subset used to fit the outcome model.

sample\_size\_A2 the number of observations in the subset used to train the parameters for fitting the treatment model.

n\_splits the number of sample splits performed.

mult\_split\_method the method used to calculate the standard errors and p-values if n\_splits is larger than 1.

alpha the significance level used.

iv\_strength a data frame with columns containing the estimated instrumental variable strength and the estimated instrumental variable strength threshold for each violation space candidate. Will only be returned if extended\_output is true.

coefficients\_all a data frame with columns for the estimated treatment coefficients, its standard errors, confidence intervals and (two-sided) p-values for each violation space candidate.

**Description**

tsci\_boosting implements Two Stage Curvature Identification (Guo and Buehlmann 2022) with boosting. Through a data-dependent way, it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

**Usage**

```
tsci_boosting(  
  Y,  
  D,  
  Z,  
  X = NULL,  
  W = X,  
  vio_space,  
  create_nested_sequence = TRUE,  
  sel_method = c("comparison", "conservative"),  
  split_prop = 2/3,  
  nrounds = 50,  
  eta = 0.3,  
  max_depth = c(1:6),  
  subsample = 1,  
  colsample_bytree = 1,  
  early_stopping = TRUE,  
  nfolds = 5,  
  self_predict = FALSE,  
  sd_boot = TRUE,  
  iv_threshold = 10,  
  threshold_boot = TRUE,  
  alpha = 0.05,  
  intercept = TRUE,  
  parallel = c("no", "multicore", "snow"),  
  nsplits = 10,  
  mult_split_method = c("FWER", "DML"),  
  ncores = 1,  
  cl = NULL,  
  raw_output = NULL,  
  B = 300  
)
```

**Arguments**

Y	observations of the outcome variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If outcome variable is binary use dummy encoding.
D	observations of the treatment variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If treatment variable is binary use dummy encoding.
Z	observations of the instrumental variable(s). Either a vector of length n or a matrix with dimension n by s. If observations are not numeric dummy encoding will be applied.
X	observations of baseline covariate(s). Either a vector of length n or a matrix with dimension n by p or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
W	(transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length n or a matrix with dimension n by p_w or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
vio_space	list with vectors of length n and/or matrices with n rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information.
create_nested_sequence	logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of vio_space to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of vio_space. See Details for more information.
sel_method	The selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.
split_prop	proportion of observations used to fit the outcome model. Has to be a value in (0, 1).
nrounds	number of boosting iterations. Can either be a single integer value or a vector of integer values to try.
eta	learning rate of the boosting algorithm. Can either be a single numeric value or a vector of numeric values to try.
max_depth	maximal tree depth. Can either be a single integer value or a vector of integer values to try.
subsample	subsample ratio of the training instance. Can either be a single numeric value or a vector of numeric values to try. Has to be a numeric value in (0, 1].
colsample_bytree	subsample ratio of columns when constructing each tree. Can either be a single numeric value or a vector of numeric values to try. Has to be a numeric value in (0, 1].
early_stopping	logical. If TRUE, early stopping will be applied to choose the optimal number of boosting iteration using the cross-validation mean squared error.



<code>nfolds</code>	a positive integer value specifying the number of folds used for cross-validation to choose best parameter combination.
<code>self_predict</code>	logical. If FALSE, it sets the diagonal of the hat matrix of each tree to zero to avoid self-prediction and rescales the off-diagonal elements accordingly.
<code>sd_boot</code>	logical. if TRUE, it determines the standard error using a bootstrap approach.
<code>iv_threshold</code>	a numeric value specifying the minimum of the threshold of IV strength test.
<code>threshold_boot</code>	logical. if TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.
<code>alpha</code>	the significance level. Has to be a numeric value between 0 and 1.
<code>intercept</code>	logical. If TRUE, an intercept is included in the outcome model.
<code>parallel</code>	one out of "no", "multicore", or "snow" specifying the parallelization method used.
<code>nsplits</code>	number of times the data will be split. Has to be an integer larger or equal 1. See Details.
<code>mult_split_method</code>	method to calculate the standard errors, p-values and to construct the confidence intervals if multi-splitting is performed. Default is "DML" if <code>nsplits == 1</code> and "FWER" otherwise. See Details.
<code>ncores</code>	the number of cores to use. Has to be an integer value larger or equal 1.
<code>cl</code>	either a parallel or snow cluster or NULL.
<code>raw_output</code>	logical. If TRUE, the coefficient and standard error estimates of each split will be returned. This is only needed for the use of the function <code>confint</code> if <code>mult_split_method</code> equals "FWER". Default is TRUE if <code>mult_split_method</code> is TRUE and FALSE otherwise.
<code>B</code>	number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the IV strength threshold if <code>threshold_boot</code> is TRUE and for the violation space selection.

## Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where  $f(Z_i, X_i)$  is estimated using L2 boosting with regression trees as base learners,  $h(Z_i, X_i)$  is approximated using the violation space candidates and  $\phi(X_i)$  is approximated by a linear combination of the columns in  $W$ . The errors are allowed to be heteroscedastic. To avoid overfitting bias the data is randomly split into two subsets  $A_1$  and  $A_2$  where the proportion of observations in the two sets is specified by `split_prop`.  $A_2$  is used to train the random forest and  $A_1$  is used to perform violation space selection and to estimate the treatment effect.

The package `xgboost` is used for boosting. If any of `nrounds`, `eta`, `max_depth`, `subsample` or `colsample_bytree` has more than one value, the best parameter combination is chosen by minimizing the cross-validation mean squared error.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list `vio_space` that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If `sel_method` is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If `sel_method` is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength is large enough. The specification of suitable violation space candidates is a crucial step because a poor approximation of  $g(Z_i, X_i)$  might not address the bias caused by the violation of the IV assumption sufficiently well. The function `create_monomials` can be used to create a predefined sequence of violation space candidates consisting of monomials. The function `create_interactions` can be used to create a predefined sequence of violation space candidates consisting of two-way interactions between the instruments themselves and between the instruments and the instruments and baseline covariates.

$W$  should be chosen to be flexible enough to approximate the functional form of  $\phi$  well as otherwise the treatment estimator might be biased.

The instrumental variable(s) are considered strong enough for violation space candidate  $V_q$  if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\} + S(V_q), 40\}$  if `threshold_boot` is TRUE, and  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\}, 40\}$  if `threshold_boot` is FALSE. The matrix  $M(V_q)$  depends on the hat matrix obtained from estimating  $f(Z_i, X_i)$ , the violation space candidate  $V_q$  and the variables to include in the outcome model  $W$ .  $S(V_q)$  is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using `threshold_boot` equals TRUE leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

`nsplits` specifies the number of data splits that should be performed. For each data split the output statistics such as the point estimates of the treatment effect are calculated. Those statistics will then be aggregated over the different data splits. It is recommended to perform multiple data splits as data splitting introduces additional randomness. By aggregating the results of multiple data splits, the effects of this randomness can be decreased. If `nsplits` is larger than 1, point estimates are aggregated by medians. Standard errors, p-values and confidence intervals are obtained by the method specified by the parameter `mult_split_method`. 'DML' uses the approach by Chernozhukov et al. (2018). 'FWER' uses the approach by Meinshausen et al. (2009) and controls for the family-wise error rate. 'FWER' does not provide standard errors. For large sample sizes, a large values for `nsplits` can lead to a high running time as for each split a new hat matrix must be calculated.

There are three possibilities to set the argument `parallel`, namely "no" for serial evaluation (default), "multicore" for parallel evaluation using forking, and "snow" for parallel evaluation using a parallel socket cluster. It is recommended to select `RNGkind` ("L'Ecuyer-CMRG") and to set a seed to ensure that the parallel computing of the package TSCI is reproducible. This ensures that each processor receives a different substream of the pseudo random number generator stream. Thus, the results are reproducible if the arguments (including `ncores`) remain unchanged. There is an op-

tional argument `cl` to specify a custom cluster if `parallel = "snow"`.

See also Carl et al. (2023) for more details.

### Value

A list containing the following elements:

`Coef_all` a series of point estimates of the treatment effect obtained by the different violation space candidates.

`sd_all` standard errors of the estimates of the treatment effect obtained by the different violation space candidates.

`pval_all` p-values of the treatment effect estimates obtained by the different violation space candidates.

`CI_all` confidence intervals for the treatment effect obtained by the different violation space candidates.

`Coef_sel` the point estimator of the treatment effect obtained by the selected violation space candidate(s).

`sd_sel` the standard error of `Coef_sel`.

`pval_sel` p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

`CI_sel` confidence interval for the treatment effect obtained by the selected violation space candidate(s).

`iv_str` IV strength using the different violation space candidates.

`iv_thol` the threshold for the IV strength using the different violation space candidates.

`Qmax` the frequency each violation space candidate was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test over the multiple data splits. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.

`q_comp` the frequency each violation space candidate was selected by the comparison method over the multiple data splits.

`q_cons` the frequency each violation space candidate was selected by the conservative method over the multiple data splits.

`invalidity` the frequency the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

`mse` the out-of-sample mean squared error of the fitted treatment model.

`FirstStage_model` the method used to fit the treatment model.

