

Package ‘miLAG’

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Type Package

Title Calculates Microbial Lag Duration (on the Population Level) from Provided Growth Curve Data

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Description Microbial growth is often measured by growth curves i.e. a table of population sizes and times of measurements.

This package allows to use such growth curve data to determine the duration of “microbial lag phase” i.e. the time needed for microbes to restart divisions.

It implements the most commonly used methods to calculate the lag duration, these methods are discussed and described in Opalek et.al. 2022.

Citation: “How to determine microbial lag phase duration?”, M. Opalek, B. Smug, D. Wloch-Salamon (2022) <doi:10.1101/2022.11.16.516631>.

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calc_baranyi_fit_lag *calc_baranyi_fit_lag*

Description

Calculates lag based on fitting baranyi model to data

Usage

```
calc_baranyi_fit_lag(
  data,
  n0,
  init_lag = NULL,
  init_gr_rate = NULL,
  algorithm = "auto",
  max_iter = 100
)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass",and one optional column: "curve_id" This is data from may come from multiple growth curves
------	---

n0	a data frame describing initial biomass for each of the curves, i.e. it has two obligatory columns: "curve_id", "N0"
init_lag	initial value for the lag parameter, defaults to NULL in which case it will be approximated based on the data
init_gr_rate	initial value for the growth rate, defaults to NULL in which case it will be approximated based on the data
algorithm	eg. "auto", "Levenberg-Marquardt", "port", defaults to "auto"
max_iter	Maximum number of iterations, defaults to 100

Value

growth curve data with additional columns ('lag', and predicted biomass 'predicted')

calc_lag	<i>calc_lag</i>
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Description

The main function that calculates lags based on growth curve data, selected method and parameters and returns an extended growth rate data frame (extended by multiple columns with parameters related to lag calculation)

Usage

```
calc_lag(data, method, pars)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", and one optional column: "curve_id" This is data from may come from multiple growth curves
method	method of lag calculation, choose one of the following: "exponential", "biomass increase", "max growth acceleration", "parameter fitting to a model"
pars	a list of parameters. Get.default.parameters function can be used to get the default ones. Otherwise create your own list with the following names: - model: if method = "parameter fitting to a model", one of the following models needs to be chosen: "logistic", "baranyi" - n0_method: "first.observation" if the first point is taken as the initial biomass or "minimal.observation" if the minimal biomass is taken as the initial point. In "healthy" growth curves these options should be equivalent but sometimes a drop in OD/biomass is observed at the beginning of a growth curve. In this case it is not obvious what to assume the initial biomass is. - tangent_method "local.regression" (if the tangent is fitted to a number of points around the maximal growth rate) or "to.point" (if the tangent is fitted only to the point where the growth rate is maximal); defaults to "to.point" - threshold: A value of the biomass increase that we can surely associate with the end

of the lag phase rather than random variation durinh the lag. Defaults to 10^2
 - curve_points: if tangent.method = "local.regression" then curve_points is the number of points the line is fitted to; defaults to 3 i.e. the point with the maximal uptake rate one point before and one point after - init_gr_rate: if logistic model is fitted. Defaults to NULL in which case the initial value will be based on the data - init_lag: if a logistic model is fitted, Defaults to NULL in which case the initial value will be based on the data - algorithm: if method = "parameter fitting to a model", nls algorithm to run the model fit; defaults to "auto" which will choose the best between bounded and unbounded "Levenberg-Marquardt" and bounded "port" - max_iter = if method = "parameter fitting to a model", the maximum number of nls iterations, defaults to 100

Value

growth curve data (time, biomass, curve_id) with the following additional columns: log_biomass, lag, line_slope, line_intercept, lag_calc_method, predicted_data, diff, second_deriv_b, tangent_point, threshold

calc_lagistic_fit_lag *calc_lagistic_fit_lag*

Description

Calculates lag based on fitting logistic model to data

Usage

```
calc_lagistic_fit_lag(
  data,
  n0,
  init_gr_rate = NULL,
  init_K = NULL,
  init_lag = NULL,
  algorithm,
  max_iter,
  return_all_params = FALSE,
  min_b = 0.2,
  min_a = 0.8
)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", and one optional column: "curve_id" This is data from may come from multiple growth curves
n0	a data frame describing initial biomass for each of the curves, i.e. it has two obligatory columns: "curve_id", "N0"

init_gr_rate	initial value for the growth rate, defaults to NULL in which case it will be approximated based on the data
init_K	initial value for the saturation parameter K, defaults to NULL in which case it will be approximated based on the data
init_lag	initial value for the lag parameter, defaults to NULL in which case it will be approximated based on the data
algorithm	eg. "auto", "Levenberg-Marquardt", "port"
max_iter	Maximum number of iterations
return_all_params	defaults to FALSE, TRUE if you also want to get K and growth.rate apart from lag
min_b	defaults to 0.2; mina and minb define where to look for exponential phase: it will be where the biomass is between min + (max-min)*(lower.bound.for.gr TO upper.bound.for.gr)
min_a	defaults to 0.8

Value

growth curve data with additional columns ('lag', and predicted biomass 'predicted'), and the fitting object if return.all.params was set to TRUE

