

Package ‘tectonic’

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Title Analyzing the Orientation of Maximum Horizontal Stress

Version 0.4.6

Description Models the direction of the maximum horizontal stress using relative plate motion parameters. Statistical algorithms to evaluate the modeling results compared with the observed data. Provides plots to visualize the results. Methods described in Stephan et al. (2023) <[doi:10.1038/s41598-023-42433-2](https://doi.org/10.1038/s41598-023-42433-2)> and Wdowinski (1998) <[doi:10.1016/S0079-1946\(98\)00091-3](https://doi.org/10.1016/S0079-1946(98)00091-3)>.

License GPL (>= 3)

URL <https://tobiste.github.io/tectonic/>

BugReports <https://github.com/tobiste/tectonic/issues>

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abs_vel	<i>Absolute Plate Velocity</i>
---------	--------------------------------

Description

Calculates the absolute angular velocity of plate motion

Usage

```
abs_vel(w, alpha, r = earth_radius())
```

Arguments

w	Angular velocity or rate or angle of rotation
alpha	Angular distance to Euler pole or small circle around Euler pole
r	Radius. Default is WGS84 Earth's radius (6371.009 km)

Value

numeric (unit of velocity: km/Myr)

See Also

[earth_radius\(\)](#)

Examples

```
abs_vel(0.21, 0)
abs_vel(0.21, 45)
abs_vel(0.21, 90)
```

angle-conversion *Degrees to Radians*

Description

Helper functions to transform between angles in degrees and radians.

Usage

```
rad2deg(rad)
```

```
deg2rad(deg)
```

Arguments

rad	(array of) angles in radians.
deg	(array of) angles in degrees.

Value

numeric. angle in degrees or radians.

Examples

```
deg2rad(seq(-90, 90, 15))
rad2deg(seq(-pi / 2, pi / 2, length = 13))
```

angle_vectors	<i>Angle Between Two Vectors</i>
---------------	----------------------------------

Description

Calculates the angle between two vectors

Usage

```
angle_vectors(x, y)
```

Arguments

x, y	Vectors in Cartesian coordinates. Can be vectors of three numbers or a matrix of 3 columns (x, y, z)
------	--

Value

numeric. angle in degrees

Examples

```
u <- c(1, -2, 3)
v <- c(-2, 1, 1)
angle_vectors(u, v)
```

axes	<i>Plot axes</i>
------	------------------

Description

Show direction axes in a map

Usage

```
axes(
  x,
  y,
  angle,
  radius = 0.5,
  arrow.code = 1,
  arrow.length = 0,
  add = FALSE,
  ...
)
```

Arguments

<code>x, y</code>	coordinates of points
<code>angle</code>	Azimuth in degrees
<code>radius</code>	length of axis
<code>arrow.code</code>	integer. Kind of arrow head. The default is 1, i.e. no arrow head. See <code>graphics::arrows()</code> for details
<code>arrow.length</code>	numeric Length of the edges of the arrow head (in inches). (Ignored if <code>arrow.code = 1</code>)
<code>add</code>	logical. add to existing plot?
<code>...</code>	optional arguments passed to <code>graphics::arrows()</code>

Value

No return value, called for side effects

Examples

```
data("san_andreas")
axes(san_andreas$lon, san_andreas$lat, san_andreas$azi, add = FALSE)
```

circle_mean_diff	<i>Circular Mean Difference</i>
------------------	---------------------------------

Description

Circular Mean Difference

Usage

```
circular_mean_difference(x, w = NULL, axial = TRUE, na.rm = TRUE)
```

```
circular_mean_difference_alt(x, w = NULL, axial = TRUE, na.rm = TRUE)
```

Arguments

<code>x</code>	numeric vector. Values in degrees.
<code>w</code>	(optional) Weights. A vector of positive numbers and of the same length as <code>x</code> .
<code>axial</code>	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
<code>na.rm</code>	logical value indicating whether NA values in <code>x</code> should be stripped before the computation proceeds.

Value

numeric

References

Mardia, K.V., and Jupp, P.E (1999). Directional Statistics, Wiley Series in Probability and Statistics. John Wiley & Sons, Inc., Hoboken, NJ, USA. doi:10.1002/9780470316979

Examples

```
data("san_andreas")
circular_mean_difference(san_andreas$azi)
circular_mean_difference(san_andreas$azi, 1 / san_andreas$unc)

circular_mean_difference_alt(san_andreas$azi)
circular_mean_difference_alt(san_andreas$azi, 1 / san_andreas$unc)
```

circle_stats

Summary Statistics of Circular Data

Description

Calculate the (weighted median) and standard deviation of orientation data.

Usage

```
circular_mean(x, w = NULL, axial = TRUE, na.rm = TRUE)
circular_var(x, w = NULL, axial = TRUE, na.rm = TRUE)
circular_sd(x, w = NULL, axial = TRUE, na.rm = TRUE)
circular_median(x, w = NULL, axial = TRUE, na.rm = TRUE)
circular_quantiles(x, w = NULL, axial = TRUE, na.rm = TRUE)
circular_IQR(x, w = NULL, axial = TRUE, na.rm = TRUE)
sample_circular_dispersion(x, w = NULL, axial = TRUE, na.rm = TRUE)
```

Arguments

x	numeric vector. Values in degrees.
w	(optional) Weights. A vector of positive numbers and of the same length as x.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Value

numeric vector

Note

Weighting may be the reciprocal of the data uncertainties.

Weightings have no effect on quasi-median and quasi-quantiles if `length(x) %% 2 != 1` and `length(x) %% 4 == 0`, respectively.

References

Mardia, K.V. (1972). *Statistics of Directional Data: Probability and Mathematical Statistics*. London: Academic Press.

Mardia, K.V., and Jupp, P.E (1999). *Directional Statistics*, Wiley Series in Probability and Statistics. John Wiley & Sons, Inc., Hoboken, NJ, USA. [doi:10.1002/9780470316979](https://doi.org/10.1002/9780470316979)

Ziegler, M. O.; Heidbach O. (2019). *Manual of the Matlab Script Stress2Grid v1.1. WSM Technical Report 19-02*, GFZ German Research Centre for Geosciences. [doi:10.2312/wsm.2019.002](https://doi.org/10.2312/wsm.2019.002)

Heidbach, O., Tingay, M., Barth, A., Reinecker, J., Kurfess, D., & Mueller, B. (2010). Global crustal stress pattern based on the World Stress Map database release 2008. *Tectonophysics* **482**, 3<U+2013>15, [doi:10.1016/j.tecto.2009.07.023](https://doi.org/10.1016/j.tecto.2009.07.023)

Examples

```
set.seed(1)
x <- rvm(10, 0, 100) %% 180
unc <- stats::runif(100, 0, 10)
circular_mean(x, 1 / unc)
circular_var(x, 1 / unc)
sample_circular_dispersion(x, 1 / unc)
circular_sd(x, 1 / unc)
circular_median(x, 1 / unc)
circular_quantiles(x, 1 / unc)
circular_IQR(x, 1 / unc)

data("san_andreas")
circular_mean(san_andreas$azi)
circular_mean(san_andreas$azi, 1 / san_andreas$unc)
circular_median(san_andreas$azi)
circular_median(san_andreas$azi, 1 / san_andreas$unc)
circular_quantiles(san_andreas$azi)
circular_quantiles(san_andreas$azi, 1 / san_andreas$unc)
circular_var(san_andreas$azi)
circular_var(san_andreas$azi, 1 / san_andreas$unc)
sample_circular_dispersion(san_andreas$azi, 1 / san_andreas$unc)

data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
circular_mean(sa.por$azi.PoR, 1 / san_andreas$unc)
circular_median(sa.por$azi.PoR, 1 / san_andreas$unc)
```



```
circular_var(sa.por$azi.PoR, 1 / san_andreas$unc)
sample_circular_dispersion(sa.por$azi.PoR, 1 / san_andreas$unc)
circular_quantiles(sa.por$azi.PoR, 1 / san_andreas$unc)
```

circular_dispersion_boot

Bootstrapped Estimates for Circular Dispersion

Description

Calculates bootstrapped estimates of the circular dispersion, its standard error and its confidence interval.

Usage

```
circular_dispersion_boot(
  x,
  y = NULL,
  w = NULL,
  w.y = NULL,
  R = 1000,
  conf.level = 0.95,
  ...
)
```

Arguments

x	numeric values in degrees.
y	numeric. The angle(s) about which the angles x disperse (in degrees).
w, w.y	(optional) Weights for x and y, respectively. A vector of positive numbers and of the same length as x.
R	The number of bootstrap replicates. positive integer (1000 by default).
conf.level	Level of confidence: $(1 - \alpha\%)/100$. (0.95 by default).
...	optional arguments passed to boot::boot()

Value

list containing:

MLE the maximum likelihood estimate of the circular dispersion

sde standard error of MLE

CI lower and upper limit of the confidence interval of MLE

See Also

[circular_dispersion\(\)](#)

Examples

```

data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
circular_dispersion(sa.por$azi.PoR, y = 135, w = 1 / san_andreas$unc)
circular_dispersion_boot(sa.por$azi.PoR, y = 135, w = 1 / san_andreas$unc, R = 1000)

```

circular_mode

Circular Mode

Description

MLE angle (maximum density) using a von Mises distribution kernel with specified concentration.

Usage

```
circular_mode(x, kappa = NULL, axial = TRUE, n = 512)
```

Arguments

x	numeric vector. Values in degrees.
kappa	von Mises distribution concentration parameter. Will be estimated using est.kappa() if not provided.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).#’ @param kappa
n	the number of equally spaced points at which the density is to be estimated.

Value

numeric

Examples

```

set.seed(1)
x <- rvm(10, 0, 100)
circular_mode(x, kappa = est.kappa(x))

```

circular_qqplot	<i>Quantile-Quantile Linearised Plot for Circular Distributions</i>
-----------------	---

Description

Uniformly distributed orientations should yield a straight line through the origin. Systematic departures from linearity will indicate preferred orientation.

Usage

```
circular_qqplot(  
  x,  
  axial = TRUE,  
  xlab = paste("i/(n+1)"),  
  ylab = NULL,  
  main = "Circular Quantile-Quantile Plot",  
  add_line = TRUE,  
  col = "#B63679FF",  
  ...  
)
```

Arguments

x	numeric. Angles in degrees
axial	Logical. Whether data are uniaxial (axial=FALSE)
xlab, ylab, main	plot labels.
add_line	logical. Whether to connect the points by straight lines?
col	color for the dots.
...	graphical parameters

Value

plot

References

Borradaile, G. J. (2003). Statistics of earth science data: their distribution in time, space, and orientation (Vol. 351, p. 329). Berlin: Springer.

Examples

```
# von Mises distribution  
x_vm <- rvm(100, mean = 0, kappa = 2)  
circular_qqplot(x_vm, pch = 20)  
  
x_norm <- rnorm(100, mean = 0, sd = 25)
```

```
circular_qqplot(x_norm, pch = 20)

# uniform (random) data
x_unif <- runif(100, 0, 360)
circular_qqplot(x_unif, pch = 20)
```

circular_range	<i>Circular Range</i>
----------------	-----------------------

Description

Length of the smallest arc which contains all the observations.

Usage

```
circular_range(x, axial = TRUE, na.rm = TRUE)
```

Arguments

x	numeric vector. Values in degrees.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Value

numeric. angle in degrees

References

Mardia, K.V., and Jupp, P.E (1999). Directional Statistics, Wiley Series in Probability and Statistics. John Wiley & Sons, Inc., Hoboken, NJ, USA. doi:[10.1002/9780470316979](https://doi.org/10.1002/9780470316979)

Examples

```
roulette <- c(43, 45, 52, 61, 75, 88, 88, 279, 357)
circular_range(roulette, axial = FALSE)

data("san_andreas")
circular_range(san_andreas$azi)
```

circular_sd_error *Standard Error of Mean Direction of Circular Data*

Description

Measure of the chance variation expected from sample to sample in estimates of the mean direction. It is a parametric estimate of the the circular standard error of the mean direction by the particular form of the standard error for the von Mises distribution. The approximated standard error of the mean direction is computed by the mean resultant length and the MLE concentration parameter κ .

Usage

```
circular_sd_error(x, w = NULL, axial = TRUE, na.rm = TRUE)
```

Arguments

x	numeric vector. Values in degrees.
w	(optional) Weights. A vector of positive numbers and of the same length as x.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Value

numeric

References

N.I. Fisher (1993) *Statistical Analysis of Circular Data*, Cambridge University Press.
 Davis (1986) *Statistics and data analysis in geology*. 2nd ed., John Wiley & Sons.

See Also

[mean_resultant_length\(\)](#), [circular_mean\(\)](#)

Examples

```
# Example data from Davis (1986), pp. 316
finland_stria <- c(
  23, 27, 53, 58, 64, 83, 85, 88, 93, 99, 100, 105, 113,
  113, 114, 117, 121, 123, 125, 126, 126, 126, 127, 127, 128, 128, 129, 132,
  132, 132, 134, 135, 137, 144, 145, 145, 146, 153, 155, 155, 155, 157, 163,
  165, 171, 172, 179, 181, 186, 190, 212
)
circular_sd_error(finland_stria, axial = FALSE)
```

```

data(san_andreas)
data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
circular_sd_error(sa.por$azi.PoR, w = 1 / san_andreas$unc)

```

circular_summary

Circular Summary Statistics

Description

Circular mean, standard deviation, variance, quasi-quantiles, mode, 95% confidence angle, standardized skewness and kurtosis

Usage

```
circular_summary(x, w = NULL, kappa = NULL, axial = TRUE, na.rm = FALSE)
```

Arguments

x	numeric vector. Values in degrees.
w	(optional) Weights. A vector of positive numbers and of the same length as x.
kappa	numeric. von Mises distribution concentration parameter used for the circular mode. Will be estimated using <code>est.kappa()</code> if not provided.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Value

named vector

See Also

[circular_mean\(\)](#), [circular_sd\(\)](#), [circular_var\(\)](#), [circular_quantiles\(\)](#), [confidence_angle\(\)](#), [second_central_moment\(\)](#), [circular_mode\(\)](#)

Examples

```

data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
circular_summary(sa.por$azi.PoR)
circular_summary(sa.por$azi.PoR, w = 1 / san_andreas$unc)

```

compact-grid

*Compact Smoothed Stress Field***Description**

Filter smoothed stress field containing a range of search radii or kernel half widths to find shortest wavelength (R) with the least circular sd. or dispersion (or any statistic) for each coordinate, respectively.