`n_A1` number of observations in A1.

`n_A2` number of observations in A2.

`nsplits` number of data splits performed.

`mult_split_method` the method used to calculate the standard errors and p-values.

`alpha` the significance level used.

## References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022
- Nicolai Meinshausen, Lukas Meier, and Peter Buehlmann. P-values for high-dimensional regression. *Journal of the American Statistical Association*, 104(488):1671-1681, 2009. 16, 18
- Victor Chernozhukov, Denis Chetverikov, Mert Demirer, Esther Duflo, Christian Hansen, Whitney Newey, and James Robins. Double/debiased machine learning for treatment and structural parameters: Double/debiased machine learning. *The Econometrics Journal*, 21(1), 2018. 4, 16, 18
- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

## See Also

[tsci\\_forest](#) for TSCI with random forest.

[tsci\\_poly](#) for TSCI with polynomial basis expansion.

[tsci\\_secondstage](#) for TSCI with user provided hat matrix.

## Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
  n <- 100
  # the IV strength
  a <- 1
  # the violation strength
  tau <- 1
  # true effect
  beta <- 1
  # treatment model
  f <- function(x) {1 + a * (x + x^2)}
  # outcome model
  g <- function(x) {1 + tau * x}

  # generate data
  mu_error <- rep(0, 2)
  Cov_error <- matrix(c(1, 0.5, 0.5, 1), 2, 2)
  Error <- MASS::mvrnorm(n, mu_error, Cov_error)
  # instrumental variable
  Z <- rnorm(n)
  # treatment variable
  D <- f(Z) + Error[, 1]
  # outcome variable
  Y <- beta * D + g(Z) + Error[, 2]
```

```

# Two Stage L2 Boosting
# create violation space candidates
vio_space <- create_monomials(Z, 2, "monomials_main")
# perform two stage curvature identification
output_B0 <- tsci_boosting(Y, D, Z, vio_space = vio_space, nsplits = 1,
                           max_depth = 2, nrounds = 10, B = 100)
summary(output_B0)
}

```

---

tsci\_forest

*Two Stage Curvature Identification with Random Forests*


---

### Description

tsci\_forest implements Two Stage Curvature Identification (Guo and Buehlmann 2022) with random forests. Through a data-dependent way, it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

### Usage

```

tsci_forest(
  Y,
  D,
  Z,
  X = NULL,
  W = X,
  vio_space,
  create_nested_sequence = TRUE,
  sel_method = c("comparison", "conservative"),
  split_prop = 2/3,
  num_trees = 200,
  mtry = NULL,
  max_depth = 0,
  min_node_size = c(5, 10, 20),
  self_predict = FALSE,
  sd_boot = TRUE,
  iv_threshold = 10,
  threshold_boot = TRUE,
  alpha = 0.05,
  nsplits = 10,
  mult_split_method = c("FWER", "DML"),
  intercept = TRUE,
  parallel = c("no", "multicore", "snow"),
  ncores = 1,
  cl = NULL,

```