```
calc_lag_fit_to_baranyi_with_lag
      calc_lag_fit_to_baranyi_with_lag
```

Description

Runs nlsLM/nls algorithms with three different parameter setups to fit the best Logistic model parameters to our data and chooses the best model

Usage

```
calc_lag_fit_to_baranyi_with_lag(
  gr_curve,
  LOG10N0 = NULL,
  init_lag = NULL,
  init_mumax = NULL,
  init_LOG10Nmax = NULL,
  algorithm = "auto",
  max_iter = 100,
  lower_bound = c(0, 0, 0, 0)
)
```

Arguments

<code>gr_curve</code>	data from one specific growth curve with these two columns: time and biomass
<code>LOG10N0</code>	the decimal logarithm of initial biomass
<code>init_lag</code>	initial value for the lag parameter
<code>init_mumax</code>	initial value for the mumax parameter
<code>init_LOG10Nmax</code>	initial value for the LOG10Nmax parameter
<code>algorithm</code>	defaults to "auto" which chooses between bounded and unbounded Levenberg-Marquardt method and the bounded port method
<code>max_iter</code>	max. number of iterations; defaults to 100
<code>lower_bound</code>	lower bound for the bounded nls optimisation; defaults to 0

Value

lag and the nls fitting object with parameters fitted to logistic model

```
calc_lag_fit_to_logistic_with_lag
      calc_lag_fit_to_logistic_with_lag
```

Description

Runs nlsLM/nls algorithm of the user's choice to fit the Logistic model parameters to our data

Usage

```
calc_lag_fit_to_logistic_with_lag(
  gr_curve,
  n0,
  init_gr_rate = init_gr_rate,
  init_K = init_K,
  init_lag = init_lag,
  algorithm = "auto",
  max_iter = 100,
  lower_bound = c(0, 0, 0)
)
```

Arguments

<code>gr_curve</code>	data from one specific growth curve with these two columns: time and biomass
<code>n0</code>	the initial biomass
<code>init_gr_rate</code>	initial value for the growth rate
<code>init_K</code>	initial value for the saturation parameter K
<code>init_lag</code>	initial value for the lag parameter

algorithm	defaults to "auto" which chooses between bounded and unbounded Levenberg-Marquardt method and the bounded port method
max_iter	max. number of iterations; defaults to 100
lower_bound	lower bound for the bounded nls optimization; defaults to 0

Value

lag and the nls fitting object with parameters fitted to logistic model

```
choose_lag_fit_algorithm_baranyi
      choose_lag_fit_algorithm_baranyi
```

Description

Runs nlsLM/nls algorithms with three different parameter setups to fit the best Baranyi parameters to our data and chooses the best model

Usage

```
choose_lag_fit_algorithm_baranyi(
  gr_curve,
  LOG10N0,
  init_lag,
  init_mumax,
  init_LOG10Nmax,
  max_iter,
  lower_bound
)
```

Arguments

gr_curve	data from one specific growth curve with the following columns: LOG10N, t
LOG10N0	init value for the LOG10N0 parameter
init_lag	initial value for the lag
init_mumax	initial value for the mumax parameter
init_LOG10Nmax	initial value for the LOG10Nmax parameter
max_iter	max. number of iterations
lower_bound	lower bound for the bounded nls optimization;

Value

the best nls fitting object with parameters fitted to Baranyi model (lowest Res.Sum Sq provided that all coefficients are nonnegative)

```
choose_lag_fit_algorithm_logistic
      choose_lag_fit_algorithm_logistic
```

Description

Runs nlsLM/nls algorithms with three different parameter setups to fit the best Logistic model parameters to our data and chooses the best model

Usage

