

# Package ‘SoftClustering’

January 20, 2025

**Type** Package

**Title** Soft Clustering Algorithms

**Description** It contains soft clustering algorithms, in particular approaches derived from rough set theory: Lingras & West original rough k-means, Peters' refined rough k-means, and PI rough k-means. It also contains classic k-means and a corresponding illustrative demo.

**Version** 2.1.3

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**Depends** R (>= 4.1)

**License** GPL-2

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.2.3

**NeedsCompilation** no

**Repository** CRAN

**Date/Publication** 2023-08-18 07:52:35 UTC

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createLowerMShipMatrix  
*Create Lower Approximation*

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### Description

Creates a lower approximation out of an upper approximation.

### Usage

```
createLowerMShipMatrix(upperMShipMatrix)
```

### Arguments

upperMShipMatrix  
An upper approximation matrix.

### Value

Returns the corresponding lower approximation.

### Author(s)

G. Peters.

---

datatypeInteger      *Rough k-Means Plotting*

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### Description

Checks for integer.

### Usage

```
datatypeInteger(x)
```

### Arguments

x      As a replacement for is.integer(). is.integer() delivers FALSE when the variable is numeric (as superset for integer etc.)

**Value**

TRUE if x is integer otherwise FALSE.

**Author(s)**

G. Peters.

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DemoDataC2D2a	<i>A small two-dimensional dataset with two clusters for demonstration purposes. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().</i>
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**Description**

A small two-dimensional dataset with two clusters for demonstration purposes. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().

**Usage**

```
data(DemoDataC2D2a)
```

**Format**

Rows: objects, columns: features

**Examples**

```
data(DemoDataC2D2a)
```

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HardKMeans	<i>Hard k-Means</i>
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**Description**

HardKMeans performs classic (hard) k-means.

**Usage**

```
HardKMeans(dataMatrix, meansMatrix, nClusters, maxIterations)
```

**Arguments**

<code>dataMatrix</code>	Matrix with the objects to be clustered. Dimension: [nObjects x nFeatures].
<code>meansMatrix</code>	Select means derived from 1 = random (unity interval), 2 = maximum distances, matrix [nClusters x nFeatures] = self-defined means. Default: 2 = maximum distances.
<code>nClusters</code>	Number of clusters: Integer in [2, nObjects). Note, nCluster must be set even when meansMatrix is a matrix. For transparency, nClusters will not be overridden by the number of clusters derived from meansMatrix. Default: nClusters=2.
<code>maxIterations</code>	Maximum number of iterations. Default: maxIterations=100.

**Value**

`$upperApprox`: Obtained upper approximations [nObjects x nClusters]. Note: Apply function `createLowerMShipMatrix()` to obtain lower approximations; and for the boundary: `boundary = upperApprox - lowerApprox`.

`$clusterMeans`: Obtained means [nClusters x nFeatures].

`$nIterations`: Number of iterations.

**Author(s)**

M. Goetz, G. Peters, Y. Richter, D. Sacker, T. Wochinger.

**References**

Lloyd, S.P. (1982) Least squares quantization in PCM. *IEEE Transactions on Information Theory* **28**, 128–137. <doi:10.1016/j.ijar.2012.10.003>.

Peters, G.; Crespo, F.; Lingras, P. and Weber, R. (2013) Soft clustering – fuzzy and rough approaches and their extensions and derivatives. *International Journal of Approximate Reasoning* **54**, 307–322. <doi:10.1016/j.ijar.2012.10.003>.

**Examples**

```
# An illustrative example clustering the sample data set DemoDataC2D2a.txt
HardKMeans(DemoDataC2D2a, 2, 2, 100)
```

---

HardKMeansDemo

*Hard k-Means Demo*

---

**Description**

HardKMeansDemo shows how hard k-means performs stepwise. The number of features is set to 2 and the maximum number of iterations is 100.

**Usage**

```
HardKMeansDemo(dataMatrix, meansMatrix, nClusters)
```

**Arguments**

dataMatrix	Matrix with the objects to be clustered. Dimension: [nObjects x nFeatures]. Default: no default set.
meansMatrix	Select means derived from 1 = random (unity interval), 2 = maximum distances, matrix [nClusters x nFeatures=2] = self-defined means. Default: meansMatrix=1 (random).
nClusters	Number of clusters: Integer in [2, min(5, nObjects-1)]. Note, nCluster must be set even when meansMatrix is a matrix. For transparency, nClusters will not be overridden by the number of clusters derived from meansMatrix. Default: nClusters=2.

**Value**

None.