```

    raw_output = NULL,
    B = 300
)

```

### Arguments

Y	observations of the outcome variable. Either a numeric vector of length $n$ or a numeric matrix with dimension $n$ by 1. If outcome variable is binary use dummy encoding.
D	observations of the treatment variable. Either a numeric vector of length $n$ or a numeric matrix with dimension $n$ by 1. If treatment variable is binary use dummy encoding.
Z	observations of the instrumental variable(s). Either a vector of length $n$ or a matrix with dimension $n$ by $s$ . If observations are not numeric dummy encoding will be applied.
X	observations of baseline covariate(s). Either a vector of length $n$ or a matrix with dimension $n$ by $p$ or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
W	(transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length $n$ or a matrix with dimension $n$ by $p_w$ or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
vio_space	list with vectors of length $n$ and/or matrices with $n$ rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information.
create_nested_sequence	logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of <code>vio_space</code> to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of <code>vio_space</code> . See Details for more information.
sel_method	the selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.
split_prop	proportion of observations used to fit the outcome model. Has to be a numeric value in $(0, 1)$ .
num_trees	number of trees in random forests. Can either be a single integer value or a vector of integer values to try.
mtry	number of covariates to possibly split at in each node of the tree of the random forest. Can either be a single integer value or a vector of integer values to try. Can also be a list of single argument function(s) returning an integer value, given the number of independent variables. The values have to be positive integers not larger than the number of independent variables in the treatment model. Default is to try all integer values between one-third of the independent variables and two-thirds of the independent variables.
max_depth	maximal tree depth in random forests. Can either be a single integer value or a vector of integer values to try. 0 correspond to unlimited depth.

<code>min_node_size</code>	minimal size of each leaf node in the random forest. Can either be a single integer value or a vector of integer values to try.
<code>self_predict</code>	logical. If FALSE, it sets the diagonal of the hat matrix of each tree to zero to avoid self-prediction and rescales the off-diagonal elements accordingly.
<code>sd_boot</code>	logical. if TRUE, it determines the standard error using a bootstrap approach.
<code>iv_threshold</code>	a numeric value specifying the minimum of the threshold of IV strength test.
<code>threshold_boot</code>	logical. If TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.
<code>alpha</code>	the significance level. Has to be a numeric value between 0 and 1.
<code>nsplits</code>	number of times the data will be split. Has to be an integer larger or equal 1. See Details.
<code>mult_split_method</code>	method to calculate the standard errors, p-values and to construct the confidence intervals if multi-splitting is performed. Default is "DML" if <code>nsplits == 1</code> and "FWER" otherwise. See Details.
<code>intercept</code>	logical. If TRUE, an intercept is included in the outcome model.
<code>parallel</code>	one out of "no", "multicore", or "snow" specifying the parallelization method used. See Details.
<code>ncores</code>	the number of cores to use. Has to be an integer value larger or equal 1.
<code>cl</code>	either a parallel or snow cluster or NULL.
<code>raw_output</code>	logical. If TRUE, the coefficient and standard error estimates of each split will be returned. This is only needed for the use of the function <code>confint</code> if <code>mult_split_method</code> equals "FWER". Default is TRUE if <code>mult_split_method</code> is TRUE and FALSE otherwise.
<code>B</code>	number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the IV strength threshold if <code>threshold_boot</code> is TRUE and for the violation space selection. It is also used to calculate the standard error if <code>sd_boot</code> is TRUE.

## Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where  $f(Z_i, X_i)$  is estimated using a random forest,  $h(Z_i, X_i)$  is approximated using the violation space candidates and  $\phi(X_i)$  is approximated by a linear combination of the columns in  $W$ . The errors are allowed to be heteroscedastic. To avoid overfitting bias the data is randomly split into two subsets  $A1$  and  $A2$  where the proportion of observations in the two sets is specified by `split_prop`.  $A2$  is used to train the random forest and  $A1$  is used to perform violation space selection and to estimate the treatment effect.

The package `ranger` is used to fit the random forest. If any of `num_trees`, `max_depth` or `min_node_size` has more than one value, the best parameter combination is chosen by minimizing the out-of-bag

mean squared error.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list `vio_space` that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If `sel_method` is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If `sel_method` is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength is large enough. The specification of suitable violation space candidates is a crucial step because a poor approximation of  $g(Z_i, X_i)$  might not address the bias caused by the violation of the IV assumption sufficiently well. The function `create_monomials` can be used to create a predefined sequence of violation space candidates consisting of monomials. The function `create_interactions` can be used to create a predefined sequence of violation space candidates consisting of two-way interactions between the instruments themselves and between the instruments and the instruments and baseline covariates.