```
choose_lag_fit_algorithm_logistic(
  gr_curve,
  n0,
  init_gr_rate = init_gr_rate,
  init_K = init_K,
  init_lag = init_lag,
  max_iter = 100,
  lower_bound = c(0, 0, 0)
)
```

Arguments

<code>gr_curve</code>	data from one specific growth curve with the following columns: LOG10N, t
<code>n0</code>	the initial biomass
<code>init_gr_rate</code>	initial value for the growth rate
<code>init_K</code>	initial value for the saturation parameter K
<code>init_lag</code>	initial value for the lag parameter
<code>max_iter</code>	max. number of iterations; defaults to 100
<code>lower_bound</code>	lower bound for the bounded nls optimization; defaults to 0

Value

the best nls fitting object with parameters fitted to logistic model (lowest Res.Sum Sq provided that all coefficients are nonnegative)

compare_algorithms	<i>compare_algorithms</i>
--------------------	---------------------------

Description

Compares results of 3 objects obtained from running nls

Usage

```
compare_algorithms(nls_LM_no_bound, nls_PORT, nlsres_LM)
```

Arguments

nls_LM_no_bound	first object resulting from running nls
nls_PORT	second object resulting from running nls
nlsres_LM	third object resulting from running nls

Value

the best fitting object (lowest Res.Sum Sq provided that all coefficients are nonnegative)

cut_the_data	<i>cut_the_data</i> Subsets the data frame containing only the observations up to the specified maximum time
--------------	--

Description

cut_the_data Subsets the data frame containing only the observations up to the specified maximum time

Usage

```
cut_the_data(data, max_time)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", and one optional column: "curve_id" This is data from may come from multiple growth curves
max_time	max. time at which we want to cut the growth curve data

Value

cut data

 fit_exp_lag

fit_exp_lag

Description

Fits the lag to multiple growth curves based on the basic tangent method

Usage

```
fit_exp_lag(data, tangent_method, n0, curve_points = 3)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", and one optional column: "curve_id" This is data from may come from multiple growth curves
tangent_method	"local.regression" (if the tangent is fitted to a number of points around the maximal growth rate) or "to.point" (if the tangent is fitted only to the point where the growth rate is maximal); defaults to "to.point"
n0	the initial biomass (a tangent line crossing N0 line will determine the lag)
curve_points	if tangent_method = "local.regression" then curve_points is the number of points the line is fitted to; defaults to 3 i.e. the point with the maximal uptake rate one point before and one point after

Value

growth curve data (as input) together with additional columns: lag, line.intercept and line.slope

fit_exp_lag_to_curve

fit_exp_lag_to_curve

Description

Fits the lag to one growth curve based on the basic tangent method

Usage

```
fit_exp_lag_to_curve(data, n0, tangent_method = "to.point", curve_points = 3)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", This is data from one growth curve only, one (mean) observation per time
n0	the initial biomass (a tangent line crossing N0 line will determine the lag)
tangent_method	"local.regression" (if the tangent is fitted to a number of points around the maximal growth rate) or "to.point" (if the tangent is fitted only to the point where the growth rate is maximal); defaults to "to.point"
curve_points	if tangent_method = "local.regression" then curve_points is the number of points the line is fitted to; defaults to 3 i.e. the point with the maximal uptake rate one point before and one point after

Value

line_slope: slope of the tangent line, line_intercept: intercept of the tangent line, lag: lag, tangent_points: i.e a data frame of all points selected for fitting the line

fit_max_infl_lag	<i>fit_max_infl_lag</i>
------------------	-------------------------

Description

Fits the lag to multiple growth curves based on the max growth acceleration method It finds where the second derivative is the largest

Usage

```
fit_max_infl_lag(data)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass",and one optional column: "curve_id" This is data from may come from multiple growth curves
------	---

Value

growth curve data (as input) together with additional columns: lag, log.biomass, time.diff, time.av, second.deriv.b, biomass.increase

```
get_all_methods_lag  get_all_methods_lag
```

Description

Runs the main function that calculates lags based on growth curve data based on all possible methods.

Usage

```
get_all_methods_lag(data, biomass_incr_threshold, pars = NULL)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", and one optional column: "curve_id" This is data from may come from multiple growth curves
biomass_incr_threshold	A value of the biomass increase that we can surely associate with the end of the lag phase rather than random variation during the lag. Needs to be set specifically to avoid unconscious use of the value set by default. If set to NULL, the value from pars will be taken
pars	a list of parameters. defaults to the ones set by get_def_pars function. Otherwise create your own list with the following names: - model: if method = "parameter fitting to a model" , one of the following models needs to be chosen: "logistic", "baranyi" - n0_method: first.observation" if the first point is taken as the initial biomass or "minimal.observation" if the minimal biomass is taken is the initial point. In "healthy" growth curves these options should be equivalent but sometimes a drop in OD/biomass is observed at the beginning of a growth curve. In this case it is not obvious what to assume the initial biomass is. - tangent.method "local.regression" (if the tangent is fitted to a number of points around the maximal growth rate) or "to.point" (if the tangent is fitted only to the point where the growth rate is maximal); defaults to "to.point" - threshold: A value of the biomass increase that we can surely associate with the end of the lag phase rather than random variation during the lag. Defaults to 10 ² - curve_points: if tangent_method = "local.regression" then curve_points is the number of points the line is fitted to; defaults to 3 i.e. the point with the maximal uptake rate one point before and one point after - init_growth.rate: if logistic model is fitted. Defaults to NULL in which case the initial value will be based on the data - init_lag: if a logistic model is fitted, Defaults to NULL in which case the initial value will be based on the data - algorithm: if method = "parameter fitting to a model", nls algorithm to run the model fit; defaults to "auto" which will choose the best between bounded and unbounded "Levenberg-Marquardt" and bounded "port" - max_iter = if method = "parameter fitting to a model", the maximum number of nls iterations, defaults to 100