**Author(s)**

G. Peters.

**References**

Lloyd, S.P. (1982) Least squares quantization in PCM. *IEEE Transactions on Information Theory* **28**, 128–137. <doi:10.1016/j.ijar.2012.10.003>.

Peters, G.; Crespo, F.; Lingras, P. and Weber, R. (2013) Soft clustering – fuzzy and rough approaches and their extensions and derivatives. *International Journal of Approximate Reasoning* **54**, 307–322. <doi:10.1016/j.ijar.2012.10.003>.

**Examples**

```
# Clustering the data set DemoDataC2D2a.txt (nClusters=2, random initial means)
HardKMeansDemo(DemoDataC2D2a,1,2)
# Clustering the data set DemoDataC2D2a.txt (nClusters=2,3,4; initially set means)
HardKMeansDemo(DemoDataC2D2a,initMeansC2D2a,2)
HardKMeansDemo(DemoDataC2D2a,initMeansC3D2a,3)
HardKMeansDemo(DemoDataC2D2a,initMeansC4D2a,4)
# Clustering the data set DemoDataC2D2a.txt (nClusters=5, initially set means)
# It leads to an empty cluster: a (rare) case for an abnormal termination of k-means.
HardKMeansDemo(DemoDataC2D2a,initMeansC5D2a,5)
```

---

initializeMeansMatrix *Initialize Means Matrix*

---

**Description**

initializeMeansMatrix delivers an initial means matrix.

**Usage**

```
initializeMeansMatrix(dataMatrix, nClusters, meansMatrix)
```

**Arguments**

dataMatrix	Matrix with the objects as basis for the means matrix.
nClusters	Number of clusters.
meansMatrix	Select means derived from 1 = random (unity interval), 2 = maximum distances, matrix [nClusters x nFeatures] = self-defined means (will be returned unchanged). Default: 2 = maximum distances.

**Value**

Initial means matrix [nClusters x nFeatures].

**Author(s)**

M. Goetz, G. Peters, Y. Richter, D. Sacker, T. Wochinger.

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initMeansC2D2a	<i>Two-dimensional dataset with two initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().</i>
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**Description**

Two-dimensional dataset with two initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().

**Usage**

```
data(initMeansC2D2a)
```

**Format**

Rows: objects, columns: features

**Examples**

```
data(initMeansC2D2a)
```

---

initMeansC3D2a	<i>Two-dimensional dataset with three initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().</i>
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**Description**

Two-dimensional dataset with three initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().

**Usage**

```
data(initMeansC3D2a)
```

**Format**

Rows: objects, columns: features

**Examples**

```
data(initMeansC3D2a)
```

---

initMeansC4D2a	<i>Two-dimensional dataset with four initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().</i>
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**Description**

Two-dimensional dataset with four initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().

**Usage**

```
data(initMeansC4D2a)
```

**Format**

Rows: objects, columns: features

**Examples**

```
data(initMeansC4D2a)
```

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initMeansC5D2a	<i>Two-dimensional dataset with five initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().</i>
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**Description**

Two-dimensional dataset with five initial cluster means for the dataset DemoDataC2D2a. See examples in the Help/Description of a function, e.g. for HardKMeansDemo().

**Usage**

```
data(initMeansC5D2a)
```

**Format**

Rows: objects, columns: features

**Examples**

```
data(initMeansC5D2a)
```

---

normalizeMatrix	<i>Matrix Normalization</i>
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**Description**

normalizeMatrix delivers a normalized matrix.

**Usage**

```
normalizeMatrix(dataMatrix, normMethod, bycol)
```

**Arguments**

dataMatrix	Matrix with the objects to be normalized.
normMethod	1 = unity interval, 2 = normal distribution (sample variance), 3 = normal distribution (population variance). Any other value returns the matrix unchanged. Default: meansMatrix = 1 (unity interval).
bycol	TRUE = columns are normalized, i.e., each column is considered separately (e.g., in case of the unity interval and a column colA: max(colA)=1 and min(colA)=0). For bycol = FALSE rows are normalized. Default: bycol = TRUE (columns are normalized).

**Value**

Normalized matrix.

**Author(s)**

M. Goetz, G. Peters, Y. Richter, D. Sacker, T. Wochinger.

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plotRoughKMeans	<i>Rough k-Means Plotting</i>
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**Description**

plotRoughKMeans plots the rough clustering results in 2D. Note: Plotting is limited to a maximum of 5 clusters.

**Usage**

```
plotRoughKMeans(dataMatrix, upperMShipMatrix, meansMatrix, plotDimensions, colouredPlot)
```

**Arguments**

`dataMatrix` Matrix with the objects to be plotted.