Usage

```
compact_grid(x, type = c("stress", "dispersion"))
```

```
compact_grid2(x, ..., FUN = min)
```

Arguments

x	output of stress2grid() , PoR_stress2grid() , stress2grid_stats() , or kernel_dispersion()
type	character. Type of the grid x. Either "stress" (when input is stress2grid() or PoR_stress2grid()) or "dispersion" (when input is kernel_dispersion()).
...	<tidy-select> One unquoted expression separated by commas. Variable names can be used as if they were positions in the data frame. Variable must be a column in x.
FUN	function is used to aggregate the data using the search radius R. Default is min() .

Value

sf object

See Also

[stress2grid\(\)](#), [PoR_stress2grid\(\)](#), [kernel_dispersion\(\)](#), [stress2grid_stats\(\)](#), [dplyr::dplyr_tidy_select\(\)](#)

Examples

```
data("san_andreas")
res <- stress2grid(san_andreas)
compact_grid(res)

## Not run:
res2 <- stress2grid_stats(san_andreas)
compact_grid2(res2, var, FUN = min)

## End(Not run)
```

confidence

Confidence Interval around the Mean Direction of Circular Data

Description

Probabilistic limit on the location of the true or population mean direction, assuming that the estimation errors are normally distributed.

Usage

```
confidence_angle(x, conf.level = 0.95, w = NULL, axial = TRUE, na.rm = TRUE)
```

```
confidence_interval(x, conf.level = 0.95, w = NULL, axial = TRUE, na.rm = TRUE)
```

Arguments

x	numeric vector. Values in degrees.
conf.level	Level of confidence: $(1 - \alpha\%)/100$. (0.95 by default).
w	(optional) Weights. A vector of positive numbers and of the same length as x.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Details

The confidence angle gives the interval, i.e. plus and minus the confidence angle, around the mean direction of a particular sample, that contains the true mean direction under a given level of confidence.

Value

Angle in degrees

References

- Davis (1986) Statistics and data analysis in geology. 2nd ed., John Wiley & Sons.
- Jammalamadaka, S. Rao and Sengupta, A. (2001). Topics in Circular Statistics, Sections 3.3.3 and 3.4.1, World Scientific Press, Singapore.

See Also

[mean_resultant_length\(\)](#), [circular_sd_error\(\)](#)

Examples

```
# Example data from Davis (1986), pp. 316
finland_stria <- c(
  23, 27, 53, 58, 64, 83, 85, 88, 93, 99, 100, 105, 113,
  113, 114, 117, 121, 123, 125, 126, 126, 126, 127, 127, 128, 128, 129, 132,
  132, 132, 134, 135, 137, 144, 145, 145, 146, 153, 155, 155, 155, 157, 163,
  165, 171, 172, 179, 181, 186, 190, 212
)
confidence_angle(finland_stria, axial = FALSE)
confidence_interval(finland_stria, axial = FALSE)

data(san_andreas)
data("nuvell1")
PoR <- subset(nuvell1, nuvell1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
confidence_angle(sa.por$azi.PoR, w = 1 / san_andreas$unc)
confidence_interval(sa.por$azi.PoR, w = 1 / san_andreas$unc)
```

confidence_interval_fisher

Confidence Interval around the Mean Direction of Circular Data after Fisher (1993)

Description

For large samples ($n \geq 25$) it performs a parametric estimate based on [sample_circular_dispersion\(\)](#). For smaller size samples, it returns a bootstrap estimate.

Usage

```
confidence_interval_fisher(
  x,
  conf.level = 0.95,
  w = NULL,
  axial = TRUE,
  na.rm = TRUE,
  boot = FALSE,
  R = 1000L,
  quiet = FALSE
)
```

Arguments

x	numeric vector. Values in degrees.
conf.level	Level of confidence: $(1 - \alpha\%)/100$. (0.95 by default).
w	(optional) Weights. A vector of positive numbers and of the same length as x.

axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.
boot	logical. Force bootstrap estimation
R	integer. number of bootstrap replicates
quiet	logical. Prints the used estimation (parametric or bootstrap).

Value

list

References

N.I. Fisher (1993) *Statistical Analysis of Circular Data*, Cambridge University Press.

Examples

```
# Example data from Davis (1986), pp. 316
finland_stria <- c(
  23, 27, 53, 58, 64, 83, 85, 88, 93, 99, 100, 105, 113,
  113, 114, 117, 121, 123, 125, 126, 126, 126, 127, 127, 128, 128, 129, 132,
  132, 132, 134, 135, 137, 144, 145, 145, 146, 153, 155, 155, 155, 157, 163,
  165, 171, 172, 179, 181, 186, 190, 212
)
confidence_interval_fisher(finland_stria, axial = FALSE)
confidence_interval_fisher(finland_stria, axial = FALSE, boot = TRUE)

data(san_andreas)
data("nuvell1")
PoR <- subset(nuvell1, nuvell1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
confidence_interval_fisher(sa.por$azi.PoR, w = 1 / san_andreas$unc)
confidence_interval_fisher(sa.por$azi.PoR, w = 1 / san_andreas$unc, boot = TRUE)
```

coordinates

Coordinate Transformations

Description

Converts vector between Cartesian and geographical coordinate systems

Usage

```
cartesian_to_geographical(n)
```

```
geographical_to_cartesian(p)
```

```
geographical_to_spherical(p)
```

Arguments

n Cartesian coordinates (x, y, z) as vector
p Geographical coordinates (latitude, longitude) as vector

Value

Functions return a (2- or 3-dimensional) vector representing a point in the requested coordinate system.

See Also

[cartesian_to_spherical\(\)](#) and [spherical_to_cartesian\(\)](#) for conversions to spherical coordinates

Examples

```
n <- c(1, -2, 3)
cartesian_to_geographical(n)
p <- c(50, 10)
geographical_to_cartesian(p)
```

coordinates2

Coordinate Transformations

Description

Converts vector between Cartesian and spherical coordinate systems

Usage

```
cartesian_to_spherical(n)
spherical_to_cartesian(p)
spherical_to_geographical(p)
```

Arguments

n Cartesian coordinates (x, y, z) as three-column vector
p Spherical coordinates (colatitude, azimuth) as two-column vector

Value

Functions return a (2- or 3-dimensional) vector representing a point in the requested coordinate system.

See Also

[cartesian_to_geographical\(\)](#) and [geographical_to_cartesian\(\)](#) for conversions to geographical coordinates

Examples

```
n <- c(1, -2, 3)
cartesian_to_spherical(n)
p <- c(50, 10)
spherical_to_cartesian(p)
```

coordinate_mod

Coordinate Correction

Description

Corrects the longitudes or latitudes to value between -180.0 and 180.0 or -90 and 90 degree

Usage

```
longitude_modulo(x)
```

```
latitude_modulo(x)
```

Arguments

x Longitude(s) or latitude(s) in degrees

Value

numeric

Examples

```
longitude_modulo(-361 + 5 * 360)
latitude_modulo(-91 + 5 * 180)
```

Description

Compilation of global models for current plate motions, including NUVEL1 (DeMets et al. 1990), NNR-NUVEL1A (DeMets et al., 1990), NNR-MORVEL56 (Argus et al., 2011), REVEL (Sella et al., 2002), GSRM2.1 (Kreemer et al., 2014), HS2-NUVEL1 (Gripp and Gordon, 1990), HS3-NUVEL1A (Gripp and Gordon, 2002), P073 (Chase 1978), AM1-2 (Minster and Jordan, 1978), ITRF2020-PPM (Altamimi et al. 2023), and PB2002 (Bird, 2003)

Usage

```
data('cpm_models')
```

Format

list containing objects of class `data.frame`

plate.name The rotating plate

plate.rot The abbreviation of the plate's name

lat,lon Coordinates of the Pole of Rotation

angle The amount of rotation (angle in 1 Myr)

plate.fix The anchored plate, i.e. `plate.rot` moves relative to `plate.fix`

model Model for current global plate motion

References

- Altamimi, Z., Métivier, L., Rebischung, P., Collilieux, X., Chanard, K., Barnéoud, J., 2023. ITRF2020 Plate Motion Model. *Geophys. Res. Lett.* **50**, 1–7. doi:10.1029/2023GL106373
- Argus, D.F., Gordon, R.G., 1991. No-net-rotation model of current plate velocities incorporating plate motion model NUVEL-1. *Geophys. Res. Lett.* **18**, 2039–2042. doi: 10.1029/91GL01532
- Argus, D. F., Gordon, R. G., & DeMets, C. (2011). Geologically current motion of 56 plates relative to the no-net-rotation reference frame. *Geochemistry, Geophysics, Geosystems*, **12**(11). 10.1029/2011GC003751.
- Chase, C.G. (1978). Plate kinematics: The Americas, East Africa, and the rest of the world. *Earth Planet. Sci. Lett.* **37**, 355–368. doi: doi:10.1016/0012821X(78)900511
- Bird, P. (2003), An updated digital model of plate boundaries, *Geochem. Geophys. Geosyst.*, **4**, 1027, doi: 10.1029/2001GC000252, 3.
- DeMets, C., Gordon, R. G., Argus, D. F., & Stein, S. (1990). Current plate motions. *Geophysical Journal International*, **101**(2), 425-478. doi:10.1111/j.1365246X.1990.tb06579.x.
- Gripp, A. E., & Gordon, R. G. (2002). Young tracks of hotspots and current plate velocities. *Geophysical Journal International*, **150**(2), 321-361. doi:10.1046/j.1365246X.2002.01627.x.

Kreemer, C., Blewitt, G., & Klein, E. C. (2014). A geodetic plate motion and Global Strain Rate Model. *Geochemistry, Geophysics, Geosystems*, **15**(10), 3849–3889. doi: 10.1002/2014GC005407.

Minster, J. and Jorda, T. (1978). Present-day plate motions. *Journal of Geophysical Research*, **83**, doi:10.1029/jb083ib11p05331.

Sella, G. F., Dixon, T. H., & Mao, A. (2002). REVEL: A model for Recent plate velocities from space geodesy. *Journal of Geophysical Research: Solid Earth*, **107**(B4). doi: 10.1029/2000jb000033.

Examples

```
data("cpm_models")
head(cpm_models[[1]])
```

deviation_norm	<i>Normalize Angle Between Two Directions</i>
----------------	---

Description

Normalizes the angle between two directions to the acute angle in between, i.e. angles between 0 and 90°

Usage

```
deviation_norm(x, y = NULL)
```

Arguments

x, y	Minuend and subtrahend. Both numeric vectors of angles in degrees. If y is missing, it treats x as difference. If not, length of subtrahend y is either 1 or equal to length(x).
------	--

Value

numeric vector, acute angles between two directions, i.e. values between 0 and 90°

Author(s)

Tobias Stephan

Examples

```
deviation_norm(175, 5)
deviation_norm(c(175, 95, 0), c(5, 85, NA))
deviation_norm(c(-5, 85, 95, 175, 185, 265, 275, 355, 365))
```

deviation_shmax	<i>Deviation of Observed and Predicted Directions of Maximum Horizontal Stress</i>
-----------------	--

Description

Calculate the angular difference between the observed and modeled direction of maximum horizontal stresses (σ_{Hmax}) along great circles, small circles, and loxodromes of the relative plate motion's Euler pole

Usage

```
deviation_shmax(prd, obs)
```

Arguments

prd	data.frame containing the modeled azimuths of σ_{Hmax} , i.e. the return object from <code>model_shmax()</code>
obs	Numeric vector containing the observed azimuth of σ_{Hmax} , same length as prd

Value

An object of class `data.frame`

dev.gc Deviation of observed stress from modeled σ_{Hmax} following great circles

dev.sc Small circles

dev.ld.cw Clockwise loxodromes

dev.ld.ccw Counter-clockwise loxodromes

Author(s)

Tobias Stephan

References

Stephan, T., Enkelmann, E., and Kroner, U. "Analyzing the horizontal orientation of the crustal stress adjacent to plate boundaries". *Sci Rep* 13. 15590 (2023). doi:[10.1038/s41598023424332](https://doi.org/10.1038/s41598023424332).

See Also

[model_shmax\(\)](#) to calculate the theoretical direction of σ_{Hmax} .

Examples

```

data("nuvel1")
# North America relative to Pacific plate:
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")

# the point where we want to model the SHmax direction:
point <- data.frame(lat = 45, lon = 20)

prd <- model_shmax(point, PoR)
deviation_shmax(prd, obs = 90)

```

dispersion

Circular Distance and Dispersion

Description

Circular distance between two angles and circular dispersion of angles about a specified angle.

Usage

```
circular_distance(x, y, axial = TRUE, na.rm = TRUE)
```

```

circular_dispersion(
  x,
  y = NULL,
  w = NULL,
  w.y = NULL,
  axial = TRUE,
  na.rm = TRUE
)

```

```
circular_distance_alt(x, y, axial = TRUE, na.rm = TRUE)
```

```

circular_dispersion_alt(
  x,
  y = NULL,
  w = NULL,
  w.y = NULL,
  axial = TRUE,
  na.rm = TRUE
)

```

Arguments

<code>x, y</code>	vectors of numeric values in degrees. <code>length(y)</code> is either 1 or <code>length(x)</code>
<code>axial</code>	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).

<code>na.rm</code>	logical. Whether NA values in <code>x</code> should be stripped before the computation proceeds.
<code>w, w.y</code>	(optional) Weights. A vector of positive numbers and of the same length as <code>x</code> . <code>w.y</code> is the (optional) weight of <code>y</code> .

Details

`circular_distance_alt()` and `circular_dispersion_alt()` are the alternative versions in Mardia and Jupp (2000), pp. 19-20. The alternative dispersion has a minimum at the sample median.

Value

`circular_distance` returns a numeric vector of positive numbers, `circular_dispersion` returns a positive number.

Note

If `y` is NULL, than the circular variance is returned.

References

- Mardia, K.V. (1972). *Statistics of Directional Data: Probability and Mathematical Statistics*. London: Academic Press.
- Mardia, K.V., and Jupp, P.E (1999). *Directional Statistics*, Wiley Series in Probability and Statistics. John Wiley & Sons, Inc., Hoboken, NJ, USA. [doi:10.1002/9780470316979](https://doi.org/10.1002/9780470316979)

See Also

`circular_mean()`, `circular_var()`.

Examples

```
a <- c(0, 2, 359, 6, 354)
circular_distance(a, 10) # distance to single value

b <- a + 90
circular_distance(a, b) # distance to multiple values

data("nuvell1")
PoR <- subset(nuvell1, nuvell1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
circular_dispersion(sa.por$azi.PoR, y = 135)
circular_dispersion(sa.por$azi.PoR, y = 135, w = 1 / san_andreas$unc)
```

distance_binned_stats *Distance Binned Summary Statistics*

Description

[Experimental] Circular summary statistics over intervals of distances.

