# Package 'drda'

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Type Package Title Dose-Response Data Analysis Version 2.0.5 Description Fit logistic functions to observed dose-response continuous data and evaluate goodness-of-fit measures. See Malyutina A., Tang J., and Pessia A. (2023) <doi:10.18637/jss.v106.i04>. License MIT + file LICENSE URL https://github.com/albertopessia/drda BugReports https://github.com/albertopessia/drda/issues **Depends** R (>= 3.6.0) Imports graphics, grDevices, stats **Suggests** knitr, rmarkdown, spelling, testthat (>= 3.1.0) VignetteBuilder knitr Config/testthat/edition 3 **Encoding** UTF-8 Language en-US LazyData true RoxygenNote 7.3.2 NeedsCompilation no Author Alberto Pessia [aut, cre] (<https://orcid.org/0000-0001-8607-9191>), Alina Malyutina [ctb] (<https://orcid.org/0000-0001-8220-5859>) Maintainer Alberto Pessia <dev@albertopessia.com> **Repository** CRAN Date/Publication 2025-01-16 10:00:02 UTC

# Contents

drda
effective_dose
gompertz_fn
gompertz_gradient
gompertz_gradient_2
loggompertz_fn
loggompertz_gradient
loggompertz_gradient_2
logistic2_fn
logistic2_gradient
logistic2_gradient_2
logistic4_fn
logistic4_gradient
logistic4_gradient_2
logistic5_fn
logistic5_gradient
logistic5_gradient_2
logistic6_fn
logistic6_gradient
logistic6_gradient_2
loglogistic2_fn 2
loglogistic2_gradient
loglogistic2_gradient_2
loglogistic4_fn 2
loglogistic4_gradient
loglogistic4_gradient_2
loglogistic5_fn
loglogistic5_gradient
loglogistic5_gradient_2
loglogistic6_fn 2
loglogistic6_gradient
loglogistic6_gradient_2
naac
nauc
plot.drda
voropm2

drda

## Description

Use the Newton's with a trust-region method to fit non-linear growth curves to observed data.

# Usage

```
drda(
   formula,
   data,
   subset,
   weights,
   na.action,
   mean_function = "logistic4",
   lower_bound = NULL,
   upper_bound = NULL,
   start = NULL,
   max_iter = 1000
)
```

## Arguments

formula	an object of class formula (or one that can be coerced to that class): a symbolic description of the model to be fitted. Currently supports only formulas of the type $y \sim x$ .
data	an optional data frame, list or environment (or object coercible by as.data.frame to a data frame) containing the variables in the model. If not found in data, the variables are taken from environment(formula), typically the environment from which drda is called.
subset	an optional vector specifying a subset of observations to be used in the fitting process.
weights	an optional vector of weights to be used in the fitting process. If provided, weighted least squares is used with weights weights (that is, minimizing sum(weights * residuals^2)), otherwise ordinary least squares is used.
na.action	a function which indicates what should happen when the data contain NAs. The default is set by the na.action setting of options, and is na.fail if that is unset. The 'factory-fresh' default is na.omit. Another possible value is NULL, no action. Value na.exclude can be useful.
mean_function	the model to be fitted. See details for available models.
lower_bound	numeric vector with the minimum admissible values of the parameters. Use -Inf to specify an unbounded parameter.
upper_bound	numeric vector with the maximum admissible values of the parameters. Use Inf to specify an unbounded parameter.

start	starting values for the parameters.
<pre>max_iter</pre>	maximum number of iterations in the optimization algorithm.

## Details

#### Available models:

Generalized (5-parameter) logistic function:

The 5-parameter logistic function can be selected by choosing mean\_function = "logistic5" or mean\_function = "15". The function is defined here as

 $alpha + delta / (1 + nu * exp(-eta * (x - phi)))^(1 / nu)$ 

where eta > 0 and nu > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

Parameter alpha is the value of the function when  $x \rightarrow -Inf$ . Parameter delta is the (signed) height of the curve. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi is related to the mid-value of the function. Parameter nu affects near which asymptote maximum growth occurs.

The value of the function when  $x \rightarrow Inf$  is alpha + delta. In dose-response studies delta can be interpreted as the maximum theoretical achievable effect.