`upperMShipMatrix` Corresponding matrix with upper approximations.

`meansMatrix` Corresponding means matrix.

`plotDimensions` An integer vector of the length 2. Defines the to be plotted feature dimensions, i.e.,  $\max(\text{plotDimensions} = c(1:2)) \leq n\text{Features}$ . Default: `plotDimensions = c(1:2)`.

`colouredPlot` Select TRUE = colouredPlot plot, FALSE = black/white plot.

**Value**

2D-plot of clustering results. The boundary objects are represented by stars (\*).

**Author(s)**

G. Peters.

RoughKMeans\_LW

*Lingras & West's Rough k-Means***Description**

RoughKMeans\_LW performs Lingras & West's k-means clustering algorithm. The commonly accepted relative threshold is applied.

**Usage**

```
RoughKMeans_LW(dataMatrix, meansMatrix, nClusters, maxIterations, threshold, weightLower)
```

**Arguments**

dataMatrix	Matrix with the objects to be clustered. Dimension: [nObjects x nFeatures].
meansMatrix	Select means derived from 1 = random (unity interval), 2 = maximum distances, matrix [nClusters x nFeatures] = self-defined means. Default: 2 = maximum distances.
nClusters	Number of clusters: Integer in [2, nObjects). Note, nCluster must be set even when meansMatrix is a matrix. For transparency, nClusters will not be overridden by the number of clusters derived from meansMatrix. Default: nClusters=2.
maxIterations	Maximum number of iterations. Default: maxIterations=100.
threshold	Relative threshold in rough k-means algorithms (threshold >= 1.0). Default: threshold = 1.5.
weightLower	Weight of the lower approximation in rough k-means algorithms (0.0 <= weightLower <= 1.0). Default: weightLower = 0.7.

**Value**

\$upperApprox: Obtained upper approximations [nObjects x nClusters]. Note: Apply function createLowerMShipMatrix() to obtain lower approximations; and for the boundary: boundary = upperApprox - lowerApprox.

\$clusterMeans: Obtained means [nClusters x nFeatures].

\$nIterations: Number of iterations.

**Author(s)**

M. Goetz, G. Peters, Y. Richter, D. Sacker, T. Wochinger.

**References**

Lingras, P. and West, C. (2004) Interval Set Clustering of web users with rough k-means. *Journal of Intelligent Information Systems* **23**, 5–16. <doi:10.1023/b:jiis.0000029668.88665.1a>.

Peters, G. (2006) Some refinements of rough k-means clustering. *Pattern Recognition* **39**, 1481–1491. <doi:10.1016/j.patcog.2006.02.002>.

Lingras, P. and Peters, G. (2011) Rough Clustering. *WIREs Data Mining and Knowledge Discovery* **1**, 64–72. <doi:10.1002/widm.16>.

Lingras, P. and Peters, G. (2012) Applying rough set concepts to clustering. In: Peters, G.; Lingras, P.; Slezak, D. and Yao, Y. Y. (Eds.) *Rough Sets: Selected Methods and Applications in Management and Engineering*, Springer, 23–37. <doi:10.1007/978-1-4471-2760-4\_2>.

Peters, G.; Crespo, F.; Lingras, P. and Weber, R. (2013) Soft clustering – fuzzy and rough approaches and their extensions and derivatives. *International Journal of Approximate Reasoning* **54**, 307–322. <doi:10.1016/j.ijar.2012.10.003>.

Peters, G. (2014) Rough clustering utilizing the principle of indifference. *Information Sciences* **277**, 358–374. <doi:10.1016/j.ins.2014.02.073>.

Peters, G. (2015) Is there any need for rough clustering? *Pattern Recognition Letters* **53**, 31–37. <doi:10.1016/j.patrec.2014.11.003>.

## Examples

```
# An illustrative example clustering the sample data set DemoDataC2D2a.txt
RoughKMeans_LW(DemoDataC2D2a, 2, 2, 100, 1.5, 0.7)
```

---

RoughKMeans\_PE

*Peters' Rough k-Means*

---

## Description

RoughKMeans\_PE performs Peters' k-means clustering algorithm.

## Usage

```
RoughKMeans_PE(dataMatrix, meansMatrix, nClusters, maxIterations, threshold, weightLower)
```

## Arguments

dataMatrix	Matrix with the objects to be clustered. Dimension: [nObjects x nFeatures].
meansMatrix	Select means derived from 1 = random (unity interval), 2 = maximum distances, matrix [nClusters x nFeatures] = self-defined means. Default: 2 = maximum distances.
nClusters	Number of clusters: Integer in [2, nObjects). Note, nCluster must be set even when meansMatrix is a matrix. For transparency, nClusters will not be overridden by the number of clusters derived from meansMatrix. Default: nClusters=2.
maxIterations	Maximum number of iterations. Default: maxIterations=100.
threshold	Relative threshold in rough k-means algorithms (threshold >= 1.0). Default: threshold = 1.5.
weightLower	Weight of the lower approximation in rough k-means algorithms (0.0 <= weightLower <= 1.0). Default: weightLower = 0.7.