Usage

```
distance_binned_stats(
  azi,
  distance,
  n.breaks = 10,
  width.breaks = NULL,
  unc = NULL,
  prd = NULL,
  prd.error = NULL,
  kappa = 2,
  R = 1000,
  conf.level = 0.95,
  ...
)
```

Arguments

azi	numeric. Azimuth values in degrees.
distance	numeric. the independent variable along the values in azi are sorted, e.g. the plate boundary distances
n.breaks	numeric. number (greater than or equal to 2) giving the number of equal-sized intervals into which distance is to be cut. Default is 10. Will be ignored if width.breaks is specified.
width.breaks	numeric. The width of the intervals into which distance is to be cut.
unc	(optional) Uncertainties of azi (in degrees) acting as inverse weighting factors for statistics.
prd	(optional) numeric. A predicted orientation in degrees.
prd.error	(optional) numeric. The uncertainty of the predicted orientation in degrees.
kappa	numeric. Concentration parameter applied for the circular mode.
R	integer. Number of bootstrap iterates for estimating the error of the dispersion.
conf.level	The level of confidence for confidence interval and bootstrapped standard error of dispersion.
...	optional arguments passed to <code>ggplot2::cut_interval()</code> and <code>ggplot2::cut_width()</code>

Value

tibble containing the `n` values for `azi` in each bin, min/median/max distance of the bin, and the summary statistics for `azi`. If `prd` is specified, the normal Chi-squared statistic, dispersion and its standard error are returned as well.

See Also

[circular_summary\(\)](#), [circular_dispersion\(\)](#), and [circular_dispersion_boot\(\)](#)

Examples

```
data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")
data("san_andreas")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
san_andreas$distance <- distance_from_pb(
  x = san_andreas,
  PoR = PoR,
  pb = plate_boundary,
  tangential = TRUE
)
dat <- san_andreas |> cbind(PoR_shmax(san_andreas, PoR, "right"))

distance_binned_stats(dat$azi.PoR,
  distance = dat$distance, width.breaks = 1,
  unc = dat$unc, prd = 135
) |> head()
```

<code>distance_from_pb</code>	<i>Distance from plate boundary</i>
-------------------------------	-------------------------------------

Description

Absolute distance of data points from the nearest plate boundary in degree

Usage

```
distance_from_pb(x, PoR, pb, tangential = FALSE, km = FALSE, ...)
```

Arguments

<code>x</code>	<code>sf</code> or <code>data.frame</code> objects of the data points in geographical coordinate system
<code>PoR</code>	Pole of Rotation. "data.frame" or object of class "euler.pole" containing the geographical coordinates of the Pole of Rotation
<code>pb</code>	<code>sf</code> objects of the plate boundary geometries in the geographical coordinate system
<code>tangential</code>	Logical. Whether the plate boundary is a tangential boundary (TRUE) or an inward and outward boundary (FALSE, the default).

km Logical. Whether the distance is expressed in kilometers (TRUE) or in degrees (FALSE, the default).

... optional arguments passed to `smoothr::densify()`

Details

The distance to the plate boundary is the longitudinal or latitudinal difference between the data point and the plate boundary (along the closest latitude or longitude) for inward/outward or tangential plate boundaries, respectively.

Value

Numeric vector of the great circle distances

References

Wdowinski, S. (1998). A theory of intraplate tectonics. *Journal of Geophysical Research: Solid Earth*, 103(3), 5037-5059. <http://dx.doi.org/10.1029/97JB03390>

Examples

```
data("nuvel1")
na_pa <- subset(nuvel1, nuvel1$plate.rot == "na")

data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")

data("san_andreas")
res <- distance_from_pb(
  x = san_andreas, PoR = na_pa, pb = plate_boundary, tangential = TRUE
)
head(res)

res.km <- distance_from_pb(
  x = san_andreas, PoR = na_pa, pb = plate_boundary, tangential = TRUE, km = TRUE
)
range(res.km)
```

dist_greatcircle *Distance between points*

Description

Returns the great circle distance between a location and all grid point in km

Usage

```
dist_greatcircle(
  lat1,
  lon1,
  lat2,
  lon2,
  r = earth_radius(),
  method = c("haversine", "orthodrome", "vincenty", "euclidean")
)
```

Arguments

lat1, lon1	numeric vector. coordinate of point(s) 1 (degrees).
lat2, lon2	numeric vector. coordinates of point(s) 2 (degrees).
r	numeric. radius of the sphere (default = 6371.0087714 km, i.e. the radius of the Earth)
method	Character. Formula for calculating great circle distance, one of: "haversine" great circle distance based on the haversine formula that is optimized for 64-bit floating-point numbers (the default) "orthodrome" great circle distance based on the spherical law of cosines "vincenty" distance based on the Vincenty formula for an ellipsoid with equal major and minor axes " euclidean " Euclidean distance (not great circle distance!)

Value

numeric vector with length equal to length(lat1)

See Also

[orthodrome\(\)](#), [haversine\(\)](#), [vincenty\(\)](#)

Examples

```
dist_greatcircle(lat1 = 20, lon1 = 12, lat2 = c(50, 30), lon2 = c(40, 32))
dist_greatcircle(
  lat1 = 20, lon1 = 12, lat2 = c(50, 30), lon2 = c(40, 32),
  method = "orthodrome"
)
dist_greatcircle(
  lat1 = 20, lon1 = 12, lat2 = c(50, 30), lon2 = c(40, 32),
  method = "vincenty"
)
dist_greatcircle(
  lat1 = 20, lon1 = 12, lat2 = c(50, 30), lon2 = c(40, 32),
  method = "euclidean"
)
```

earth_radius	<i>Earth's radius in km</i>
--------------	-----------------------------

Description

IERS mean radius of Earth in km (based on WGS 84)

Usage

```
earth_radius()
```

Value

numeric value

equivalent_rotation	<i>Equivalent rotation</i>
---------------------	----------------------------

Description

Transforms a sequence of rotations into a new reference system

Usage

```
equivalent_rotation(x, fixed, rot)
```

Arguments

x	Object of class "data.frame" containing the Euler poles of plate rotations: plate.rot Moving plate lat, lon coordinates of Euler pole angle Angle of rotation plate.fix Fixed plate
fixed	plate that will be regarded as fixed. Has to be one out of x\$plate.fix
rot	(optional) plate that will be regarded as rotating. Has to be one out of x\$plate.rot.

Value

sequence of plate rotations in new reference system. Same object class as x

See Also

[relative_rotation\(\)](#)

Examples

```

data(nuvel1) # load the NUVEL1 rotation parameters

# all nuvel1 rotation equivalent to fixed Africa:
equivalent_rotation(nuvel1, fixed = "af")
# relative plate motion between Eurasia and India:
equivalent_rotation(nuvel1, "eu", "in")

```

est.kappa

Concentration parameter of von Mises distribution

Description

Computes the maximum likelihood estimate of κ , the concentration parameter of a von Mises distribution, given a set of angular measurements.

Usage

```
est.kappa(x, w = NULL, bias = FALSE, ...)
```

Arguments

x	numeric. angles in degrees
w	numeric. weightings
bias	logical parameter determining whether a bias correction is used in the computation of the MLE. Default for bias is FALSE for no bias correction.
...	optional parameters passed to <code>circular_mean()</code>

Value

numeric.

Examples

```

set.seed(123)
est.kappa(rvm(100, 90, 10), w = 1 / runif(100, 0, 10))

```

euler_pole	<i>Euler pole object</i>
------------	--------------------------

Description

Creates an object of the orientation of the Euler pole axis

Usage

```
euler_pole(x, y, z = NA, geo = TRUE, angle = NA)
```

Arguments

x	latitude or x coordinate of Euler pole axis
y	longitude or y
z	z coordinate
geo	logical, TRUE (the default) if Euler pole axis is given in geographical coordinates (latitude, longitude). FALSE if given in Cartesian coordinates (x, y, z)
angle	(optional) Angle of rotation in degrees (CCW rotation if angle is positive)

Value

An object of class "euler.pole" containing the Euler pole axis in both geographical and Cartesian coordinates and the angle of rotation in radians.

Examples

```
euler_pole(90, 0, angle = 45)
euler_pole(0, 0, 1, geo = FALSE)
```

euler_to_Q4	<i>Quaternion from Euler angle-axis representation for rotations</i>
-------------	--

Description

Quaternion from Euler angle-axis representation for rotations

Usage

```
euler_to_Q4(x, normalize = FALSE)
```

Arguments

x	"euler.pole" object
normalize	logical. Whether a quaternion normalization should be applied (TRUE) or not (FALSE, the default).

Value

object of class "quaternion"

get_azimuth	<i>Azimuth Between two Points</i>
-------------	-----------------------------------

Description

Calculate initial bearing (or forward azimuth/direction) to go from point a to point b following great circle arc on a sphere.

Usage

```
get_azimuth(lat_a, lon_a, lat_b, lon_b)
```

Arguments

lat_a, lat_b Numeric. Latitudes of a and b (in degrees).
lon_a, lon_b Numeric. Longitudes of a and b (in degrees).

Details

`get_azimuth()` is based on the spherical law of tangents. This formula is for the initial bearing (sometimes referred to as forward azimuth) which if followed in a straight line along a great circle arc will lead from the start point a to the end point b.

$$\theta = \arctan 2(\sin \Delta\lambda \cos \psi_2, \cos \psi_1 \sin \psi_1 - \sin \psi_1 \cos \psi_2 \cos \Delta\lambda)$$

where ψ_1, λ_1 is the start point, ψ_2, λ_2 the end point ($\Delta\lambda$ is the difference in longitude).

Value

numeric. Azimuth in degrees

References

<http://www.movable-type.co.uk/scripts/latlong.html>

Examples

```
berlin <- c(52.517, 13.4) # Berlin
tokyo <- c(35.7, 139.767) # Tokyo
get_azimuth(berlin[1], berlin[2], tokyo[1], tokyo[2])
```

import_WSM2016

*World Stress Map Database (WSM) Release 2016***Description**

Download WSM2016 database from the GFZ sever and applies optional filters. If `destdir` is specified, the data can be reloaded in a later R session using `load_WSM2016()` using the same arguments.

Usage

```
download_WSM2016(destdir = tempdir(), load = TRUE, ...)
```

```
load_WSM2016(
  file,
  quality = c("A", "B", "C", "D", "E"),
  lat_range = c(-90, 90),
  lon_range = c(-180, 180),
  depth_range = c(-Inf, Inf),
  method = c("BO", "BOC", "BOT", "BS", "DIF", "FMA", "FMF", "FMS", "GFI", "GFM", "GFS",
    "GVA", "HF", "HFG", "HFM", "HFP", "OC", "PC", "SWB", "SWL", "SWS"),
  regime = c("N", "NS", "T", "TS", "S", NA)
)
```

Arguments

<code>destdir</code>	where to save files, defaults to <code>base::tempdir()</code> , <code>base::getwd()</code> is also possible.
<code>load</code>	TRUE load the dataset into R, FALSE return the file name of the downloaded object.
<code>...</code>	(optional) arguments passed to <code>load_WSM2016()</code>
<code>file</code>	the name of the file which the data are to be read from.
<code>quality</code>	a character vectors containing the quality levels to be included. Includes all quality ranks (A-E) by default.
<code>lat_range, lon_range</code>	two-element numeric vectors giving the range of latitudes and longitudes (in degrees).
<code>depth_range</code>	two-element numeric vectors giving the depth interval (in km)
<code>method</code>	a character vectors containing the methods of stress inversion to be included. Includes all methods by default. See WSM2016 manual for used acronyms.
<code>regime</code>	a character vectors containing the stress regimes to be included. Acronyms: "N" - normal, "T" - thrust, "S" - strike-slip, "NS" - oblique normal, "TS" - oblique thrust, and NA - unknown faulting

Value

sf object of and the parsed numeric uncertainty (unc) based on the reported standard deviation and the quality rank. If load=FALSE, the path to the downloaded file is returned.

Note

Because of R-compatibility and easy readability reasons, the downloaded dataset is a modified version of the original, WSM server version: All column names have been changed from uppercase (in the original dataset) to lowercase characters. Unknown azimuth values are represented by NA values instead of 999 in the original. Unknown regimes are represented by NA instead of "U" in the original.

Source

<https://datapub.gfz-potsdam.de/download/10.5880.WSM.2016.001/wsm2016.csv>

References

Heidbach, O., M. Rajabi, X. Cui, K. Fuchs, B. Müller, J. Reinecker, K. Reiter, M. Tingay, F. Wenzel, F. Xie, M. O. Ziegler, M.-L. Zoback, and M. D. Zoback (2018): The World Stress Map database release 2016: Crustal stress pattern across scales. *Tectonophysics*, **744**, 484-498, doi:10.1016/j.tecto.2018.07.007.

Examples

```
## Not run:
download_WSM2016(
  quality = c("A", "B", "C"), lat_range = c(51, 72),
  lon_range = c(-180, -130), depth_range = c(0, 10), method = "FMS"
)

## End(Not run)
```

is.euler

Check if object is euler.pole

Description

Check if object is euler.pole

Usage

```
is.euler(x)
```

Arguments

x object of class "euler.pole"

Value

logical

`kuiper_test`*Kuiper Test of Circular Uniformity*

Description

Kuiper's test statistic is a rotation-invariant Kolmogorov-type test statistic. The critical values of a modified Kuiper's test statistic are used according to the tabulation given in Stephens (1970).

Usage

```
kuiper_test(x, alpha = 0, axial = TRUE, quiet = FALSE)
```

Arguments

<code>x</code>	numeric vector containing the circular data which are expressed in degrees
<code>alpha</code>	Significance level of the test. Valid levels are 0.01, 0.05, and 0.1. This argument may be omitted (NULL, the default), in which case, a range for the p-value will be returned.
<code>axial</code>	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or circular, i.e. 2π -periodical (FALSE).
<code>quiet</code>	logical. Prints the test's decision.

Details

If `statistic > p.value`, the null hypothesis is rejected. If not, randomness (uniform distribution) cannot be excluded.

Value

list containing the test statistic `statistic` and the significance level `p.value`.

Examples

```
# Example data from Mardia and Jupp (2001), pp. 93
pidgeon_homing <- c(55, 60, 65, 95, 100, 110, 260, 275, 285, 295)
kuiper_test(pidgeon_homing, alpha = .05)

# San Andreas Fault Data:
data(san_andreas)
data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
kuiper_test(sa.por$azi.PoR, alpha = .05)
```

line_azimuth	<i>Extract azimuths of line segments</i>
--------------	--

Description

Extract azimuths of line segments

Usage

```
line_azimuth(x, warn = TRUE)
```

```
lines_azimuths(x)
```

Arguments

x	sf object of type "LINESTRING" or "MULTILINESTRING"
warn	logical; if TRUE, warn if "MULTILINESTRING" (default).