The instrumental variable(s) are considered strong enough for violation space candidate  $V_q$  if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\} + S(V_q), 40\}$  if `threshold_boot` is TRUE, and  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\}, 40\}$  if `threshold_boot` is FALSE. The matrix  $M(V_q)$  depends on the hat matrix obtained from estimating  $f(Z_i, X_i)$ , the violation space candidate  $V_q$  and the variables to include in the outcome model  $w$ .  $S(V_q)$  is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using `threshold_boot` equals TRUE leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

`nsplits` specifies the number of data splits that should be performed. For each data split the output statistics such as the point estimates of the treatment effect are calculated. Those statistics will then be aggregated over the different data splits. It is recommended to perform multiple data splits as data splitting introduces additional randomness. By aggregating the results of multiple data splits, the effects of this randomness can be decreased. If `nsplits` is larger than 1, point estimates are aggregated by medians. Standard errors, p-values and confidence intervals are obtained by the method specified by the parameter `mult_split_method`. 'DML' uses the approach by Chernozhukov et al. (2018). 'FWER' uses the approach by Meinshausen et al. (2009) and controls for the family-wise error rate. 'FWER' does not provide standard errors. For large sample sizes, a large values for `nsplits` can lead to a high running time as for each split a new hat matrix must be calculated.

There are three possibilities to set the argument `parallel`, namely "no" for serial evaluation (default), "multicore" for parallel evaluation using forking, and "snow" for parallel evaluation using a parallel socket cluster. It is recommended to select `RNGkind` ("L'Ecuyer-CMRG") and to set a seed to ensure that the parallel computing of the package TSCI is reproducible. This ensures that each processor receives a different substream of the pseudo random number generator stream. Thus, the results are reproducible if the arguments (including `ncores`) remain unchanged. There is an optional argument `cl` to specify a custom cluster if `parallel = "snow"`.



Results obtained on different operating systems might differ even when the same seed is set. The reason for this lies in the way the random forest algorithm in ranger is implemented. Currently, we are not aware of a solution to ensure reproducibility across operating systems when using tsci\_forest. However, tsci\_boosting, tsci\_poly and tsci\_secondstage do not have this issue.

See also Carl et al. (2023) for more details.

## Value

A list containing the following elements:

Coef\_all a series of point estimates of the treatment effect obtained by the different violation space candidates.

sd\_all standard errors of the estimates of the treatment effect obtained by the different violation space candidates.

pval\_all p-values of the treatment effect estimates obtained by the different violation space candidates.

CI\_all confidence intervals for the treatment effect obtained by the different violation space candidates.

Coef\_sel the point estimator of the treatment effect obtained by the selected violation space candidate(s).

sd\_sel the standard error of Coef\_sel.

pval\_sel p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

CI\_sel confidence interval for the treatment effect obtained by the selected violation space candidate(s).

iv\_str IV strength using the different violation space candidates.

iv\_thol the threshold for the IV strength using the different violation space candidates.

Qmax the frequency each violation space candidate was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test over the multiple data splits. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.

q\_comp the frequency each violation space candidate was selected by the comparison method over the multiple data splits.

q\_cons the frequency each violation space candidate was selected by the conservative method over the multiple data splits.

invalidity the frequency the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

mse the out-of-sample mean squared error of the fitted treatment model.

FirstStage\_model the method used to fit the treatment model.

n\_A1 number of observations in A1.

n\_A2 number of observations in A2.

nsplits number of data splits performed.

mult\_split\_method the method used to calculate the standard errors and p-values.

alpha the significance level used.

## References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022
- Nicolai Meinshausen, Lukas Meier, and Peter Buehlmann. P-values for high-dimensional regression. *Journal of the American Statistical Association*, 104(488):1671-1681, 2009. 16, 18
- Victor Chernozhukov, Denis Chetverikov, Mert Demirer, Esther Duflo, Christian Hansen, Whitney Newey, and James Robins. Double/debiased machine learning for treatment and structural parameters: Double/debiased machine learning. *The Econometrics Journal*, 21(1), 2018. 4, 16, 18
- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

## See Also

[tsci\\_boosting](#) for TSCI with boosting.

[tsci\\_poly](#) for TSCI with polynomial basis expansion.

[tsci\\_secondstage](#) for TSCI with user provided hat matrix.

## Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
  n <- 100
  # the IV strength
  a <- 1
  # the violation strength
  tau <- 1
  # true effect
  beta <- 1
  # treatment model
  f <- function(x) {1 + a * (x + x^2)}
  # outcome model
  g <- function(x) {1 + tau * x}

  # generate data
  mu_error <- rep(0, 2)
  Cov_error <- matrix(c(1, 0.5, 0.5, 1), 2, 2)
```

```

Error <- MASS::mvrnorm(n, mu_error, Cov_error)
# instrumental variable
Z <- rnorm(n)
# treatment variable
D <- f(Z) + Error[, 1]
# outcome variable
Y <- beta * D + g(Z) + Error[, 2]

# Two Stage Random Forest
# create violation space candidates
vio_space <- create_monomials(Z, 2, "monomials_main")
# perform two stage curvature identification
output_RF <- tsci_forest(Y, D, Z, vio_space = vio_space, nsplits = 1,
                        num_trees = 50, B = 100)
summary(output_RF)
}