#### 4-parameter logistic function:

The 4-parameter logistic function is the default model of drda. It can be explicitly selected by choosing mean\_function = "logistic4" or mean\_function = "l4". The function is obtained by setting nu = 1 in the generalized logistic function, that is

alpha + delta / (1 + exp(-eta \* (x - phi)))

where eta > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

Parameter alpha is the value of the function when x -> -Inf. Parameter delta is the (signed) height of the curve. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi represents the x value at which the curve is equal to its mid-point, i.e. f(phi; alpha, delta, eta, phi) = alpha + The value of the function when x -> Inf is alpha + delta. In dose-response studies delta can be interpreted as the maximum theoretical achievable effect.

#### 2-parameter logistic function:

The 2-parameter logistic function can be selected by choosing mean\_function = "logistic2" or mean\_function = "l2". For a monotonically increasing curve set nu = 1, alpha = 0, and delta = 1:

1 / (1 + exp(-eta \* (x - phi)))

For a monotonically decreasing curve set nu = 1, alpha = 1, and delta = -1:

1 - 1 / (1 + exp(-eta \* (x - phi)))

where eta > 0. The lower bound of the curve is zero while the upper bound of the curve is one. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi represents the x value at which the curve is equal to its mid-point, i.e. f(phi; eta, phi) = 1 / 2.

#### *Gompertz function:*

The Gompertz function is the limit for  $nu \rightarrow 0$  of the 5-parameter logistic function. It can be selected by choosing mean\_function = "gompertz" or mean\_function = "gz". The function is defined in this package as

alpha + delta \* exp(-exp(-eta \* (x - phi)))
where eta > 0.

Parameter alpha is the value of the function when  $x \rightarrow -Inf$ . Parameter delta is the (signed) height of the curve. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi sets the displacement along the x-axis.

The value of the function when  $x \rightarrow Inf$  is alpha + delta. In dose-response studies delta can be interpreted as the maximum theoretical achievable effect.

The mid-point of the function, that is alpha + delta / 2, is achieved at x = phi - log(log(2)) / eta.

#### *Generalized (5-parameter) log-logistic function:*

The 5-parameter log-logistic function is selected by setting mean\_function = "loglogistic5" or mean\_function = "115". The function is defined here as

alpha + delta \* (x^eta / (x^eta + nu \* phi^eta))^(1 / nu)

where  $x \ge 0$ , eta > 0, phi > 0, and nu > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing). The function is defined only for positive values of the predictor variable x.

Parameter alpha is the value of the function at x = 0. Parameter delta is the (signed) height of the curve. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi is related to the mid-value of the function. Parameter nu affects near which asymptote maximum growth occurs.

The value of the function when  $x \rightarrow Inf$  is alpha + delta. In dose-response studies delta can be interpreted as the maximum theoretical achievable effect.

#### 4-parameter log-logistic function:

The 4-parameter log-logistic function is selected by setting mean\_function = "loglogistic4" or mean\_function = "ll4". The function is obtained by setting nu = 1 in the generalized log-logistic function, that is

alpha + delta \* x^eta / (x^eta + phi^eta)

where  $x \ge 0$  and  $eta \ge 0$ . When delta is positive (negative) the curve is monotonically increasing (decreasing). The function is defined only for positive values of the predictor variable x.

Parameter alpha is the value of the function at x = 0. Parameter delta is the (signed) height of the curve. Parameter et a represents the steepness (growth rate) of the curve. Parameter phi represents the x value at which the curve is equal to its mid-point, i.e. f(phi; alpha, delta, eta, phi) = alpha + delta. The value of the function when  $x \rightarrow Inf$  is alpha + delta. In dose-response studies delta can be interpreted as the maximum theoretical achievable effect.

2-parameter log-logistic function:

The 2-parameter log-logistic function is selected by setting mean\_function = "loglogistic2" or mean\_function = "ll2". For a monotonically increasing curve set nu = 1, alpha = 0, and delta = 1:

x^eta / (x^eta + phi^eta)

For a monotonically decreasing curve set nu = 1, alpha = 1, and delta = -1:

1 - x^eta / (x^eta + phi^eta)

where  $x \ge 0$ , eta > 0, and phi > 0. The lower bound of the curve is zero while the upper bound of the curve is one.