Details

It is recommended to perform `line_azimuth()` on single line objects, i.e. type "LINESTRING", instead of "MULTILINESTRING". This is because the azimuth of the last point of a line will be calculated to the first point of the next line otherwise. This will cause a warning message (if `warn = TRUE`). For "MULTILINESTRING" objects, use `lines_azimuths()`.

Value

sf object of type "POINT" with the columns and entries of the first row of x

Examples

```
data("plates")

# one line:
subset(plates, pair == "af-eu") |>
  smoothr::densify() |>
  line_azimuth()

# multiple lines:
lines_azimuths(plates[1:5, ])
```

mean_resultant_length *Mean Resultant Length*

Description

Measure of spread around the circle. It should be noted that: If $R=0$, then the data is completely spread around the circle. If $R=1$, the data is completely concentrated on one point.

Usage

```
mean_resultant_length(x, w = NULL, na.rm = TRUE)
```

Arguments

x	numeric vector. Values in degrees, for which the mean, median or standard deviation are required.
w	(optional) Weights. A vector of positive numbers, of the same length as x.
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Value

numeric.

References

Mardia, K.V. (1972). *Statistics of Directional Data: Probability and Mathematical Statistics*. London: Academic Press.

Examples

```
# Example data from Davis (1986), pp. 316
finland_stria <- c(
  23, 27, 53, 58, 64, 83, 85, 88, 93, 99, 100, 105, 113,
  113, 114, 117, 121, 123, 125, 126, 126, 126, 127, 127, 128, 128, 129, 132,
  132, 132, 134, 135, 137, 144, 145, 145, 146, 153, 155, 155, 155, 157, 163,
  165, 171, 172, 179, 181, 186, 190, 212
)
mean_resultant_length(finland_stria, w = NULL, na.rm = FALSE) # 0.800
```

model_shmax	<i>Theoretical Direction of Maximum Horizontal Stress in the geographical reference system.</i>
-------------	---

Description

Models the direction of maximum horizontal stress σ_{Hmax} along great circles, small circles, and loxodromes at a given point or points according to the relative plate motion in the geographical coordinate reference system.

Usage

```
model_shmax(df, euler)
```

Arguments

df	data.frame containing the coordinates of the point(s) (lat, lon).
euler	"data.frame" or object of class "euler.pole" containing the geographical coordinates of the Euler pole

Details

σ_{Hmax} following *great circles* is the (initial) bearing between the given point and the pole of relative plate motion. σ_{Hmax} along *small circles*, clockwise, and counter-clockwise *loxodromes* is 90° , $+45^\circ$, and 135° (-45°) to this great circle bearing, respectively.

Value

data.frame

gc Azimuth of modeled σ_{Hmax} following great circles

sc Small circles

ld.cw Clockwise loxodromes

ld.ccw Counter-clockwise loxodromes

Author(s)

Tobias Stephan

References

Stephan, T., Enkelmann, E., and Kroner, U. "Analyzing the horizontal orientation of the crustal stress adjacent to plate boundaries". *Sci Rep* 13. 15590 (2023). doi:10.1038/s41598023424332.

See Also

[deviation_shmax\(\)](#) to compute the deviation of the modeled direction from the observed direction of σ_{Hmax} . [PoR_shmax\(\)](#) to calculate the azimuth of σ_{Hmax} in the pole of rotation reference system.

Examples

```

data("nuvel1")
# North America relative to Pacific plate:
euler <- subset(nuvel1, nuvel1$plate.rot == "na")

# the point where we want to model the SHmax direction:
point <- data.frame(lat = 45, lon = 20)

model_shmax(point, euler)

```

norm_chisq

*Normalized Chi-Squared Test for Circular Data***Description**

A quantitative comparison between the predicted and observed directions of σ_{Hmax} is obtained by the calculation of the average azimuth and by a normalized χ^2 test.

Usage

```
norm_chisq(obs, prd, unc)
```

Arguments

obs	Numeric vector containing the observed azimuth of σ_{Hmax} , same length as prd
prd	Numeric vector containing the modeled azimuths of σ_{Hmax} , i.e. the return object from <code>model_shmax()</code>
unc	Uncertainty of observed σ_{Hmax} , either a numeric vector or a number

Details

The normalized χ^2 test is

$$Norm\chi_i^2 == \frac{\sum_{i=1}^M \left(\frac{\alpha_i - \alpha_{predict}}{\sigma_i} \right)^2}{\sum_{i=1}^M \left(\frac{90}{\sigma_i} \right)^2}$$

The value of the chi-squared test statistic is a number between 0 and 1 indicating the quality of the predicted σ_{Hmax} directions. Low values (≤ 0.15) indicate good agreement, high values (> 0.7) indicate a systematic misfit between predicted and observed σ_{Hmax} directions.

Value

Numeric vector

References

Wdowinski, S., 1998, A theory of intraplate tectonics. *Journal of Geophysical Research: Solid Earth*, **103**, 5037-5059, doi: 10.1029/97JB03390.

Examples

```

data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na") # North America relative to
# Pacific plate
data(san_andreas)
point <- data.frame(lat = 45, lon = 20)
prd <- model_shmax(point, PoR)
norm_chisq(obs = c(50, 40, 42), prd$sc, unc = c(10, NA, 5))

data(san_andreas)
prd2 <- PoR_shmax(san_andreas, PoR, type = "right")
norm_chisq(obs = prd2$azi.PoR, 135, unc = san_andreas$unc)

```

nuvel1

NUVEL-1 Global model of current plate motions

Description

NNR-NUVEL-1 global model of current plate motions by DeMets et al. 1990

Usage

```
data('nuvel1')
```

Format

An object of class `data.frame`

plate.name The rotating plate

plate.rot The abbreviation of the plate's name

lat,lon Coordinates of the Pole of Rotation

angle The amount of rotation (angle in 1 Myr)

plate.fix The anchored plate, i.e. `plate.rot` moves relative to `plate.fix`

source Reference to underlying study

References

DeMets, C., Gordon, R. G., Argus, D. F., & Stein, S. (1990). Current plate motions. *Geophysical Journal International*, **101**(2), 425-478. doi:10.1111/j.1365246X.1990.tb06579.x.

Examples

```

data("nuvel1")
head("nuvel1")

```

nuvel1_plates *Plate Boundaries on the Earth*

Description

Global set of present plate boundaries on the Earth based on NUVEL-1 model by DeMets et al. 1990

Usage

```
data('nuvel1_plates')
```

Format

An object of class sf

References

DeMets, C., Gordon, R. G., Argus, D. F., & Stein, S. (1990). Current plate motions. *Geophysical Journal International*, **101**(2), 425-478. doi:10.1111/j.1365246X.1990.tb06579.x.

Examples

```
data("nuvel1_plates")
head("nuvel1_plates")
```

parse_wsm *Numerical values to World Stress Map Quality Ranking*

Description

Assigns numeric values of the precision (sd.) of each measurement to the categorical quality ranking of the World Stress Map (A, B, C, D, E).

Usage

```
parse_wsm_quality(x)

quantise_wsm_quality(x)
```

Arguments

x Either a string or a character/factor vector of WSM quality ranking

Value

"numeric". the standard deviation of stress azimuth

Note

quantise_wsm_quality() was renamed to parse_wsm_quality() to create a more consistent API.

References

Heidbach, O., Barth, A., Müller, B., Reinecker, J., Stephansson, O., Tingay, M., Zang, A. (2016). WSM quality ranking scheme, database description and analysis guidelines for stress indicator. *World Stress Map Technical Report 16-01*, GFZ German Research Centre for Geosciences. [doi:10.2312/wsm.2016.001](https://doi.org/10.2312/wsm.2016.001)

Examples

```
parse_wsm_quality(c("A", "B", "C", "D", NA, "E"))
data("san_andreas")
parse_wsm_quality(san_andreas$quality)
```

 pb2002

Global model of current plate motions

Description

PB2002 global model of current plate motions by Bird 2003

Usage

```
data('pb2002')
```

Format

An object of class `data.frame`

plate.name The rotating plate

plate.rot The abbreviation of the plate's name

lat,lon Coordinates of the Pole of Rotation

angle The amount of rotation (angle in 1 Myr)

plate.fix The anchored plate, i.e. `plate.rot` moves relative to `plate.fix`

source Reference to underlying study

References

Bird, P. (2003), An updated digital model of plate boundaries, *Geochem. Geophys. Geosyst.*, **4**, 1027, doi: 10.1029/2001GC000252, 3.

Examples

```
data("pb2002")
head("pb2002")
```

plates

Plate Boundaries on the Earth

Description

Global set of present plate boundaries on the Earth based on PB2002 model by Bird (2003). Contains the plate boundary displacement types such as inward, outward, or tangentially displacement.

Usage

```
data('plates')
```

Format

An object of class sf

References

Bird, P. (2003), An updated digital model of plate boundaries, *Geochem. Geophys. Geosyst.*, **4**, 1027, doi: 10.1029/2001GC000252, 3.

Examples

```
data("plates")
head("plates")
```

plot_density

Circular Density Plot

Description

Plot the multiples of a von Mises density distribution

Usage

```
plot_density(  
  x,  
  kappa = NULL,  
  axial = TRUE,  
  n = 512,  
  norm.density = FALSE,  
  ...,  
  scale = 1.1,  
  shrink = 1,  
  add = TRUE,  
  main = NULL,
```

```

    labels = TRUE,
    at = seq(0, 360 - 45, 45),
    cborder = TRUE,
    grid = FALSE
  )

```

Arguments

x	Data to be plotted. A numeric vector containing angles (in degrees).
kappa	Concentration parameter for the von Mises distribution. Small kappa gives smooth density lines. Will be estimated using <code>est.kappa()</code> if not provided.
axial	Logical. Whether data are uniaxial (<code>axial=FALSE</code>) or biaxial (<code>TRUE</code> , the default).
n	the number of equally spaced points at which the density is to be estimated.
norm.density	logical. Normalize the density?
...	Further graphical parameters may also be supplied as arguments.
scale	radius of plotted circle. Default is 1.1.
shrink	parameter that controls the size of the plotted function. Default is 1.
add	logical. Add to existing plot? (<code>TRUE</code> by default).
main	Character string specifying the title of the plot.
labels	Either a logical value indicating whether to plot labels next to the tick marks, or a vector of labels for the tick marks.
at	Optional vector of angles at which tick marks should be plotted. Set <code>at=numeric(0)</code> to suppress tick marks.
cborder	logical. Border of rose plot.
grid	logical. Whether a grid should be added.

Value

plot or calculated densities as numeric vector

See Also

[dvm\(\)](#)

Examples

```

# Plot the rose histogram first:
rose(san_andreas$azi, dots = TRUE, stack = TRUE, dot_cex = 0.5, dot_pch = 21)

# Add density curve outside of main plot:
plot_density(san_andreas$azi,
  kappa = 100, col = "#51127CFF", shrink = 1.5,
  norm.density = FALSE
)

# Plot density inside plot only:

```

```
plot_density(san_andreas$azi,
  kappa = 100, col = "#51127CFF", add = FALSE,
  scale = .5, shrink = 2, norm.density = TRUE, grid = TRUE
)
```

plot_points

Add Points to a Circular Plot

Description

Add points to a plot of circular data points on the current graphics device.

Usage

```
plot_points(
  x,
  axial = TRUE,
  stack = FALSE,
  binwidth = 1,
  cex = 1,
  sep = 0.025,
  jitter_factor = 0,
  ...,
  scale = 1.1,
  add = TRUE,
  main = NULL,
  labels = TRUE,
  at = seq(0, 360 - 45, 45),
  cborder = TRUE
)
```

Arguments

x	Data to be plotted. A numeric vector containing angles (in degrees).
axial	Logical. Whether data are uniaxial (<code>axial=FALSE</code>) or biaxial (<code>TRUE</code> , the default).
stack	logical: if <code>TRUE</code> , points are stacked on the perimeter of the circle. Otherwise, all points are plotted on the perimeter of the circle. Default is <code>FALSE</code> .
binwidth	numeric. Bin width (in degrees) for the stacked dot plots. ignored when <code>stack==FALSE</code> . Is set to 1 degree by default.
cex	character (or symbol) expansion: a numerical vector. This works as a multiple of <code>par("cex")</code> .
sep	constant used to specify the distance between stacked points, if <code>stack==TRUE</code> or in the case of more than one dataset. Default is <code>0.025</code> ; smaller values will create smaller spaces.

<code>jitter_factor</code>	numeric. Adds a small amount of random variation to the location of each points along radius that is added to scale. Jitter is ignored when <code>stack==TRUE</code>). If 0, no jitter is added (by default); if negative, the points fall into the circle.
<code>...</code>	Further graphical parameters may also be supplied as arguments.
<code>scale</code>	radius of plotted circle. Default is 1.1. Larger values shrink the circle, while smaller values enlarge the circle.
<code>add</code>	logical
<code>main</code>	Character string specifying the title of the plot.
<code>labels</code>	Either a logical value indicating whether to plot labels next to the tick marks, or a vector of labels for the tick marks.
<code>at</code>	Optional vector of angles at which tick marks should be plotted. Set <code>at=numeric(0)</code> to suppress tick marks.
<code>cborder</code>	logical. Border of rose plot.

Value

A list with information on the plot

Examples

```
x <- rvm(100, mean = 90, k = 5)

# plot point without jitter
plot_points(x, add = FALSE)

# with some jitter
plot_points(x, jitter_factor = .2, add = FALSE)

# stacked dots:
plot_points(x, stack = TRUE, binwidth = 3, add = FALSE)
```

PoR2Geo_azimuth	<i>Azimuth Conversion From PoR to Geographical Coordinate Reference System</i>
-----------------	--

Description

Conversion of PoR azimuths into geographical azimuths

Usage

```
PoR2Geo_azimuth(x, PoR, axial = TRUE)
```

Arguments

x	data.frame containing the PoR equivalent azimuths (azi.PoR), and either the geographical coordinates of the point(s) or the PoR-equivalent coordinates.
PoR	data.frame containing the geographical location of the Euler pole (lat, lon)
axial	logical. Whether the azimuth is axial (0-180) or directional (0-360).

Value

numeric vector of transformed azimuths (in degrees)

References

Stephan, T., Enkelmann, E., and Kroner, U. "Analyzing the horizontal orientation of the crustal stress adjacent to plate boundaries". *Sci Rep* 13. 15590 (2023). doi:10.1038/s41598023424332.

See Also

[PoR_shmax\(\)](#)

Examples

```
data("nuvel1")
# North America relative to Pacific plate:
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
data("san_andreas")
san_andreas$azi.PoR <- PoR_shmax(san_andreas, PoR)

# convert back to geo CRS
PoR2Geo_azimuth(san_andreas, PoR) |> head()
```

PoR_azi	<i>Azimuth Conversion from Geographical to PoR Coordinate Reference System</i>
---------	--

Description

Transforms azimuths and models the direction of maximum horizontal stress σ_{Hmax} in the Euler pole (Pole of Rotation) coordinate reference system. When type of plate boundary is given, it also gives the deviation from the theoretically predicted azimuth of σ_{Hmax} , the circular distance, and the normalized χ^2 statistics.