```

---

tsci\_poly

*Two Stage Curvature Identification with Polynomial Basis Expansion*


---

## Description

tsci\_poly implements Two Stage Curvature Identification (Guo and Buehlmann 2022) with a basis expansion by monomials. Through a data-dependent way it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

## Usage

```

tsci_poly(
  Y,
  D,
  Z,
  X = NULL,
  W = X,
  vio_space = NULL,
  create_nested_sequence = TRUE,
  sel_method = c("comparison", "conservative"),
  min_order = 1,
  max_order = 10,
  exact_order = NULL,
  order_selection_method = c("grid search", "backfitting"),
  max_iter = 100,
  conv_tol = 10^-6,
  gcv = FALSE,
  nfolds = 5,
  sd_boot = TRUE,

```

```

iv_threshold = 10,
threshold_boot = TRUE,
alpha = 0.05,
intercept = TRUE,
B = 300
)

```

## Arguments

Y	observations of the outcome variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If outcome variable is binary use dummy encoding.
D	observations of the treatment variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If treatment variable is binary use dummy encoding.
Z	observations of the instrumental variable(s). Either a vector of length n or a matrix with dimension n by s. If observations are not numeric dummy encoding will be applied.
X	observations of baseline covariate(s). Either a vector of length n or a matrix with dimension n by p or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
W	(transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length n or a matrix with dimension n by p_w or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
vio_space	either NULL or a list with numeric vectors of length n and/or numeric matrices with n rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information. If NULL, then the violation space candidates are chosen to be a nested sequence of monomials with degree depending on the orders of the polynomials used to fit the treatment model.
create_nested_sequence	logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of vio_space to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of vio_space. See Details for more information.
sel_method	The selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.
min_order	either a single integer value or a vector of integer values of length s specifying the smallest order of polynomials to use in the selection of the treatment model. If a single integer value is provided, the polynomials of all instrumental variables use this value.
max_order	either a single integer value or a vector of integer values of length s specifying the largest order of polynomials to use in the selection of the treatment model. If a single integer value is provided, the polynomials of all instrumental variables use this value.

exact_order	either a single integer value or a vector of integer values of length $s$ specifying the exact order of polynomials to use in the treatment model. If a single integer value is provided, the polynomials of all instrumental variables use this value.
order_selection_method	method used to select the best fitting order of polynomials for the treatment model. Must be either 'grid search' or 'backfitting'. 'grid search' can be very slow if the number of instruments is large.
max_iter	number of iterations used in the backfitting algorithm if order_selection_method is 'backfitting'. Has to be a positive integer value.
conv_tol	tolerance of convergence in the backfitting algorithm if order_selection_method is 'backfitting'.
gcv	logical. If TRUE, the generalized cross-validation mean squared error is used to determine the best fitting order of polynomials for the treatment model. If FALSE, k-fold cross-validation is used instead.
nfolds	number of folds used for the k-fold cross-validation if gcv is FALSE. Has to be a positive integer value.
sd_boot	logical. if TRUE, it determines the standard error using a bootstrap approach.
iv_threshold	a numeric value specifying the minimum of the threshold of IV strength test.
threshold_boot	logical. if TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.
alpha	the significance level. Has to be a numeric value between 0 and 1.
intercept	logical. If TRUE, an intercept is included in the outcome model.
B	number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the iv strength threshold if threshold_boot is TRUE and for the violation space selection.

## Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where  $f(Z_i, X_i)$  is estimated using a polynomial basis expansion of the instrumental variables and a linear combination of the baseline covariates,  $h(Z_i, X_i)$  is approximated using the violation space candidates and  $\phi(X_i)$  is approximated by a linear combination of the columns in  $W$ . The errors are allowed to be heteroscedastic.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list `vio_space` that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If `sel_method` is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If `sel_method` is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength

is large enough. If `vio_space` is NULL the violation space candidates are chosen to be a nested sequence of polynomials of the instrumental variables up to the degrees used to fit the treatment model. This guarantees that the possible spaces of the violation will be tested. If the functional form of the outcome model is not well-known it is advisable to use the default values for `W` and `vio_space`.

The instrumental variable(s) are considered strong enough for violation space candidate  $V_q$  if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\} + S(V_q), 40\}$  if `threshold_boot` is TRUE, and  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\}, 40\}$  if `threshold_boot` is FALSE. The matrix  $M(V_q)$  depends on the hat matrix obtained from estimating  $f(Z_i, X_i)$ , the violation space candidate  $V_q$  and the variables to include in the outcome model  $W$ .  $S(V_q)$  is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using `threshold_boot` equals TRUE leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

See also Carl et al. (2023) for more details.

## Value

A list containing the following elements:

`Coef_all` a series of point estimates of the treatment effect obtained by the different violation space candidates.

`sd_all` standard errors of the estimates of the treatment effect obtained by the different violation space candidates.

`pval_all` p-values of the treatment effect estimates obtained by the different violation space candidates.

`CI_all` confidence intervals for the treatment effect obtained by the different violation space candidates.

`Coef_sel` the point estimator of the treatment effect obtained by the selected violation space candidate(s).

`sd_sel` the standard error of `Coef_sel`.

`pval_sel` p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

`CI_sel` confidence interval for the treatment effect obtained by the selected violation space candidate(s).

`iv_str` IV strength using the different violation space candidates.

`iv_thol` the threshold for the IV strength using the different violation space candidates.

`Qmax` the violation space candidate that was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.

`q_comp` the violation space candidate that was selected by the comparison method over the multiple data splits.

`q_cons` the violation space candidate that was selected by the conservative method over the multiple data splits.