Parameter eta represents the steepness (growth rate) of the curve. Parameter phi represents the x value at which the curve is equal to its mid-point, i.e. f(phi; eta, phi) = 1 / 2.

#### log-Gompertz function:

The log-Gompertz function is the limit for  $nu \rightarrow 0$  of the 5-parameter log-logistic function. It can be selected by choosing mean\_function = "loggompertz" or mean\_function = "lgz". The function is defined in this package as alpha + delta \* exp(-(phi / x)^eta)

where x > 0, eta > 0, and phi > 0. Note that the limit for  $x \rightarrow 0$  is alpha. When delta is positive (negative) the curve is monotonically increasing (decreasing). The function is defined only for positive values of the predictor variable x.

Parameter alpha is the value of the function at x = 0. Parameter delta is the (signed) height of the curve. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi sets the displacement along the x-axis.

The value of the function when  $x \rightarrow Inf$  is alpha + delta. In dose-response studies delta can be interpreted as the maximum theoretical achievable effect.

Constrained optimization:

It is possible to search for the maximum likelihood estimates within pre-specified interval regions.

*Note*: Hypothesis testing is not available for constrained estimates because asymptotic approximations might not be valid.

#### Value

An object of class drda and model\_fit, where model is the chosen mean function. It is a list containing the following components:

converged boolean value assessing if the optimization algorithm converged or not.

iterations total number of iterations performed by the optimization algorithm

constrained boolean value set to TRUE if optimization was constrained.

estimated boolean vector indicating which parameters were estimated from the data.

coefficients maximum likelihood estimates of the model parameters.

rss minimum value (found) of the residual sum of squares.

df.residuals residual degrees of freedom.

fitted.values fitted mean values.

residuals residuals, that is response minus fitted values.

weights (only for weighted fits) the specified weights.

mean\_function model that was used for fitting.

**n** effective sample size.

sigma corrected maximum likelihood estimate of the standard deviation.

loglik maximum value (found) of the log-likelihood function.

**fisher.info** observed Fisher information matrix evaluated at the maximum likelihood estimator.

vcov approximate variance-covariance matrix of the model parameters.

call the matched call.

terms the terms object used.

model the model frame used.

na.action (where relevant) information returned by model.frame on the special handling of NAs.

#### effective\_dose

#### Examples

```
# by default `drda` uses a 4-parameter logistic function for model fitting
fit_14 <- drda(response ~ log_dose, data = voropm2)</pre>
# get a general overview of the results
summary(fit_14)
# compare the model against a flat horizontal line and the full model
anova(fit_14)
# 5-parameter logistic curve appears to be a better model
fit_15 <- drda(response ~ log_dose, data = voropm2, mean_function = "15")</pre>
plot(fit_14, fit_15)
# fit a 2-parameter logistic function
fit_12 <- drda(response ~ log_dose, data = voropm2, mean_function = "12")</pre>
# compare our models
anova(fit_12, fit_14)
# use log-logistic functions when utilizing doses (instead of log-doses)
# here we show the use of other arguments as well
fit_115 <- drda(</pre>
 response ~ dose, weights = weight, data = voropm2,
 mean_function = "loglogistic5", lower_bound = c(0.5, -1.5, 0, -Inf, 0.25),
 upper_bound = c(1.5, 0.5, 5, Inf, 3), start = c(1, -1, 3, 100, 1),
 max_iter = 10000
)
# note that the maximum likelihood estimate is outside the region of
# optimization: not only the variance-covariance matrix is now singular but
# asymptotic assumptions do not hold anymore.
```

effective\_dose Effective dose

#### Description

Estimate effective doses, that is the x values for which f(x) = y.

## Usage

```
effective_dose(object, y, type, level)
```

## Arguments

object	fit object as returned by drda.
У	numeric vector with response levels (default 0.5).
type	character string with either "relative" (default) or "absolute".
level	level of confidence intervals (default 0.95).

#### Details

Given a fitted model f(x; theta) we seek the values x at which the function is equal to the specified response values.