Usage

```
PoR_azimuth(x, PoR, axial = TRUE)
```

```
PoR_shmax(x, PoR, type = c("none", "in", "out", "right", "left"))
```


Arguments

x	sf object or a <code>data.frame</code> containing the coordinates of the point(s) (lat, lon). x must contain the direction of σ_{Hmax} as column <code>azi</code> and its standard deviation as <code>unc</code> (the latter is optional)
PoR	" <code>data.frame</code> " or object of class " <code>euler.pole</code> " containing the geographical coordinates of the Euler pole
axial	logical. Whether the azimuth is axial (0-180) or directional (0-360).
type	Character. Type of plate boundary (optional). Can be "out", "in", "right", or "left" for outward, inward, right-lateral, or left-lateral moving plate boundaries, respectively. If "none" (the default), only the PoR-equivalent azimuth is returned.

Details

The azimuth of σ_{Hmax} in the pole of rotation reference system is approximate 0 (or 180), 45, 90, 135 degrees if the stress is sourced by an outward, sinistral, inward, or dextral moving plate boundary, respectively. directions of σ_{Hmax} with respect to the four plate boundary types.

Value

PoR_azimuth returns numeric vector of the transformed azimuth in degrees. PoR_shmax returns either a numeric vector of the azimuths in the transformed coordinate system (in degrees), or a "`data.frame`" with

`azi.PoR` the transformed azimuths (in degrees),
`prd` the predicted azimuths (in degrees),
`dev` the deviation between the transformed and the predicted azimuth (in degrees),
`nchisq` the Norm χ^2 test statistic, and
`cdist` the angular distance between the transformed and the predicted azimuth.

References

Stephan, T., Enkelmann, E., and Kroner, U. "Analyzing the horizontal orientation of the crustal stress adjacent to plate boundaries". *Sci Rep* 13. 15590 (2023). doi:10.1038/s41598023424332.

See Also

[model_shmax\(\)](#) to compute the theoretical direction of σ_{Hmax} in the geographical reference system. [deviation_shmax\(\)](#) to compute the deviation of the modeled direction from the observed direction of σ_{Hmax} . [norm_chisq\(\)](#) to calculate the normalized χ^2 statistics. [circular_distance\(\)](#) to calculate the angular distance.

Examples

```
data("nuvel1")
# North America relative to Pacific plate:
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
```

```
data("san_andreas")
res <- PoR_shmax(san_andreas, PoR, type = "right")
head(res)
```

PoR_coordinates *Coordinates of the Pole of Rotation Reference System*

Description

Retrieve the PoR equivalent coordinates of an object

Usage

```
PoR_coordinates(x, PoR)
```

Arguments

x	sf or data.frame containing lat and lon coordinates (lat, lon)
PoR	Pole of Rotation. "data.frame" or object of class "euler.pole" containing the geographical coordinates of the Euler pole

Value

`PoR_coordinates()` returns data.frame with the PoR coordinates (lat.PoR, lon.PoR).

Examples

```
data("nuvel1")
por <- subset(nuvel1, nuvel1$plate.rot == "na") # North America relative to Pacific plate
data("san_andreas")

# coordinates from sf object
san_andreas.por_sf <- PoR_coordinates(san_andreas, por)
head(san_andreas.por_sf)

# coordinates from data.frame
san_andreas.por_df <- PoR_coordinates(sf::st_drop_geometry(san_andreas), por)
head(san_andreas.por_df)
```

PoR_crs	<i>PoR coordinate reference system</i>
---------	--

Description

Create the reference system transformed in Euler pole coordinate

Usage

```
PoR_crs(x)
```

Arguments

x "data.frame" or "euler.pole" object containing the geographical coordinates of the Euler pole

Details

The PoR coordinate reference system is oblique transformation of the geographical coordinate system with the Euler pole coordinates being the the translation factors.

Value

Object of class crs

See Also

[sf::st_crs\(\)](#)

Examples

```
data("nuvel1")
por <- subset(nuvel1, nuvel1$plate.rot == "na") # North America relative to Pacific plate
PoR_crs(por)
```

PoR_distance	<i>Distance to Pole of Rotation</i>
--------------	-------------------------------------

Description

Retrieve the (angular) distance to the PoR (Euler pole).

Usage

```
PoR_distance(x, PoR, FUN = orthodrome)
```

Arguments

x	sf or data.frame containing lat and lon coordinates (lat, lon)
PoR	Pole of Rotation. "data.frame" or object of class "euler.pole" containing the geographical coordinates of the Euler pole
FUN	function to calculate the great-circle distance. orthodrome() , haversine() (the default), or vincenty() .

Value

numeric vector

Examples

```

data("nuvel1")
por <- subset(nuvel1, nuvel1$plate.rot == "na") # North America relative to Pacific plate
data("san_andreas")

# distance form sf object
PoR_distance(san_andreas, por)

# distance form data.frame
PoR_distance(sf::st_drop_geometry(san_andreas), por)
PoR_distance(sf::st_drop_geometry(san_andreas), por, FUN = orthodrome)
PoR_distance(sf::st_drop_geometry(san_andreas), por, FUN = vincenty)

```

PoR_map

Map of data in Pole of Rotation reference frame

Description

Transforms the spatial data and azimuths into the PoR reference frame and shows them in a map

Usage

```

PoR_map(
  x,
  PoR,
  pb = NULL,
  type = c("none", "in", "out", "right", "left"),
  show.deviation = FALSE,
  ...
)

```

Arguments

<code>x, pb</code>	sf objects of the data points and the plate boundary geometries in the geographical coordinate system
<code>PoR</code>	Pole of Rotation. "data.frame" or object of class "euler.pole" containing the geographical coordinates of the Pole of Rotation
<code>type</code>	Character. Type of plate boundary (optional). Can be "out", "in", "right", or "left" for outward, inward, right-lateral, or left-lateral moving plate boundaries, respectively. If "none" (the default), only the PoR-equivalent azimuth is returned.
<code>show.deviation</code>	logical. Whether the data should be color-coded according to the deviation from the prediction, or according to the stress regime? Is ignored if <code>type=='none'</code> .
<code>...</code>	optional arguments passed to <code>tectonicr.colors()</code>

Value

plot

See Also

`PoR_shmax()`, `axes()`, `tectonicr.colors()`

Examples

```
data("nuvel1")
na_pa <- subset(nuvel1, nuvel1$plate.rot == "na")

data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")

data("san_andreas")
PoR_map(san_andreas, PoR = na_pa, pb = plate_boundary, type = "right", show.deviation = TRUE)
```

PoR_stress2grid

Spatial Interpolation of SHmax in PoR Coordinate Reference System

Description

The data is transformed into the PoR system before the interpolation. The interpolation grid is returned in geographical coordinates and azimuths.

Usage

```
PoR_stress2grid(
  x,
  PoR,
  grid = NULL,
```

```

    PoR_grid = TRUE,
    lon_range = NULL,
    lat_range = NULL,
    gridsize = 2.5,
    ...
)

PoR_stress2grid_stats(
  x,
  PoR,
  grid = NULL,
  PoR_grid = TRUE,
  lon_range = NULL,
  lat_range = NULL,
  gridsize = 2.5,
  ...
)

```

Arguments

x	sf object containing azi SHmax in degree unc Uncertainties of SHmax in degree type Methods used for the determination of the orientation of SHmax
PoR	Pole of Rotation. "data.frame" or object of class "euler.pole" containing the geographical coordinates of the Euler pole
grid	(optional) Point object of class sf.
PoR_grid	logical. Whether the grid should be generated based on the coordinate range in the PoR (TRUE, the default) CRS or the geographical CRS (FALSE). Is ignored if grid is specified.
lon_range, lat_range	(optional) numeric vector specifying the minimum and maximum longitudes and latitudes (are ignored if "grid" is specified).
gridsize	Numeric. Target spacing of the regular grid in decimal degree. Default is 2.5 (is ignored if grid is specified)
...	Arguments passed to stress2grid()

Details

Stress field and wavelength analysis in PoR system and back-transformed

Value

sf object containing

lon,lat longitude and latitude in geographical CRS (in degrees)

lon.PoR,lat.PoR longitude and latitude in PoR CRS (in degrees)

azi geographical mean SHmax in degree
azi.PoR PoR mean SHmax in degree
sd Standard deviation of SHmax in degrees
R Search radius in km
mdr Mean distance of datapoints per search radius
N Number of data points in search radius

See Also

[stress2grid\(\)](#), [compact_grid\(\)](#)

Examples

```
data("san_andreas")
data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
PoR_stress2grid(san_andreas, PoR)

## Not run:
PoR_stress2grid_stats(san_andreas, PoR)

## End(Not run)
```

por_transformation *Conversion between spherical PoR to geographical coordinate system*

Description

Transformation from spherical PoR to geographical coordinate system and vice versa

Usage

```
geographical_to_PoR(x, PoR)
```

```
PoR_to_geographical(x, PoR)
```

Arguments

x	Can be either a "data.frame" containing lat and lon coordinates of a point in the geographical CRS or the lat.PoR, lon.PoR) of the point in the PoR CRS, a two-column matrix containing the lat and lon coordinates, a sf object, or a raster object.
PoR	Pole of Rotation. "data.frame" or object of class "euler.pole" containing the geographical coordinates of the Euler pole

Value

object of same type of `x` with the transformed coordinates. If `x` was a `data.frame`, transformed coordinates are named `lat.PoR` and `lon.PoR` for PoR CRS, or `lat` and `lon` for geographical CRS).

Examples

```
data("nuvel1")
por <- subset(nuvel1, nuvel1$plate.rot == "na") # North America relative to Pacific plate
data("san_andreas")
san_andreas.por <- geographical_to_PoR(san_andreas, por)
head(san_andreas.por)
head(PoR_to_geographical(san_andreas.por, por))
```

 prd_err

Error of Model's Prediction

Description

The maximum error in the model's predicted azimuth given the Pole of rotations uncertainty and distance of the data point to the pole.

Usage

```
prd_err(dist_PoR, sigma_PoR = 1)
```

Arguments

<code>dist_PoR</code>	Distance to Euler pole (great circle distance, in degree)
<code>sigma_PoR</code>	uncertainty of the position of the Pole of rotation (in degree).

Value

numeric vector. The maximum error for azimuths prediction (in degree)

References

Ramsay, J.A. Folding and fracturing of rocks. McGraw-Hill, New York, 1967.

See Also

[PoR_shmax\(\)](#) and [model_shmax\(\)](#) for the model's prediction, and [orthodrome\(\)](#) for great circle distances.

Examples

```

prd_err(67, 1)

# San Andreas example:
data("nuvel1")
por <- subset(nuvel1, nuvel1$plate.rot == "na") # North America relative to Pacific plate
data("san_andreas")
d <- PoR_distance(san_andreas, por)
prd_err(d)

```

projected_pb_strike *Strike of the plate boundary projected on data point*

Description

The fault's strike in the PoR CRS projected on the data point along the predicted stress trajectories.

Usage

```
projected_pb_strike(x, PoR, pb, tangential = FALSE, ...)
```

Arguments

x, pb	sf objects of the data points and the plate boundary geometries in the geographical coordinate system
PoR	Pole of rotation. "data.frame" or object of class "euler.pole" containing the geographical coordinates of the Euler pole
tangential	Logical. Whether the plate boundary is a tangential boundary (TRUE) or an inward and outward boundary (FALSE, the default).
...	optional arguments passed to <code>smoothr::densify()</code>

Details

Useful to calculate the beta angle, i.e. the angle between SHmax direction (in PoR CRS!) and the fault's strike (in PoR CRS). The beta angle is the same in geographical and PoR coordinates.

Value

Numeric vector of the strike direction of the plate boundary (in degree)

Note

The algorithm calculates the great circle bearing between line vertices. Since transform plate boundaries represent small circle lines in the PoR system, this great-circle azimuth is only a approximation of the true (small-circle) azimuth.

Examples

```

data("nuvel1")
na_pa <- subset(nuvel1, nuvel1$plate.rot == "na")

data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")

data("san_andreas")
res <- projected_pb_strike(
  x = san_andreas, PoR = na_pa, pb = plate_boundary, tangential = TRUE
)
head(res)
head(san_andreas$azi - res) # beta angle

```

quick_plot

Plotting Stress Analysis Results

Description

Creates a set of plots including the azimuth as a function of the distance to the plate boundary, the Norm Chi-squared as a function of the distance to the plate boundary, the circular distance (and dispersion) a function of the distance to the plate boundary, a von-Mises QQ plot, and a rose diagram of the quality-weighted frequency distribution of the azimuths.

Usage

```
quick_plot(azi, distance, prd, unc = NULL, regime, width = 51)
```

Arguments

azi	numeric. Azimuth of σ_{Hmax}
distance	numeric. Distance to plate boundary
prd	numeric. the predicted direction of σ_{Hmax}
unc	numeric. Uncertainty of observed σ_{Hmax} , either a numeric vector or a number
regime	character vector. The stress regime (following the classification of the World Stress Map)
width	integer. window width (in number of observations) for moving average of the azimuths, circular dispersion, and Norm Chi-square statistics. If NULL, an optimal width will be estimated.

Details

Plot 1 shows the transformed azimuths as a function of the distance to the plate boundary. The red line indicates the rolling circular mean, stippled red lines indicate the 95% confidence interval about the mean.

Plot 2 shows the normalized χ^2 statistics as a function of the distance to the plate boundary. The red line shows the rolling χ^2 statistic.

Plot 3 shows the circular distance of the transformed azimuths to the predicted azimuth, as a function of the distance to the plate boundary. The red line shows the rolling circular dispersion about the prediction.

Plot 4 give the rose diagram of the transformed azimuths.

Value

four R base plots

See Also

[PoR_shmax\(\)](#), [distance_from_pb\(\)](#), [circular_mean\(\)](#), [circular_dispersion\(\)](#), [confidence_interval_fisher\(\)](#), [norm_chisq\(\)](#), [weighted_rayleigh\(\)](#), [vm_qqplot\(\)](#)

Examples

```
data("nuvel1")
na_pa <- subset(nuvel1, nuvel1$plate.rot == "na")

data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")

data("san_andreas")
res <- PoR_shmax(san_andreas, na_pa, "right")
d <- distance_from_pb(san_andreas, na_pa, plate_boundary, tangential = TRUE)
quick_plot(res$azi.PoR,
  distance = d, prd = res$prd, unc = san_andreas$unc,
  regime = san_andreas$regime
)
```

rayleigh_test

Rayleigh Test of Circular Uniformity

Description

Performs a Rayleigh test for uniformity of circular/directional data by assessing the significance of the mean resultant length.