**Value**

\$upperApprox: Obtained upper approximations [nObjects x nClusters]. Note: Apply function createLowerMShipMatrix() to obtain lower approximations; and for the boundary: boundary = upperApprox - lowerApprox.

\$clusterMeans: Obtained means [nClusters x nFeatures].

\$nIterations: Number of iterations.

**Author(s)**

M. Goetz, G. Peters, Y. Richter, D. Sacker, T. Wochinger.

**References**

Peters, G. (2006) Some refinements of rough k-means clustering. *Pattern Recognition* **39**, 1481–1491. <doi:10.1016/j.patcog.2006.02.002>.

Peters, G.; Crespo, F.; Lingras, P. and Weber, R. (2013) Soft clustering – fuzzy and rough approaches and their extensions and derivatives. *International Journal of Approximate Reasoning* **54**, 307–322. <doi:10.1016/j.ijar.2012.10.003>.

Peters, G. (2014) Rough clustering utilizing the principle of indifference. *Information Sciences* **277**, 358–374. <doi:10.1016/j.ins.2014.02.073>.

Peters, G. (2015) Is there any need for rough clustering? *Pattern Recognition Letters* **53**, 31–37. <doi:10.1016/j.patrec.2014.11.003>.

**Examples**

```
# An illustrative example clustering the sample data set DemoDataC2D2a.txt
RoughKMeans_PE(DemoDataC2D2a, 2, 2, 100, 1.5, 0.7)
```

---

RoughKMeans\_PI

PI *Rough k-Means*

---

**Description**

RoughKMeans\_PI performs pi k-means clustering algorithm in its standard case. Therefore, weights are not required.

**Usage**

```
RoughKMeans_PI(dataMatrix, meansMatrix, nClusters, maxIterations, threshold)
```

**Arguments**

<code>dataMatrix</code>	Matrix with the objects to be clustered. Dimension: [nObjects x nFeatures].
<code>meansMatrix</code>	Select means derived from 1 = random (unity interval), 2 = maximum distances, matrix [nClusters x nFeatures] = self-defined means. Default: 2 = maximum distances.
<code>nClusters</code>	Number of clusters: Integer in [2, nObjects). Note, nCluster must be set even when meansMatrix is a matrix. For transparency, nClusters will not be overridden by the number of clusters derived from meansMatrix. Default: nClusters=2.
<code>maxIterations</code>	Maximum number of iterations. Default: maxIterations=100.
<code>threshold</code>	Relative threshold in rough k-means algorithms (threshold >= 1.0). Default: threshold = 1.5.

**Value**

`$upperApprox`: Obtained upper approximations [nObjects x nClusters]. Note: Apply function `createLowerMSHIPMatrix()` to obtain lower approximations; and for the boundary: `boundary = upperApprox - lowerApprox`.

`$clusterMeans`: Obtained means [nClusters x nFeatures].

`$nIterations`: Number of iterations.

**Author(s)**

M. Goetz, G. Peters, Y. Richter, D. Sacker, T. Wochinger.

**References**

Peters, G. (2006) Some refinements of rough k-means clustering. *Pattern Recognition* **39**, 1481–1491. <doi:10.1016/j.patcog.2006.02.002>.

Peters, G.; Crespo, F.; Lingras, P. and Weber, R. (2013) Soft clustering – fuzzy and rough approaches and their extensions and derivatives. *International Journal of Approximate Reasoning* **54**, 307–322. <doi:10.1016/j.ijar.2012.10.003>.

Peters, G. (2014) Rough clustering utilizing the principle of indifference. *Information Sciences* **277**, 358–374. <doi:10.1016/j.ins.2014.02.073>.

Peters, G. (2015) Is there any need for rough clustering? *Pattern Recognition Letters* **53**, 31–37. <doi:10.1016/j.patrec.2014.11.003>.

**Examples**

```
# An illustrative example clustering the sample data set DemoDataC2D2a.txt
RoughKMeans_PI(DemoDataC2D2a, 2, 2, 100, 1.5)
```

---

RoughKMeans\_SHELL      *Rough k-Means Shell*

---

### Description

RoughKMeans\_SHELL performs rough k-means algorithms with options for normalization and a 2D-plot of the results.