If responses are given on a relative scale (type = "relative"), then y is expected to range in the interval (0, 1).

If responses are given on an absolute scale (type = "absolute"), then y is free to vary on the whole real line. Note, however, that the solution does not exist when y is not in the image of the function.

## Value

Numeric matrix with the effective doses and the corresponding confidence intervals. Each row is associated with each value of y.

## Examples

```
drda_fit <- drda(response ~ log_dose, data = voropm2)
effective_dose(drda_fit)</pre>
```

```
# relative values are given on the (0, 1) range
effective_dose(drda_fit, y = c(0.2, 0.8))
```

```
# explicitly say when we are using actual response values effective_dose(drda_fit, y = c(0.2, 0.8), type = "absolute")
```

# use a different confidence level effective\_dose(drda\_fit, y = 0.6, level = 0.8)

gompertz\_fn Gompertz function

#### Description

Evaluate at a particular set of parameters the Gompertz function.

## Usage

gompertz\_fn(x, theta)

#### Arguments

Х	numeric vector at which the Gompertz function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta phi).

#### Details

The Gompertz function f(x; theta) is defined here as

g(x; theta) = exp(-exp(-eta \* (x - phi))) f(x; theta) = alpha + delta g(x; theta) where theta = c(alpha, delta, eta, phi), alpha is the value of the function when x -> -Inf, delta is the (signed) height of the curve, eta > 0 is the steepness of the curve or growth rate, and phi is related with the value of function at x = 0.

When delta < 0 the curve is monotonically decreasing while it is monotonically increasing for delta > 0.

## Value

Numeric vector of the same length of x with the values of the Gompertz function.

gompertz\_gradient Gompertz function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the Gompertz function.

#### Usage

```
gompertz_gradient(x, theta)
gompertz_hessian(x, theta)
gompertz_gradient_hessian(x, theta)
```

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

## Details

The Gompertz function f(x; theta) is defined here as  $g(x; theta) = \exp(-\exp(-eta * (x - phi))) f(x; theta) = alpha + delta <math>g(x; theta)$  where theta = c(alpha, delta, eta, phi) and eta > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

## Value

Gradient or Hessian evaluated at the specified point.

gompertz\_gradient\_2 Gompertz function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the Gompertz function.

#### Usage

```
gompertz_gradient_2(x, theta)
gompertz_hessian_2(x, theta)
gompertz_gradient_hessian_2(x, theta)
```

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

## Details

The Gompertz function f(x; theta) is defined here as  $g(x; theta) = \exp(-\exp(-eta * (x - phi))) f(x; theta) = alpha + delta <math>g(x; theta)$ 

where theta = c(alpha, delta, eta, phi) and eta > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

This set of functions use a different parameterization from link[drda]{gompertz\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta).

Note that argument theta is on the original scale and not on the log scale.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

loggompertz\_fn log-Gompertz function

#### Description

Evaluate at a particular set of parameters the log-Gompertz function.

## Usage

```
loggompertz_fn(x, theta)
```

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

## Details

```
The log-Gompertz function f(x; \text{ theta}) is defined here as

f(x; \text{ theta}) = \text{alpha} + \text{delta } \exp(-(\text{phi} / x)^{\text{eta}})

where x \ge 0, theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0. By convention we set

f(0; \text{ theta}) = \lim_{x \to 0} f(x; \text{ theta}) = \text{alpha}.
```

## Value

Numeric vector of the same length of x with the values of the log-logistic function.

loggompertz\_gradient Log-Gompertz function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the log-Gompertz function.

## Usage

```
loggompertz_gradient(x, theta)
```

```
loggompertz_hessian(x, theta)
```

loggompertz\_gradient\_hessian(x, theta)

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

## Details

The log-Gompertz function f(x; theta) is defined here as  $f(x; \text{theta}) = \text{alpha} + \text{delta} \exp(-(\text{phi} / x)^{\text{eta}})$ where  $x \ge 0$ , theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0. By convention we set  $f(0; \text{theta}) = \lim_{x \to 0} f(x; \text{theta}) = \text{alpha}.$ 

#### Value

Gradient or Hessian evaluated at the specified point.

loggompertz\_gradient\_2

```
Log-Gompertz function gradient and Hessian
```

#### Description

Evaluate at a particular set of parameters the gradient and Hessian of the log-Gompertz function.