`invalidity` shows whether the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

`mse` the out-of-sample mean squared error of the treatment model.

## References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022
- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

## See Also

[tsci\\_forest](#) for TSCI with random forest.

[tsci\\_boosting](#) for TSCI with boosting.

[tsci\\_secondstage](#) for TSCI with user provided hat matrix.

## Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
  n <- 100
  # the IV strength
  a <- 1
  # the violation strength
  tau <- 1
  # true effect
  beta <- 1
  # treatment model
  f <- function(x) {1 + a * (x + x^2)}
  # outcome model
  g <- function(x) {1 + tau * x}

  # generate data
  mu_error <- rep(0, 2)
  Cov_error <- matrix(c(1, 0.5, 0.5, 1), 2, 2)
  Error <- MASS::mvrnorm(n, mu_error, Cov_error)
  # instrumental variable
```

```

Z <- rnorm(n)
# treatment variable
D <- f(Z) + Error[, 1]
# outcome variable
Y <- beta * D + g(Z) + Error[, 2]

# Two Stage Polynomials
output_P0 <- tsci_poly(Y, D, Z, max_order = 3, max_iter = 20, B = 100)
summary(output_P0)
}

```

---

tsci\_secondstage

*Two Stage Curvature Identification with User Provided Hat Matrix*


---

## Description

tsci\_secondstage implements Two Stage Curvature Identification (Guo and Buehlmann 2022) for a user-provided hat matrix. Through a data-dependent way it tests for the smallest sufficiently large violation space among a pre-specified sequence of nested violation space candidates. Point and uncertainty estimates of the treatment effect for all violation space candidates including the selected violation space will be returned amongst other relevant statistics.

## Usage