### Usage

```
RoughKMeans_SHELL(clusterAlgorithm, dataMatrix, meansMatrix, nClusters,
                    normalizationMethod, maxIterations, plotDimensions,
                    colouredPlot, threshold, weightLower)
```

### Arguments

clusterAlgorithm	Select 0 = classic k-means, 1 = Lingras & West's rough k-means, 2 = Peters' rough k-means, 3 = $\pi$ rough k-means. Default: clusterAlgorithm = 3 ( $\pi$ rough k-means).
dataMatrix	Matrix with the objects to be clustered. Dimension: [nObjects x nFeatures].
meansMatrix	Select means derived from 1 = random (unity interval), 2 = maximum distances, matrix [nClusters x nFeatures] = self-defined means. Default: 2 = maximum distances.
nClusters	Number of clusters: Integer in [2, nObjects). Note, nCluster must be set even when meansMatrix is a matrix. For transparency, nClusters will not be overridden by the number of clusters derived from meansMatrix. Default: nClusters=2. Note: Plotting is limited to a maximum of 5 clusters.
normalizationMethod	1 = unity interval, 2 = normal distribution (sample variance), 3 = normal distribution (population variance). Any other value returns the matrix unchanged. Default: meansMatrix = 1 (unity interval).
maxIterations	Maximum number of iterations. Default: maxIterations=100.
plotDimensions	An integer vector of the length 2. Defines the to be plotted feature dimensions, i.e., $\max(\text{plotDimensions} = c(1:2)) \leq n\text{Features}$ . Default: plotDimensions = c(1:2).
colouredPlot	Select TRUE = colouredPlot plot, FALSE = black/white plot.
threshold	Relative threshold in rough k-means algorithms (threshold $\geq 1.0$ ). Default: threshold = 1.5. Note: It can be ignored for classic k-means.
weightLower	Weight of the lower approximation in rough k-means algorithms ( $0.0 \leq \text{weightLower} \leq 1.0$ ). Default: weightLower = 0.7. Note: It can be ignored for classic k-means and $\pi$ rough k-means

**Value**

2D-plot of clustering results. The boundary objects are represented by stars (\*).

\$upperApprox: Obtained upper approximations [nObjects x nClusters]. Note: Apply function createLowerMShipMatrix() to obtain lower approximations; and for the boundary: boundary = upperApprox - lowerApprox.

\$clusterMeans: Obtained means [nClusters x nFeatures].

\$nIterations: Number of iterations.

**Author(s)**

M. Goetz, G. Peters, Y. Richter, D. Sacker, T. Wochinger.

**References**

Lloyd, S.P. (1982) Least squares quantization in PCM. *IEEE Transactions on Information Theory* **28**, 128–137. <doi:10.1016/j.ijar.2012.10.003>.

Lingras, P. and West, C. (2004) Interval Set Clustering of web users with rough k-means. *Journal of Intelligent Information Systems* **23**, 5–16. <doi:10.1023/b:jiis.0000029668.88665.1a>.

Peters, G. (2006) Some refinements of rough k-means clustering. *Pattern Recognition* **39**, 1481–1491. <doi:10.1016/j.patcog.2006.02.002>.

Lingras, P. and Peters, G. (2011) Rough Clustering. *WIREs Data Mining and Knowledge Discovery* **1**, 64–72. <doi:10.1002/widm.16>.

Lingras, P. and Peters, G. (2012) Applying rough set concepts to clustering. In: Peters, G.; Lingras, P.; Slezak, D. and Yao, Y. Y. (Eds.) *Rough Sets: Selected Methods and Applications in Management and Engineering*, Springer, 23–37. <doi:10.1007/978-1-4471-2760-4\_2>.

Peters, G.; Crespo, F.; Lingras, P. and Weber, R. (2013) Soft clustering – fuzzy and rough approaches and their extensions and derivatives. *International Journal of Approximate Reasoning* **54**, 307–322. <doi:10.1016/j.ijar.2012.10.003>.

Peters, G. (2014) Rough clustering utilizing the principle of indifference. *Information Sciences* **277**, 358–374. <doi:10.1016/j.ins.2014.02.073>.

Peters, G. (2015) Is there any need for rough clustering? *Pattern Recognition Letters* **53**, 31–37. <doi:10.1016/j.patrec.2014.11.003>.

**Examples**

```
# An illustrative example clustering the sample data set DemoDataC2D2a.txt
RoughKMeans_SHELL(3, DemoDataC2D2a, 2, 2, 1, 100, c(1:2), TRUE, 1.5, 0.7)
```

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