### Usage

```
loggompertz_gradient_2(x, theta)
```

```
loggompertz_hessian_2(x, theta)
```

loggompertz\_gradient\_hessian\_2(x, theta)

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

#### Details

The log-Gompertz function f(x; theta) is defined here as  $f(x; \text{theta}) = \text{alpha} + \text{delta} \exp(-(\text{phi} / x)^{\text{eta}})$ where  $x \ge 0$ , theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0. By convention we set  $f(0; \text{theta}) = \lim_{x \to 0} f(x; \text{theta}) = \text{alpha}.$ 

## logistic2\_fn

This set of functions use a different parameterization from link[drda]{loggompertz\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta) and phi2 = log(phi).

Note that argument theta is on the original scale and not on the log scale.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

logistic2\_fn 2-parameter logistic function

## Description

Evaluate at a particular set of parameters the 2-parameter logistic function.

#### Usage

```
logistic2_fn(x, theta)
```

#### Arguments

Х	numeric vector at which the logistic function is to be evaluated.
theta	numeric vector with the four parameters in the form $c(alpha, delta, eta, phi)$ . alpha can only be equal to 0 or 1 while delta can only be equal to 1 or -1.

#### Details

The 2-parameter logistic function f(x; theta) is defined here as  $g(x; \text{ theta}) = 1 / (1 + \exp(-\text{eta} * (x - \text{phi}))) f(x; \text{ theta}) = alpha + delta g(x; \text{ theta})$ 

where theta = c(alpha, delta, eta, phi) and eta > 0. Only eta and phi are free to vary (therefore the name) while vector c(alpha, delta) is constrained to be either c(0, 1) (monotonically increasing curve) or c(1, -1) (monotonically decreasing curve).

This function allows values other than  $\{0, 1, -1\}$  for alpha and delta but will coerce them to their proper constraints.

## Value

Numeric vector of the same length of x with the values of the logistic function.

logistic2\_gradient 2-parameter logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 2-parameter logistic function.

#### Usage

```
logistic2_gradient(x, theta, delta)
logistic2_hessian(x, theta, delta)
logistic2_gradient_hessian(x, theta, delta)
```

#### Arguments

Х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the two parameters in the form c(eta, phi).
delta	value of delta parameter (either 1 or -1).

## Details

The 2-parameter logistic function f(x; theta) is defined here as g(x; theta) = 1 / (1 + exp(-eta \* (x - phi))) f(x; theta) = alpha + delta <math>g(x; theta) where theta = c(alpha, delta, eta, phi) and eta > 0. Only eta and phi are free to vary (therefore the name) while vector c(alpha, delta) is constrained to be either c(0, 1) (monotonically

## Value

Gradient or Hessian evaluated at the specified point.

increasing curve) or c(1, -1) (monotonically decreasing curve).

logistic2\_gradient\_2 2-parameter logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 2-parameter logistic function.

## logistic4\_fn

## Usage

```
logistic2_gradient_2(x, theta, delta)
logistic2_hessian_2(x, theta, delta)
logistic2_gradient_hessian_2(x, theta, delta)
```

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the two parameters in the form c(eta, phi).
delta	value of delta parameter (either 1 or -1).

## Details

The 2-parameter logistic function f(x; theta) is defined here as g(x; theta) = 1 / (1 + exp(-eta \* (x - phi))) f(x; theta) = alpha + delta <math>g(x; theta) where theta = c(alpha, delta, eta, phi) and eta > 0. Only eta and phi are free to vary (there-

fore the name) while vector c(alpha, delta) is constrained to be either c(0, 1) (monotonically increasing curve) or c(1, -1) (monotonically decreasing curve).

This set of functions use a different parameterization from link[drda]{logistic2\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta).

Note that argument theta is on the original scale and not on the log scale.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

logistic4\_fn 4-parameter logistic function

## Description

Evaluate at a particular set of parameters the 4-parameter logistic function.