Usage

```
rayleigh_test(x, mu = NULL, axial = TRUE, quiet = FALSE)
```

Arguments

x	numeric vector. Values in degrees
mu	(optional) The specified or known mean direction (in degrees) in alternative hypothesis
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
quiet	logical. Prints the test's decision.

Details

H_0 : angles are randomly distributed around the circle.

H_1 : angles are from unimodal distribution with unknown mean direction and mean resultant length (when mu is NULL. Alternatively (when mu is specified), angles are uniformly distributed around a specified direction.

If `statistic > p.value`, the null hypothesis is rejected, i.e. the length of the mean resultant differs significantly from zero, and the angles are not randomly distributed.

Value

a list with the components:

R or **C** mean resultant length or the dispersion (if mu is specified). Small values of R (large values of C) will reject uniformity. Negative values of C indicate that vectors point in opposite directions (also lead to rejection).

`statistic` test statistic

`p.value` significance level of the test statistic

Note

Although the Rayleigh test is consistent against (non-uniform) von Mises alternatives, it is not consistent against alternatives with $p = 0$ (in particular, distributions with antipodal symmetry, i.e. axial data). Tests of non-uniformity which are consistent against all alternatives include Kuiper's test (`kuiper_test()`) and Watson's U^2 test (`watson_test()`).

References

Mardia and Jupp (2000). Directional Statistics. John Wiley and Sons.

Wilkie (1983): Rayleigh Test for Randomness of Circular Data. Appl. Statist. 32, No. 3, pp. 311-312

Jammalamadaka, S. Rao and Sengupta, A. (2001). Topics in Circular Statistics, Sections 3.3.3 and 3.4.1, World Scientific Press, Singapore.

See Also

[mean_resultant_length\(\)](#), [circular_mean\(\)](#), [norm_chisq\(\)](#), [kuiper_test\(\)](#), [watson_test\(\)](#), [weighted_rayleigh\(\)](#)

Examples

```
# Example data from Mardia and Jupp (2001), pp. 93
pidgeon_homing <- c(55, 60, 65, 95, 100, 110, 260, 275, 285, 295)
rayleigh_test(pidgeon_homing, axial = FALSE)

# Example data from Davis (1986), pp. 316
finland_stria <- c(
  23, 27, 53, 58, 64, 83, 85, 88, 93, 99, 100, 105, 113,
  113, 114, 117, 121, 123, 125, 126, 126, 126, 127, 127, 128, 128, 129, 132,
  132, 132, 134, 135, 137, 144, 145, 145, 146, 153, 155, 155, 155, 157, 163,
  165, 171, 172, 179, 181, 186, 190, 212
)
rayleigh_test(finland_stria, axial = FALSE)
rayleigh_test(finland_stria, mu = 105, axial = FALSE)

# Example data from Mardia and Jupp (2001), pp. 99
atomic_weight <- c(
  rep(0, 12), rep(3.6, 1), rep(36, 6), rep(72, 1),
  rep(108, 2), rep(169.2, 1), rep(324, 1)
)
rayleigh_test(atomic_weight, 0, axial = FALSE)

# San Andreas Fault Data:
data(san_andreas)
rayleigh_test(san_andreas$azi)
data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
rayleigh_test(sa.por$azi.PoR, mu = 135)
```

relative_rotation	<i>Relative rotation between two rotations</i>
-------------------	--

Description

Calculates the relative rotation between two rotations, i.e. the difference from rotation 1 to rotation 2.

Usage

```
relative_rotation(r1, r2)
```

Arguments

r1, r2 Objects of class "euler.pole". First rotation is r1, followed rotation r2.

Value

list. Euler axes (geographical coordinates) and Euler angles (in degrees)

References

Schaeben, H., Kroner, U. and Stephan, T. (2021). Euler Poles of Tectonic Plates. In B. S. Daza Sagar, Q. Cheng, J. McKinley and F. Agterberg (Eds.), *Encyclopedia of Mathematical Geosciences. Encyclopedia of Earth Sciences Series* (pp. 1–7). Springer Nature Switzerland AG 2021. doi: 10.1007/978-3-030-26050-7_435-1.

See Also

`euler_pole()` for class "euler.pole"

Examples

```
a <- euler_pole(90, 0, angle = 45)
b <- euler_pole(0, 0, 1, geo = FALSE, angle = -15)
relative_rotation(a, b)
relative_rotation(b, a)
```

rolling_test

Apply Rolling Functions using Circular Statistical Tests for Uniformity

Description

A generic function for applying a function to rolling margins of an array.

Usage

```
roll_normchisq(
  obs,
  prd,
  unc = NULL,
  width = NULL,
  by.column = FALSE,
  partial = TRUE,
  fill = NA,
  ...
)
```

```
roll_rayleigh(
  obs,
  prd,
  unc = NULL,
  width = NULL,
  by.column = FALSE,
  partial = TRUE,
  fill = NA,
  ...
)
```

```
roll_dispersion(  
  x,  
  y,  
  w = NULL,  
  w.y = NULL,  
  width = NULL,  
  by.column = FALSE,  
  partial = TRUE,  
  fill = NA,  
  ...  
)
```

```
roll_confidence(  
  x,  
  conf.level = 0.95,  
  w = NULL,  
  axial = TRUE,  
  width = NULL,  
  by.column = FALSE,  
  partial = TRUE,  
  fill = NA,  
  ...  
)
```

```
roll_dispersion_CI(  
  x,  
  y,  
  w = NULL,  
  w.y = NULL,  
  R,  
  conf.level = 0.95,  
  width = NULL,  
  by.column = FALSE,  
  partial = TRUE,  
  fill = NA,  
  ...  
)
```

```
roll_dispersion_sde(  
  x,  
  y,  
  w = NULL,  
  w.y = NULL,  
  R,  
  conf.level = 0.95,  
  width = NULL,  
  by.column = FALSE,
```

```

    partial = TRUE,
    fill = NA,
    ...
)

```

Arguments

obs	Numeric vector containing the observed azimuth of σ_{Hmax} , same length as prd
prd	Numeric vector containing the modeled azimuths of σ_{Hmax} , i.e. the return object from <code>model_shmax()</code>
unc	Uncertainty of observed σ_{Hmax} , either a numeric vector or a number
width	integer specifying the window width (in numbers of observations) which is aligned to the original sample according to the <code>align</code> argument. If NULL, an optimal width is estimated.
by.column	logical. If TRUE, FUN is applied to each column separately.
partial	logical or numeric. If FALSE then FUN is only applied when all indexes of the rolling window are within the observed time range. If TRUE (default), then the subset of indexes that are in range are passed to FUN. A numeric argument to partial can be used to determine the minimal window size for partial computations. See below for more details.
fill	a three-component vector or list (recycled otherwise) providing filling values at the left/within/to the right of the data range. See the <code>fill</code> argument of <code>zoo::na.fill()</code> for details
...	optional arguments passed to <code>zoo::rollapply()</code>
x, y	numeric. Directions in degrees
w, w.y	(optional) Weights of x and y, respectively. A vector of positive numbers and of the same length as x.
conf.level	Level of confidence: $(1 - \alpha\%)/100$. (0.95 by default).
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
R	The number of bootstrap replicates.

Value

numeric vector with the test statistic of the rolling test. `roll_dispersion_CI` returns a 2-column matrix with the lower and the upper confidence limits

Note

If the rolling functions are applied to values that are a function of distance it is recommended to sort the values first.

Examples

```

data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")
data("san_andreas")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
distance <- distance_from_pb(
  x = san_andreas,
  PoR = PoR,
  pb = plate_boundary,
  tangential = TRUE
)
dat <- san_andreas[order(distance), ]
dat.PoR <- PoR_shmax(san_andreas, PoR, "right")
roll_normchisq(dat.PoR$azi.PoR, 135, dat$unc) |> head()
roll_rayleigh(dat.PoR$azi.PoR, prd = 135, unc = dat$unc) |> head()
roll_dispersion(dat.PoR$azi.PoR, y = 135, w = 1 / dat$unc) |> head()
roll_confidence(dat.PoR$azi.PoR, w = 1 / dat$unc) |> head()

roll_dispersion_CI(dat.PoR$azi.PoR, y = 135, w = 1 / dat$unc, R = 10) |> head()

```

roll_circstats

*Apply Rolling Functions using Circular Statistics***Description**

A generic function for applying a function to rolling margins of an array.

Usage

```

roll_circstats(
  x,
  w = NULL,
  FUN,
  axial = TRUE,
  na.rm = TRUE,
  width = NULL,
  by.column = FALSE,
  partial = TRUE,
  fill = NA,
  ...
)

```

Arguments

x numeric vector. Values in degrees.

w (optional) Weights. A vector of positive numbers and of the same length as **x**.

FUN the function to be applied

axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.
width	integer specifying the window width (in numbers of observations) which is aligned to the original sample according to the align argument. If NULL, an optimal width is calculated.
by.column	logical. If TRUE, FUN is applied to each column separately.
partial	logical or numeric. If FALSE then FUN is only applied when all indexes of the rolling window are within the observed time range. If TRUE (default), then the subset of indexes that are in range are passed to FUN. A numeric argument to partial can be used to determine the minimal window size for partial computations. See below for more details.
fill	a three-component vector or list (recycled otherwise) providing filling values at the left/within/to the right of the data range. See the fill argument of <code>zoo::na.fill()</code> for details
...	optional arguments passed to <code>zoo::rollapply()</code>

Value

numeric vector with the results of the rolling function.

Note

If the rolling statistics are applied to values that are a function of distance it is recommended to sort the values first.

Examples

```
data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")
data("san_andreas")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
distance <- distance_from_pb(
  x = san_andreas,
  PoR = PoR,
  pb = plate_boundary,
  tangential = TRUE
)
dat <- san_andreas[order(distance), ]
roll_circstats(dat$aзи, w = 1 / dat$unc, circular_mean, width = 51) |> head()
```

rose	<i>Rose Diagram</i>
------	---------------------

Description

Plots a rose diagram (rose of directions), the analogue of a histogram or density plot for angular data.

Usage

```
rose(  
  x,  
  weights = NULL,  
  binwidth = NULL,  
  bins = NULL,  
  axial = TRUE,  
  equal_area = TRUE,  
  muci = TRUE,  
  round_binwidth = 0,  
  mtext = "N",  
  main = NULL,  
  sub = NULL,  
  at = seq(0, 360 - 45, 45),  
  cborder = TRUE,  
  labels = TRUE,  
  col = "grey",  
  dots = FALSE,  
  dot_pch = 1,  
  dot_cex = 1,  
  dot_col = "slategrey",  
  stack = FALSE,  
  jitter_factor = 0,  
  grid = FALSE,  
  grid.lines = seq(0, 135, 45),  
  grid.circles = seq(0.2, 1, 0.2),  
  add = FALSE,  
  ...  
)
```

Arguments

x	Data to be plotted. A numeric vector containing angles (in degrees).
weights	Optional vector of numeric weights associated with x.
binwidth	The width of the bins (in degrees).
bins	number of arcs to partition the circle width. Overridden by binwidth.
axial	Logical. Whether data are uniaxial (<code>axial=FALSE</code>) or biaxial (<code>TRUE</code> , the default).

<code>equal_area</code>	Logical. Whether the radii of the bins are proportional to the frequencies (<code>equal_area=FALSE</code> , i.e. equal-angle) or proportional to the square-root of the frequencies (<code>equal_area=TRUE</code> , the default).
<code>muci</code>	logical. Whether the mean and its 95% CI are added to the plot or not.
<code>round_binwidth</code>	integer. Number of decimal places of bin width (0 by default).
<code>mtext</code>	character. String to be drawn at the top margin of the plot ("N" by default)
<code>main, sub</code>	Character string specifying the title and subtitle of the plot. If <code>sub = NULL</code> , it will show the bin width.
<code>at</code>	Optional vector of angles at which tick marks should be plotted. Set <code>at=numeric(0)</code> to suppress tick marks.
<code>cborder</code>	logical. Border of rose plot.
<code>labels</code>	Either a logical value indicating whether to plot labels next to the tick marks, or a vector of labels for the tick marks.
<code>col</code>	fill color of bins
<code>dots</code>	logical. Whether a circular dot plot should be added (FALSE is the default).
<code>dot_cex, dot_pch, dot_col</code>	Plotting arguments for circular dot plot
<code>stack</code>	logical. Groups and stacks the dots if TRUE. Default is FALSE.
<code>jitter_factor</code>	Add a small amount of noise to the angles' radius that is added to scale. Jitter is ignored when <code>stack==TRUE</code>). If 0, no jitter is added (by default); if negative, the points fall into the circle.
<code>grid</code>	logical. Whether to add a grid. Default is FALSE.
<code>grid.lines, grid.circles</code>	numeric. Adds a sequence of straight grid lines and circles based on angles and radii, respectively. Ignored when <code>grid=FALSE</code>
<code>add</code>	logical.
<code>...</code>	Additional arguments passed to <code>spatstat.explore::rose()</code> .

Value

A window (class "owin") containing the plotted region or a list of the calculated frequencies.

Note

If bins and binwidth are NULL, an optimal bin width will be calculated using Scott (1979):

$$w_b = \frac{R}{n^{\frac{1}{3}}}$$

with n being the length of x, and the range R being either 180 or 360 degree for axial or directional data, respectively.

If "axial" == TRUE, the binwidth is adjusted to guarantee symmetrical fans.

Examples

```
x <- rvm(100, mean = 90, k = 5)
rose(x, axial = FALSE, border = TRUE, grid = TRUE)

data("san_andreas")
rose(san_andreas$azi, main = "equal area")
rose(san_andreas$azi, equal_area = FALSE, main = "equal angle")

# weighted frequencies:
rose(san_andreas$azi, weights = 1 / san_andreas$unc, main = "weighted")

# add dots:
rose(san_andreas$azi, dots = TRUE, main = "dot plot", jitter = .2)

# stack dots:
rose(san_andreas$azi,
     dots = TRUE, stack = TRUE, dot_cex = 0.5, dot_pch = 21,
     main = "stacked dot plot"
)
```

rose_geom

Direction Lines and Fans in Circular Diagram

Description

Direction Lines and Fans in Circular Diagram

Usage

```
rose_line(x, radius = 1, axial = TRUE, add = TRUE, ...)
```

```
rose_fan(x, d, radius = 1, axial = TRUE, add = TRUE, ...)
```

Arguments

x	angles in degrees
radius	of the plotted circle
axial	Logical. Whether x are uniaxial (axial=FALSE) or biaxial (TRUE, the default).
add	logical. Add to existing plot?
...	optional arguments passed to <code>graphics::segments()</code> or <code>graphics::polygon()</code>
d	width of a fan (in degrees)

Value

No return value, called for side effects

Examples

```

angles <- c(0, 10, 45)
radius <- c(.7, 1, .2)
lwd <- c(2, 1, .75)
col <- c(1, 2, 3)
rose_line(angles, radius = radius, axial = FALSE, add = FALSE, lwd = lwd, col = col)

```

rose_stats

Show Average Direction and Spread in Rose Diagram

Description

Adds the average direction (and its spread) to an existing rose diagram.