Value

growth curve data (time, biomass, curve_id) with the column: lag_calculation_method, and with the following additional columns: log_biomass, lag, line_slope, line_intercept, lag_calculation_method, predicted_data, diff, second_deriv_b, tangent_point, threshold Note that each growth curve will appear

get_def_pars	<i>get_def_pars Set defaults parameters used by calc_lag function</i>
--------------	---

Description

get_def_pars Set defaults parameters used by calc_lag function

Usage

```
get_def_pars()
```

Value

list of parameters

get_init_pars_baranyi	<i>get_init_pars_baranyi</i>
-----------------------	------------------------------

Description

Finds reasonable approximation for baranyi growth curve parameters (init_mumax, lag) based on the growth curve and some initial values These approximations will be used as the initial values for the proper optimization algorithm run later.

Usage

```
get_init_pars_baranyi(
  data_this_curve,
  this_n0,
  init_lag,
  init_gr_rate,
  min_b = 0.2,
  min_a = 0.8
)
```

Arguments

<code>data_this_curve</code>	data from one specific growth curve with these two columns: time and biomass
<code>this_n0</code>	the initial biomass
<code>init_lag</code>	initial value for the lag parameter
<code>init_gr_rate</code>	initial value for the growth rate
<code>min_b</code>	defaults to 0.2; <code>min_a</code> and <code>min_b</code> define where to look for exponential phase: it will be where the biomass is between $\min + (\max - \min) * (\min_a \text{ TO } \min_b)$
<code>min_a</code>	defaults to 0.8

Value

list of parameters: `init_mumax`, `init_lag`

```
get_init_pars_logistic
      get_init_pars_logistic
```

Description

Finds reasonable approximation for logistic growth curve parameters (K, lag, growth rate) based on the growth curve and some initial values. These approximations will be used as the initial values for the proper optimization algorithm run later.

Usage

```
get_init_pars_logistic(
  data_this_curve,
  this_n0,
  init_K,
  init_lag,
  init_gr_rate,
  min_b = 0.2,
  min_a = 0.8
)
```

Arguments

<code>data_this_curve</code>	data from one specific growth curve with these two columns: time and biomass
<code>this_n0</code>	the initial biomass
<code>init_K</code>	initial value for the saturation parameter K
<code>init_lag</code>	initial value for the lag parameter
<code>init_gr_rate</code>	initial value for the growth rate
<code>min_b</code>	defaults to 0.2; <code>min_a</code> and <code>min_b</code> define where to look for exponential phase: it will be where the biomass is between $\min + (\max - \min) * (\min_a \text{ TO } \min_b)$
<code>min_a</code>	defaults to 0.8

Value

list of parameters: init_K, init_lag, init_gr_rate,

get_lag	<i>get_lag</i>
---------	----------------

Description

The most basic function that calculates lags based on growth curve data, selected method and parameters. It uses calc_lag function and strips the results to only get lag parameter for each growth curve id.