```

tsci_secondstage(
  Y,
  D,
  Z,
  W = NULL,
  vio_space,
  create_nested_sequence = TRUE,
  weight,
  A1_ind = NULL,
  sel_method = c("comparison", "conservative"),
  sd_boot = TRUE,
  iv_threshold = 10,
  threshold_boot = TRUE,
  alpha = 0.05,
  intercept = TRUE,
  B = 300
)

```

## Arguments

Y observations of the outcome variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If outcome variable is binary use dummy encoding.



D	observations of the treatment variable. Either a numeric vector of length n or a numeric matrix with dimension n by 1. If treatment variable is binary use dummy encoding.
Z	observations of the instrumental variable(s). Either a vector of length n or a matrix with dimension n by s. If observations are not numeric dummy encoding will be applied.
W	(transformed) observations of baseline covariate(s) used to fit the outcome model. Either a vector of length n or a matrix with dimension n by p_w or NULL (if no covariates should be included). If observations are not numeric dummy encoding will be applied.
vio_space	list with vectors of length n and/or matrices with n rows as elements to specify the violation space candidates. If observations are not numeric dummy encoding will be applied. See Details for more information.
create_nested_sequence	logical. If TRUE, the violation space candidates (in form of matrices) are defined sequentially starting with an empty violation matrix and subsequently adding the next element of vio_space to the current violation matrix. If FALSE, the violation space candidates (in form of matrices) are defined as the empty space and the elements of vio_space. See Details for more information.
weight	the hat matrix of the treatment model.
A1_ind	indices of the observations that will be used to fit the outcome model. Must be of same length as the number of rows and columns of weight. If NULL, all observations will be used.
sel_method	The selection method used to estimate the treatment effect. Either "comparison" or "conservative". See Details.
sd_boot	logical. if TRUE, it determines the standard error using a bootstrap approach.
iv_threshold	a numeric value specifying the minimum of the threshold of IV strength test.
threshold_boot	logical. if TRUE, it determines the threshold of the IV strength using a bootstrap approach. If FALSE, it does not perform a bootstrap. See Details.
alpha	the significance level. Has to be a numeric value between 0 and 1.
intercept	logical. If TRUE, an intercept is included in the outcome model.
B	number of bootstrap samples. Has to be a positive integer value. Bootstrap methods are used to calculate the iv strength threshold if threshold_boot is TRUE and for the violation space selection.

## Details

The treatment and outcome models are assumed to be of the following forms:

$$D_i = f(Z_i, X_i) + \delta_i$$

$$Y_i = \beta \cdot D_i + h(Z_i, X_i) + \phi(X_i) + \epsilon_i$$

where  $f(Z_i, X_i)$  is estimated using a random forest,  $h(Z_i, X_i)$  is approximated using the hat matrix weight provided by the user and  $\phi(X_i)$  is approximated by a linear combination of the columns in W. The errors are allowed to be heteroscedastic. A1 is used to perform violation space selection and

to estimate the treatment effect.

The violation space candidates should be in a nested sequence as the violation space selection is performed by comparing the treatment estimate obtained by each violation space candidate with the estimates of all violation space candidates further down the list `vio_space` that provide enough IV strength. Only if no significant difference was found in all of those comparisons, the violation space candidate will be selected. If `sel_method` is 'comparison', the treatment effect estimate of this violation space candidate will be returned. If `sel_method` is 'conservative', the treatment effect estimate of the successive violation space candidate will be returned provided that the IV strength is large enough. The specification of suitable violation space candidates is a crucial step because a poor approximation of  $g(Z_i, X_i)$  might not address the bias caused by the violation of the IV assumption sufficiently well. The function `create_monomials` can be used to create a predefined sequence of violation space candidates consisting of monomials. The function `create_interactions` can be used to create a predefined sequence of violation space candidates consisting of two-way interactions between the instruments themselves and between the instruments and the instruments and baseline covariates.

The instrumental variable(s) are considered strong enough for violation space candidate  $V_q$  if the estimated IV strength using this violation space candidate is larger than the obtained value of the threshold of the IV strength. The formula of the threshold of the IV strength has the form  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\} + S(V_q), 40\}$  if `threshold_boot` is TRUE, and  $\min\{\max\{2 \cdot \text{Trace}[M(V_q)], \text{iv\_threshold}\}, 40\}$  if `threshold_boot` is FALSE. The matrix  $M(V_q)$  depends on the hat matrix obtained from estimating  $f(Z_i, X_i)$ , the violation space candidate  $V_q$  and the variables to include in the outcome model  $w$ .  $S(V_q)$  is obtained using a bootstrap and aims to adjust for the estimation error of the IV strength. Usually, the value of the threshold of the IV strength obtained using the bootstrap approach is larger. Thus, using `threshold_boot` equals TRUE leads to a more conservative IV strength test. For more information see subsection 3.3 in Guo and Buehlmann (2022).

See also Carl et al. (2023) for more details.

## Value

A list containing the following elements:

`Coef_all` a series of point estimates of the treatment effect obtained by the different violation space candidates.

`sd_all` standard errors of the estimates of the treatment effect obtained by the different violation space candidates.

`pval_all` p-values of the treatment effect estimates obtained by the different violation space candidates.

`CI_all` confidence intervals for the treatment effect obtained by the different violation space candidates.

`Coef_sel` the point estimator of the treatment effect obtained by the selected violation space candidate(s).

`sd_sel` the standard error of `Coef_sel`.

`pval_sel` p-value of the treatment effect estimate obtained by the selected violation space candidate(s).

- `CI_sel` confidence interval for the treatment effect obtained by the selected violation space candidate(s).
- `iv_str` IV strength using the different violation space candidates.
- `iv_thol` the threshold for the IV strength using the different violation space candidates.
- `Qmax` the violation space candidate that was the largest violation space candidate for which the IV strength was considered large enough determined by the IV strength test. If 0, the IV Strength test failed for the first violation space candidate. Otherwise, violation space selection was performed.
- `q_comp` the violation space candidate that was selected by the comparison method over the multiple data splits.
- `q_cons` the violation space candidate that was selected by the conservative method over the multiple data splits.
- `invalidity` shows whether the instrumental variable(s) were considered valid, invalid or too weak to test for violations. The instrumental variables are considered too weak to test for violations if the IV strength is already too weak using the first violation space candidate (besides the empty violation space). Testing for violations is always performed by using the comparison method.

## References

- Zijian Guo, and Peter Buehlmann. Two Stage Curvature Identification with Machine Learning: Causal Inference with Possibly Invalid Instrumental Variables. *arXiv:2203.12808*, 2022
- Nicolai Meinshausen, Lukas Meier, and Peter Buehlmann. P-values for high-dimensional regression. *Journal of the American Statistical Association*, 104(488):1671-1681, 2009. 16, 18
- Victor Chernozhukov, Denis Chetverikov, Mert Demirer, Esther Duflo, Christian Hansen, Whitney Newey, and James Robins. Double/debiased machine learning for treatment and structural parameters: Double/debiased machine learning. *The Econometrics Journal*, 21(1), 2018. 4, 16, 18
- David Carl, Corinne Emmenegger, Peter Buehlmann, and Zijian Guo. TSCI: two stage curvature identification for causal inference with invalid instruments. *arXiv:2304.00513*, 2023

## See Also

[tsci\\_boosting](#) for TSCI with boosting.

[tsci\\_forest](#) for TSCI with random forest.

[tsci\\_poly](#) for TSCI with polynomial basis expansion.

## Examples

```
### a small example without baseline covariates
if (require("MASS")) {
  # sample size
```



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