Usage

```

rose_stats(
  x,
  weights = NULL,
  axial = TRUE,
  avg = c("mean", "median", "sample_median"),
  spread = c("CI", "fisher", "sd", "IQR", "mdev"),
  f = 1,
  avg.col = "#B63679FF",
  avg.lty = 2,
  avg.lwd = 1.5,
  spread.col = ggplot2::alpha("#B63679FF", 0.2),
  spread.border = FALSE,
  spread.lty = NULL,
  spread.lwd = NULL,
  add = TRUE,
  ...
)

```

Arguments

x	Data to be plotted. A numeric vector containing angles (in degrees).
weights	Optional vector of numeric weights associated with x.
axial	Logical. Whether data are uniaxial (<code>axial=FALSE</code>) or biaxial (<code>TRUE</code> , the default).
avg	character. The average estimate for x. Either the circular mean ("mean", the default), the circular Quasi Median ("median"), or the sample median ("sample_median").
spread	character. The measure of spread to be plotted as a fan. Either 95% confidence interval ("CI", the default), Fishers confidence interval ("fisher"), the circular standard deviation ("sd"), the Quasi interquartile range on the circle ("IQR"), or the sample median deviation ("mdev"). NULL if no fan should be drawn.
f	factor applied on spread. 1 by default.

avg.col	color for the average line
avg.lty	line type of the average line
avg.lwd	line width of the average line
spread.col	color of the spread fan
spread.border	logical. Whether to draw a border of the fan or not.
spread.lty	line type of the spread fan's border
spread.lwd	line width of the spread fan's border
add	logical.
...	optional arguments to <code>circular_plot()</code> if <code>add</code> is <code>FALSE</code> .

Value

No return value, called for side effects

See Also

[rose\(\)](#) for plotting the rose diagram, and [circular_mean\(\)](#), [circular_median\(\)](#), [circular_sample_median\(\)](#), [confidence_interval\(\)](#), [confidence_interval_fisher\(\)](#), [circular_sd\(\)](#), [circular_IQR\(\)](#), [circular_sample_median_deviation\(\)](#) for statistical parameters.

Examples

```
data("san_andreas")
rose(san_andreas$azi, weights = 1 / san_andreas$unc, mucj = FALSE)
rose_stats(san_andreas$azi, weights = 1 / san_andreas$unc, avg = "sample_median", spread = "mdev")
```

sample_median

Circular Sample Median and Deviation

Description

Sample median direction for a vector of circular data

Usage

```
circular_sample_median(x, axial = TRUE, na.rm = TRUE)
```

```
circular_sample_median_deviation(x, axial = TRUE, na.rm = TRUE)
```

Arguments

x	numeric vector. Values in degrees.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Value

numeric

References

N.I. Fisher (1993) *Statistical Analysis of Circular Data*, Cambridge University Press.

Examples

```
set.seed(1)
x <- rvm(n = 100, mean = 0, kappa = 10)
circular_sample_median(x)
circular_sample_median_deviation(x)

data("san_andreas")
circular_sample_median(san_andreas$azi)
circular_sample_median_deviation(san_andreas$azi)
```

second_central_moment *Second Central Momentum*

Description

Measures the skewness (a measure of the asymmetry of the probability distribution) and the kurtosis (measure of the "tailedness" of the probability distribution). Standardized versions are the skewness and kurtosis normalized by the mean resultant length, Mardia 1972).

Usage

```
second_central_moment(x, w = NULL, axial = TRUE, na.rm = FALSE)
```

Arguments

x	numeric vector. Values in degrees.
w	(optional) Weights. A vector of positive numbers and of the same length as x.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
na.rm	logical value indicating whether NA values in x should be stripped before the computation proceeds.

Details

Negative values of skewness indicate skewed data in counterclockwise direction.

Large kurtosis values indicate tailed, values close to 0 indicate packed data.

Value

list containing

skewness second central sine momentum, i.e. the skewness

std_skewness standardized skewness

kurtosis second central cosine momentum, i.e. the kurtosis

std_kurtosis standardized kurtosis

Examples

```
data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
second_central_moment(sa.por$azi.PoR)
second_central_moment(sa.por$azi.PoR, w = 1 / san_andreas$unc)
```

spec_atan

Quadrant-specific inverse of the tangent

Description

Returns the quadrant specific inverse of the tangent

Usage

```
atan2_spec(x, y)
```

```
atan2d_spec(x, y)
```

Arguments

x, y dividend and divisor that comprise the sum of sines and cosines, respectively.

Value

numeric.

References

Jammalamadaka, S. Rao, and Ambar Sengupta (2001). Topics in circular statistics. Vol. 5. world scientific.

spherical_angle	<i>Angle along great circle on spherical surface</i>
-----------------	--

Description

Smallest angle between two points on the surface of a sphere, measured along the surface of the sphere

Usage

```
orthodrome(lat1, lon1, lat2, lon2)
```

```
haversine(lat1, lon1, lat2, lon2)
```

```
vincenty(lat1, lon1, lat2, lon2)
```

Arguments

lat1, lat2 numeric vector. latitudes of point 1 and 2 (in radians)

lon1, lon2 numeric vector. longitudes of point 1 and 2 (in radians)

Details

"orthodrome" based on the spherical law of cosines

"haversine" uses haversine formula that is optimized for 64-bit floating-point numbers

"vincenty" uses Vincenty formula for an ellipsoid with equal major and minor axes

Value

numeric. angle in radians

References

- Imboden, C. & Imboden, D. (1972). Formel fuer Orthodrome und Loxodrome bei der Berechnung von Richtung und Distanz zwischen Beringungs- und Wiederfundort. *Die Vogelwarte* **26**, 336-346.
- Sinnott, Roger W. (1984). Virtues of the Haversine. *Sky and telescope* **68**(2), 158. Vincenty, T. (1975). Direct and inverse solutions of geodesics on the ellipsoid with application of nested equations. *Survey Review*, **23**(176), 88-93. doi:10.1179/sre.1975.23.176.88.
- <http://www.movable-type.co.uk/scripts/latlong.html>
- <http://www.edwilliams.org/avform147.htm>

Examples

```

berlin <- c(52.52, 13.41) |> deg2rad()
calgary <- c(51.04, -114.072) |> deg2rad()
orthodrome(berlin[1], berlin[2], calgary[1], calgary[2])
haversine(berlin[1], berlin[2], calgary[1], calgary[2])
vincenty(berlin[1], berlin[2], calgary[1], calgary[2])

```

stress2grid

Spatial Interpolation of SHmax

Description

Stress field interpolation and wavelength analysis using a kernel (weighted) mean/median and standard deviation/IQR of stress data

Usage

```

stress2grid(
  x,
  stat = c("mean", "median"),
  grid = NULL,
  lon_range = NULL,
  lat_range = NULL,
  gridsize = 2,
  min_data = 3L,
  threshold = 25,
  arte_thres = 200,
  method_weighting = FALSE,
  quality_weighting = TRUE,
  dist_weight = c("inverse", "linear", "none"),
  idp = 1,
  qp = 1,
  mp = 1,
  dist_threshold = 0.1,
  R_range = seq(50, 1000, 50),
  ...
)

```

```

stress2grid_stats(
  x,
  grid = NULL,
  lon_range = NULL,
  lat_range = NULL,
  gridsize = 2,
  min_data = 4L,
  threshold = 25,
  arte_thres = 200,

```

```

method_weighting = FALSE,
quality_weighting = TRUE,
dist_weight = c("inverse", "linear", "none"),
idp = 1,
qp = 1,
mp = 1,
dist_threshold = 0.1,
R_range = seq(50, 1000, 50),
kappa = NULL,
...
)

```

Arguments

<code>x</code>	sf object containing azi SHmax in degree unc (optional) Uncertainties of SHmax in degree type (optional) Methods used for the determination of the direction of SHmax
<code>stat</code>	whether the direction of interpolated SHmax is based on the circular mean and standard deviation ("mean", the default) or the circular median and interquartile range ("median")
<code>grid</code>	(optional) Point object of class sf.
<code>lon_range, lat_range</code>	(optional) numeric vector specifying the minimum and maximum longitudes and latitudes (ignored if <code>grid</code> is specified).
<code>gridsize</code>	numeric. Target spacing of the regular grid in decimal degree. Default is 2.5. (is ignored if <code>grid</code> is specified)
<code>min_data</code>	integer. Minimum number of data per bin. Default is 3 for <code>stress2grid()</code> and 4 for <code>stress2grid_stats()</code> .
<code>threshold</code>	numeric. Threshold for deviation of direction. Default is 25
<code>arte_thres</code>	numeric. Maximum distance (in km) of the grid point to the next data point. Default is 200
<code>method_weighting</code>	logical. If a method weighting should be applied: Default is FALSE. If FALSE, overwrites <code>mp</code> .
<code>quality_weighting</code>	logical. If a quality weighting should be applied: Default is TRUE. If FALSE, overwrites <code>qp</code> .
<code>dist_weight</code>	Distance weighting method which should be used. One of "none", "linear", or "inverse" (the default).
<code>idp, qp, mp</code>	numeric. The weighting power of inverse distance, quality and method. Default is 1. The higher the value, the more weight it will put. When set to 0, no weighting is applied. <code>idp</code> is only effective if inverse distance weighting (<code>dist_weight="inverse"</code>) is applied.
<code>dist_threshold</code>	numeric. Distance weight to prevent overweight of data nearby (0 to 1). Default is 0.1

R_range	numeric value or vector specifying the kernel half-width(s), i.e. the search radius (in km). Default is seq(50, 1000, 50)
...	(optional) arguments to dist_greatcircle()
kappa	numeric. von Mises distribution concentration parameter used for the circular mode. Will be estimated using est.kappa() if not provided.

Details

[stress2grid\(\)](#) is a modified version of the MATLAB script "stress2grid" by Ziegler and Heidbach (2019). [stress2grid_stats\(\)](#) is based on [stress2grid\(\)](#) but yields more circular summary statistics (see [circular_summary\(\)](#)).

Value

sf object containing

lon,lat longitude and latitude in degrees

azi Mean SHmax in degree

sd Standard deviation of SHmax in degrees

R Search radius in km

mdr Mean distance of datapoints per search radius

N Number of data points in search radius

When [stress2grid_stats\(\)](#), **azi** and **sd** are replaced by the output of [circular_summary\(\)](#).

Source

<https://github.com/MorZieg/Stress2Grid>

References

Ziegler, M. and Heidbach, O. (2019). Matlab Script Stress2Grid v1.1. GFZ Data Services. [doi:10.5880/wsm.2019.002](https://doi.org/10.5880/wsm.2019.002)

See Also

[dist_greatcircle\(\)](#), [PoR_stress2grid\(\)](#), [compact_grid\(\)](#), [circular_mean\(\)](#), [circular_median\(\)](#), [circular_sd\(\)](#), [circular_summary\(\)](#)

Examples

```
data("san_andreas")
stress2grid(san_andreas, stat = "median")
## Not run:
stress2grid_stats(san_andreas)

## End(Not run)
```

stress_analysis *Quick analysis of a stress data set*

Description

Returns the converted azimuths, distances to the plate boundary, statistics of the model, and some plots.

Usage

```
stress_analysis(
  x,
  PoR,
  type = c("none", "in", "out", "right", "left"),
  pb,
  plot = TRUE,
  ...
)
```

Arguments

x	data.frame or sf object containing the coordinates of the point(s) (lat, lon), the direction of σ_{Hmax} azi and its standard deviation unc (optional)
PoR	Pole of Rotation. data.frame or object of class "euler.pole" containing the geographical coordinates of the Euler pole
type	Character. Type of plate boundary (optional). Can be "out", "in", "right", or "left" for outward, inward, right-lateral, or left-lateral moving plate boundaries, respectively. If "none" (the default), only the PoR-equivalent azimuth is returned.
pb	(optional) sf object of the plate boundary geometries in the geographical coordinate system
plot	(logical). Whether to produce a plot additional to output.
...	optional arguments to distance_from_pb()

Value

list containing the following values:

results data.frame showing the the coordinate and azimuth conversions (lat.PoR, lon.PoR, and azi.PoR), the predicted azimuths (prd), deviation angle from predicted (dev), circular distance (cdist), misfit to predicted stress direction (nchisq) and, if given, distance to tested plate boundary (distance)

stats array with circular (weighted) mean, circular standard deviation, circular variance, circular median, skewness, kurtosis, the 95% confidence angle, circular dispersion, and the normalized Chi-squared test statistic

test list containing the test results of the (weighted) Rayleigh test against the uniform distribution about the predicted orientation.

See Also

[PoR_shmax\(\)](#), [distance_from_pb\(\)](#), [norm_chisq\(\)](#), [quick_plot\(\)](#), [circular_summary\(\)](#)

Examples

```
data("nuvel1")
na_pa <- subset(nuvel1, nuvel1$plate.rot == "na")

data("plates")
plate_boundary <- subset(plates, plates$pair == "na-pa")

data("san_andreas")
stress_analysis(san_andreas, na_pa, type = "right", plate_boundary, plot = TRUE)
```

stress_colors	<i>Color palette for stress regime</i>
---------------	--

Description

Color palette for stress regime

Usage

```
stress_colors()
```

Value

function

Examples

```
stress_colors()
```

stress_data	<i>Example crustal stress dataset</i>
-------------	---------------------------------------

Description

Subsets of the World Stress Map (WSM) compilation of information on the crustal present-day stress field (Version 1.1. 2019).

Usage

```
data('san_andreas')
```

```
data('tibet')
```

```
data('iceland')
```

Format

A sf object / data.frame with 10 columns. Each row represents a different in-situ stress measurement:

id Measurement identifier

lat latitude in degrees

lon longitude in degrees

azi SHmax azimuth in degrees

unc MMeasurement standard deviation (in degrees)

type Type of measurement

depth Depth in km

quality WSM quality rank

regime Stress regime

An object of class sf (inherits from data.frame) with 1126 rows and 10 columns.

An object of class sf (inherits from data.frame) with 1165 rows and 10 columns.

An object of class sf (inherits from data.frame) with 490 rows and 10 columns.

Details

'san_andreas' contains 407 stress data adjacent to the San Andreas Fault to be tested against a tangentially displaced plate boundary.

"tibet" contains 947 stress data from the Himalaya and Tibetan plateau to be tested against an inward-moving displaced plate boundary.