Usage

```
get_lag(data, method, pars)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", and one optional column: "curve_id" This is data from may come from multiple growth curves
method	method of lag calculation, choose one of the following: "exponential", "biomass increase", "max growth acceleration", "parameter fitting to a model"
pars	a list of parameters. Get.default.parameters function can be used to get the default ones. Otherwise create your own list with the following names: - model: if method = "parameter fitting to a model", one of the following models needs to be chosen: "logistic", "baranyi" - n0_method: first.observation" if the first point is taken as the initial biomass or "minimal.observation" if the minimal biomass is taken as the initial point. In "healthy" growth curves these options should be equivalent but sometimes a drop in OD/biomass is observed at the beginning of a growth curve. In this case it is not obvious what to assume the initial biomass is. - tangent_method "local.regression" (if the tangent is fitted to a number of points around the maximal growth rate) or "to.point" (if the tangent is fitted only to the point where the growth rate is maximal); defaults to "to.point" - threshold: A value of the biomass increase that we can surely associate with the end of the lag phase rather than random variation during the lag. Defaults to 10 ² - curve_points: if tangent.method = "local.regression" then curve_points is the number of points the line is fitted to; defaults to 3 i.e. the point with the maximal uptake rate one point before and one point after - init_gr_rate: if logistic model is fitted. Defaults to NULL in which case the initial value will be based on the data - init_lag: if a logistic model is fitted, Defaults to NULL in which case the initial value will be based on the data - algorithm: if method = "parameter fitting to a model", nls algorithm to run the model fit; defaults to "auto" which will choose the best between bounded and unbounded "Levenberg-Marquardt" and bounded "port" - max_iter = if method = "parameter fitting to a model", the maximum number of nls iterations, defaults to 100

Value

lag per each curve_id

get_n0	<i>get_n0</i>
--------	---------------

Description

Gets the initial biomass to relate to

Usage

```
get_n0(biomass, n0_method)
```

Arguments

biomass	vector of biomass (chronologically ordered as in growth curve)
n0_method	"first.observation" if the first point is taken as the initial biomass or "minimal.observation" if the minimal biomass is taken as the initial point. In "healthy" growth curves these options should be equivalent but sometimes a drop in OD/biomass is observed at the beginning of a growth curve. In this case it is not obvious what to assume the initial biomass is.

Value

a value of the initial biomass (either the first observation or the minimum value depending on the parameter N0.method)

get_theme	<i>get_theme</i>
-----------	------------------

Description

This function sets a ggplot theme without grid. The theme removes the major and minor grid lines, sets a white background with a gray border and adjusts the text size.

Usage

```
get_theme(text_size = 12)
```

Arguments

text_size	defaults to 12
-----------	----------------

Value

a ggplot theme

lag_biomass_incr *lag_biomass_incr*

Description

Fits the lag to multiple growth curves based on the biomass increase method

Usage

```
lag_biomass_incr(data, threshold, n0)
```

Arguments

data	a data frame with two required columns names: "time" and "biomass", and one optional column: "curve_id" This is data from may come from multiple growth curves
threshold	A value of the biomass increase that we can surely associate with the end of the lag phase rather than random variation during the lag
n0	the initial biomass (lag will be defined as the time point where the difference between biomass and N0 reaches a predefined threshold)

Value

growth curve data (as input) together with additional columns: N0, increase.from.N0, lag

make_grwoth_curve_df *make_grwoth_curve_df*

Description

Create a growth curve data frame that can be later passed to the lag calculation functions

Usage

```
make_grwoth_curve_df(time, biomass, curve_id = NULL)
```

Arguments

time	numeric vector of times when biomass was measured (chronologically ordered as in growth curve)
biomass	numeric vector of measured biomass values (chronologically ordered as in growth curve)
curve_id	character vector of growth curve identifiers (i.e. if there are multiple measurements done at the same time point, they should have different curve_id)

Value

a data frame representing growth curve data

plot_data	<i>plot_data</i>
-----------	------------------

Description

Plots the provided growth curve (one single growth curve) on logarithmic scale

Usage

```
plot_data(data_new, log10_transform = TRUE)
```

Arguments

data_new	a data frame with two required columns names: "time" and "biomass"
log10_transform	if to plot y axis (biomass) on log10 scale

Value

ggplot object with a growth curve

plot_lag_fit	<i>plot_lag_fit</i>
--------------	---------------------

Description

Plots the provided growth curve (one single growth curve) together with the calculated lag and and the rationale for lag calculation

Usage

```
plot_lag_fit(data_new, print_lag_info = TRUE, log10_transform = TRUE)
```

Arguments

data_new	a data frame output by Calculate.Lag function: it needs to have the following columns: "time", "biomass", "tangent.point", "predicted.data", "threshold", "N0", "second.deriv.b", "line.intercept", "line.slope"
print_lag_info	if set to "TRUE" prints the lag length on the graph
log10_transform	if to plot y axis (biomass) on log10 scale

Value

ggplot object with a growth curve

smooth_data	<i>smooth_data Smoothens growth curves data</i>
-------------	---

Description

smooth_data Smoothens growth curves data

Usage

```
smooth_data(data, smooth_kind = "3RS3R")
```

Arguments

data	a data frame with two required columns names: "time" and "biomass",and one optional column: "curve_id" This is data from may come from multiple growth curves
smooth_kind	kind used for the smooth functions, defaults to "3RS3R"

Value

smoothened data

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