'iceland' contains 201 stress data from Iceland to be tested against a outward-moving displaced plate boundary.

Source

<https://www.world-stress-map.org/>

References

Heidbach, O., M. Rajabi, X. Cui, K. Fuchs, B. Müller, J. Reinecker, K. Reiter, M. Tingay, F. Wenzel, F. Xie, M. O. Ziegler, M.-L. Zoback, and M. D. Zoback (2018): The World Stress Map database release 2016: Crustal stress pattern across scales. *Tectonophysics*, **744**, 484-498, doi:10.1016/j.tecto.2018.07.007.

See Also

[download_WSM2016\(\)](#) for description of columns and stress regime acronyms

Examples

```
data("san_andreas")
head(san_andreas)
```

```
data("tiber")
head(tiber)
```

```
data("iceland")
head(iceland)
```

stress_paths

Theoretical Plate Tectonic Stress Paths

Description

Construct σ_{Hmax} lines that are following small circles, great circles, or loxodromes of an Euler pole for the relative plate motion.

Usage

```
eulerpole_paths(x, type = c("sc", "gc", "ld"), n = 10, angle = 45, cw)
```

```
eulerpole_smallcircles(x, n = 10)
```

```
eulerpole_greatcircles(x, n = 10)
```

```
eulerpole_loxodromes(x, n = 10, angle = 45, cw)
```

Arguments

x	Either an object of class "euler.pole" or "data.frame" containing coordinates of Euler pole in lat, lon, and rotation angle (optional).
type	Character string specifying the type of curves to export. Either "sm" for small circles (default), "gc" for great circles, or "ld" for loxodromes.
n	Number of equally spaced curves; n = 10 by default (angular distance between curves: 180 / n)
angle	Direction of loxodromes; angle = 45 by default.
cw	logical. Sense of loxodromes: TRUE for clockwise loxodromes (left-lateral displaced plate boundaries). FALSE for counterclockwise loxodromes (right-lateral displaced plate boundaries).

Details

Maximum horizontal stress can be aligned to three types of curves related to relative plate motion:

Small circles Lines that have a constant distance to the Euler pole. If `x` contains `angle`, output additionally gives absolute velocity on small circle (degree/Myr -> km/Myr).

Great circles Paths of the shortest distance between the Euler pole and its antipodal position.

Loxodromes Lines of constant bearing, i.e. curves cutting small circles at a constant angle.

Value

sf object

Author(s)

Tobias Stephan

Examples

```
data("nuvel1")
por <- subset(nuvel1, nuvel1$plate.rot == "na") # North America relative to
# Pacific plate

eulerpole_smallcircles(por)
eulerpole_greatcircles(por)
eulerpole_loxodromes(x = por, angle = 45, n = 10, cw = FALSE)
eulerpole_loxodromes(x = por, angle = 30, cw = TRUE)
eulerpole_smallcircles(data.frame(lat = 30, lon = 10))
```

superimposed_shmax *SHmax direction resulting from multiple plate boundaries*

Description

Calculates a σ_{Hmax} direction at given coordinates, sourced by multiple plate boundaries. This first-order approximation is the circular mean of the superimposed theoretical directions, weighted by the rotation rates of the underlying PoRs.

Usage

```
superimposed_shmax(df, PoRs, types, absolute = TRUE, PoR_weighting = NULL)
```

Arguments

<code>df</code>	data.frame containing the coordinates of the point(s) (<code>lat</code> , <code>lon</code>), and the direction of σ_{Hmax} <code>azi</code> (in degrees)
<code>PoRs</code>	multirow data.frame or "euler.pole" object that must contain <code>lat</code> , <code>lon</code> and <code>angle</code>

types	character vector with length equal to number of rows in PoRs. Type of plate boundary. Must be "out", "in", "right", or "left" for outward, inward, right-lateral, or left-lateral moving plate boundaries, respectively.
absolute	logical. Whether the resultant azimuth should be weighted using the absolute rotation at the points or the angular rotation of the PoRs.
PoR_weighting	(optional) numeric vector with length equal to number of rows in PoRs. Extra weightings for the used PoRs.

Value

two column vector. azi is the resultant azimuth in degrees / geographical CRS), R is the resultant length.

See Also

[model_shmax\(\)](#)

[superimposed_shmax_PB\(\)](#) for considering distances to plate boundaries

Examples

```
data(san_andreas)
data(nuve11)
pors <- subset(nuve11, plate.rot %in% c("eu", "na"))
res <- superimposed_shmax(san_andreas, pors, types = c("in", "right"), PoR_weighting = c(2, 1))
head(res)
```

superimposed_shmax_PB *SHmax direction resulting from multiple plate boundaries considering distance to plate boundaries*

Description

Calculates a σ_{Hmax} direction at given coordinates, sourced by multiple plate boundaries. This first-order approximation is the circular mean of the superimposed theoretical directions, weighted by the rotation rates of the underlying PoRs, the inverse distance to the plate boundaries, and the type of plate boundary.

Usage

```
superimposed_shmax_PB(
  x,
  pbs,
  model,
  rotation_weighting = TRUE,
  type_weights = c(divergent = 1, convergent = 3, transform_L = 2, transform_R = 2),
  idp = 1
)
```

Arguments

x	grid. An object of sf, sfc or 2-column matrix
pbs	plate boundaries. sf object
model	data.frame containing the Euler pole parameters. See equivalent_rotation() for details.
rotation_weighting	logical.
type_weights	named vector.
idp	numeric. Weighting power of inverse distance. The higher the number, the less impact far-distant boundaries have. When set to 0, no weighting is applied.

Value

two-column matrix. azi is the resultant azimuth (in degrees), R is the resultant length.

See Also

[superimposed_shmax\(\)](#)

Examples

```
na_grid <- sf::st_make_grid(san_andreas, what = "centers", cellsize = 1)
na_plate <- subset(plates, plateA == "na" | plateB == "na")
cpm <- cpm_models[["NNR-MORVEL56"]]

# make divergent to ridge-push:
na_plate <- transform(na_plate, type = ifelse(na_plate$pair == "eu-na", "convergent", type))

res <- superimposed_shmax_PB(na_grid, na_plate, model = cpm, idp = 2)
head(res)
```

tectonicr.colors *Colors for input variables*

Description

assigns colors to continuous or categorical values for plotting

Usage

```
tectonicr.colors(
  x,
  n = 10,
  pal = NULL,
  categorical = FALSE,
  na.value = "grey",
  ...
)
```

Arguments

<code>x</code>	values for color assignment
<code>n</code>	integer. number of colors for continuous colors (i.e. ‘categorical = FALSE’).
<code>pal</code>	either a named vector specifying the colors for categorical values, or a color function. If NULL, default colors are <code>RColorBrewer::brewer.pal()</code> (categorical = TRUE) and <code>viridis::viridis()</code> (categorical = FALSE).
<code>categorical</code>	logical.
<code>na.value</code>	color for NA values (categorical).
<code>...</code>	optional arguments passed to palette function

Value

named color vector

Examples

```
val1 <- c("N", "S", "T", "T", NA)
tectonicr.colors(val1, categorical = TRUE)
tectonicr.colors(val1, pal = stress_colors(), categorical = TRUE)

val2 <- runif(10)
tectonicr.colors(val2, n = 5)
```

vcross

Vector cross product

Description

Vector or cross product

Usage

```
vcross(x, y)
```

Arguments

<code>x, y</code>	numeric vectors of length 3
-------------------	-----------------------------

Value

numeric vector of length 3

Examples

```
vcross(c(1, 2, 3), c(4, 5, 6))
```

`vm_qqplot`*von Mises Quantile-Quantile Plot*

Description

Produces a Q-Q plot of the data against a specified von Mises distribution to graphically assess the goodness of fit of the model.

Usage

```
vm_qqplot(  
  x,  
  w = NULL,  
  axial = TRUE,  
  mean = NULL,  
  kappa = NULL,  
  xlab = "von Mises quantile function",  
  ylab = "Empirical quantile function",  
  main = "von Mises Q-Q Plot",  
  col = "#B63679FF",  
  add_line = TRUE,  
  ...  
)
```

Arguments

<code>x</code>	numeric. Angles in degrees
<code>w</code>	numeric. optional weightings for <code>x</code> to estimate mean and kappa.
<code>axial</code>	Logical. Whether data are uniaxial (<code>axial=FALSE</code>)
<code>mean</code>	numeric. Circular mean of the von Mises distribution. If <code>NULL</code> , it will be estimated from <code>x</code> .
<code>kappa</code>	numeric. Concentration parameter of the von Mises distribution. If <code>NULL</code> , it will be estimated from <code>x</code> .
<code>xlab, ylab, main</code>	plot labels.
<code>col</code>	color for the dots.
<code>add_line</code>	logical. Whether to connect the points by straight lines?
<code>...</code>	graphical parameters

Value

plot

Examples

```
# von Mises distribution
x_vm <- rvm(100, mean = 0, kappa = 4)
vm_qqplot(x_vm, axial = FALSE, pch = 20)

# uniform distribution
x_unif <- runif(100, 0, 360)
vm_qqplot(x_unif, axial = FALSE, pch = 20)
```

vonmises

*The von Mises Distribution***Description**

Density, probability distribution function, quantiles, and random generation for the circular normal distribution with mean and kappa.

Usage

```
rvm(n, mean, kappa)

dvm(theta, mean, kappa, log = FALSE, axial = FALSE)

pvm(theta, mean, kappa, from = NULL, tol = 1e-20)

qvm(p, mean = 0, kappa, from = NULL, tol = .Machine$double.eps^(0.6), ...)
```

Arguments

n	integer. Number of observations in degrees
mean	numeric. Mean angle in degrees
kappa	numeric. Concentration parameter in the range (0, Inf]
theta	numeric. Angular value in degrees
log	logical. If TRUE, probabilities p are given as log(p).
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or directional, i.e. 2π -periodical (FALSE).
from	if NULL is set to $\mu - \pi$. This is the value from which the pvm and qvm are evaluated. in degrees.
tol	numeric. The precision in evaluating the distribution function or the quantile.
p	numeric. Vector of probabilities with values in [0, 1].
...	parameters passed to <code>stats::integrate()</code> .

Value

dvm gives the density, pvm gives the probability of the von Mises distribution function, rvm generates random deviates (in degrees), and qvm provides quantiles (in degrees).

Examples

```

set.seed(1)
x <- rvm(5, mean = 90, kappa = 2)

dvm(x, mean = 90, kappa = 2)
dvm(x, mean = 90, kappa = 2, axial = TRUE)

pvm(x, mean = 90, kappa = 2)
qvm(c(.25, .5, .75), mean = 90, kappa = 2)

```

 watson_test

Watson's U^2 Test of Circular Uniformity

Description

Watson's test statistic is a rotation-invariant Cramer - von Mises test

Usage

```

watson_test(
  x,
  alpha = 0,
  dist = c("uniform", "vonmises"),
  axial = TRUE,
  mu = NULL,
  quiet = FALSE
)

```

Arguments

x	numeric vector. Values in degrees
alpha	Significance level of the test. Valid levels are 0.01, 0.05, and 0.1. This argument may be omitted (NULL, the default), in which case, a range for the p-value will be returned.
dist	Distribution to test for. The default, "uniform", is the uniform distribution. "vonmises" tests the von Mises distribution.
axial	logical. Whether the data are axial, i.e. π -periodical (TRUE, the default) or circular, i.e. 2π -periodical (FALSE).
mu	(optional) The specified mean direction (in degrees) in alternative hypothesis
quiet	logical. Prints the test's decision.

Details

If `statistic > p.value`, the null hypothesis is rejected. If not, randomness (uniform distribution) cannot be excluded.

Value

list containing the test statistic `statistic` and the significance level `p.value`.

References

Mardia and Jupp (2000). *Directional Statistics*. John Wiley and Sons.

Examples

```
# Example data from Mardia and Jupp (2001), pp. 93
pidgeon_homing <- c(55, 60, 65, 95, 100, 110, 260, 275, 285, 295)
watson_test(pidgeon_homing, alpha = .05)

# San Andreas Fault Data:
data(san_andreas)
data("nuvel1")
PoR <- subset(nuvel1, nuvel1$plate.rot == "na")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
watson_test(sa.por$azi.PoR, alpha = .05)
watson_test(sa.por$azi.PoR, alpha = .05, dist = "vonmises")
```

 weighted_rayleigh

Weighted Goodness-of-fit Test for Circular Data

Description

Weighted version of the Rayleigh test (or V0-test) for uniformity against a distribution with a priori expected von Mises concentration.

Usage

```
weighted_rayleigh(x, mu = NULL, w = NULL, axial = TRUE, quiet = FALSE)
```

Arguments

<code>x</code>	numeric vector. Values in degrees
<code>mu</code>	The <i>a priori</i> expected direction (in degrees) for the alternative hypothesis.
<code>w</code>	numeric vector weights of length <code>length(x)</code> . If <code>NULL</code> , the non-weighted Rayleigh test is performed.
<code>axial</code>	logical. Whether the data are axial, i.e. π -periodical (<code>TRUE</code> , the default) or directional, i.e. 2π -periodical (<code>FALSE</code>).
<code>quiet</code>	logical. Prints the test's decision.

Details

The Null hypothesis is uniformity (randomness). The alternative is a distribution with a (specified) mean direction (`mu`). If `statistic >= p.value`, the null hypothesis of randomness is rejected and angles derive from a distribution with a (or the specified) mean direction.

Value

a list with the components:

R or C mean resultant length or the dispersion (if μ is specified). Small values of R (large values of C) will reject uniformity. Negative values of C indicate that vectors point in opposite directions (also lead to rejection).

statistic Test statistic

p.value significance level of the test statistic

See Also

[rayleigh_test\(\)](#)

Examples

```
# Load data
data("cpm_models")
data(san_andreas)
PoR <- equivalent_rotation(cpm_models[["NNR-MORVEL56"]], "na", "pa")
sa.por <- PoR_shmax(san_andreas, PoR, "right")
data("iceland")
PoR.ice <- equivalent_rotation(cpm_models[["NNR-MORVEL56"]], "eu", "na")
ice.por <- PoR_shmax(iceland, PoR.ice, "out")
data("tibet")
PoR.tib <- equivalent_rotation(cpm_models[["NNR-MORVEL56"]], "eu", "in")
tibet.por <- PoR_shmax(tibet, PoR.tib, "in")

# GOF test:
weighted_rayleigh(tibet.por$azi.PoR, mu = 90, w = 1 / tibet$unc)
weighted_rayleigh(ice.por$azi.PoR, mu = 0, w = 1 / iceland$unc)
weighted_rayleigh(sa.por$azi.PoR, mu = 135, w = 1 / san_andreas$unc)
```

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