#### Usage

logistic4\_fn(x, theta)

#### Arguments

Х	numeric vector at which the logistic function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

#### Details

The 4-parameter logistic function f(x; theta) is defined here as

g(x; theta) = 1 / (1 + exp(-eta \* (x - phi))) f(x; theta) = alpha + delta g(x; theta) where theta = c(alpha, delta, eta, phi), alpha is the value of the function when x -> -Inf, delta is the (signed) height of the curve, eta > 0 is the steepness of the curve or growth rate (also known as the Hill coefficient), and phi is the value of x at which the curve is equal to its mid-point. When delta < 0 the curve is monotonically decreasing while it is monotonically increasing for delta > 0.

The mid-point f(phi; theta) is equal to alpha + delta / 2 while the value of the function for x -> Inf is alpha + delta.

## Value

Numeric vector of the same length of x with the values of the logistic function.

logistic4\_gradient 4-parameter logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 4-parameter logistic function.

#### Usage

logistic4\_gradient(x, theta)

```
logistic4_hessian(x, theta)
```

```
logistic4_gradient_hessian(x, theta)
```

#### Arguments

Х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta,
	phi).

## Details

The 4-parameter logistic function f(x; theta) is defined here as g(x; theta) = 1 / (1 + exp(-eta \* (x - phi))) f(x; theta) = alpha + delta <math>g(x; theta) where theta = c(alpha, delta, eta, phi) and eta > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

## Value

Gradient or Hessian evaluated at the specified point.

16

#### Description

Evaluate at a particular set of parameters the gradient and Hessian of the 4-parameter logistic function.

#### Usage

```
logistic4_gradient_2(x, theta)
```

logistic4\_hessian\_2(x, theta)

logistic4\_gradient\_hessian\_2(x, theta)

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

#### Details

The 4-parameter logistic function f(x; theta) is defined here as  $g(x; \text{ theta}) = 1 / (1 + \exp(-\text{eta} * (x - \text{phi}))) f(x; \text{ theta}) = \text{alpha} + \text{delta } g(x; \text{ theta})$ 

where theta = c(alpha, delta, eta, phi) and eta > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

This set of functions use a different parameterization from link[drda]{logistic4\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta).

Note that argument theta is on the original scale and not on the log scale.

#### Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

logistic5\_fn

#### Description

Evaluate at a particular set of parameters the 5-parameter logistic function.

## Usage

logistic5\_fn(x, theta)

#### Arguments

х	numeric vector at which the logistic function is to be evaluated.
theta	numeric vector with the five parameters in the form c(alpha, delta, eta, phi, nu).

## Details

The 5-parameter logistic function f(x; theta) is defined here as  $g(x; theta) = 1 / (1 + nu * exp(-eta * (x - phi)))^(1 / nu) f(x; theta) = alpha + delta <math>g(x; theta)$  where theta = c(alpha, delta, eta, phi, nu), eta > 0, and nu > 0.

When delta is positive (negative) the curve is monotonically increasing (decreasing). When  $x \rightarrow$ -Inf the value of the function is alpha while the value of the function for  $x \rightarrow$ Inf is alpha + delta.

Parameter alpha is the value of the function when  $x \rightarrow -Inf$ . Parameter delta is the (signed) height of the curve. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi is related to the mid-value of the function. Parameter nu affects near which asymptote maximum growth occurs.

## Value

Numeric vector of the same length of x with the values of the logistic function.

logistic5\_gradient 5-parameter logistic function gradient and Hessian

#### Description

Evaluate at a particular set of parameters the gradient and Hessian of the 5-parameter logistic function.

## logistic5\_gradient\_2

## Usage

```
logistic5_gradient(x, theta)
logistic5_hessian(x, theta)
logistic5_gradient_hessian(x, theta)
```

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the five parameters in the form c(alpha, delta, eta, phi, nu).

## Details

The 5-parameter logistic function f(x; theta) is defined here as  $g(x; theta) = 1 / (1 + nu * exp(-eta * (x - phi)))^(1 / nu) f(x; theta) = alpha + delta g(x; theta)$  where theta = c(alpha, delta, eta, phi, nu), eta > 0, and nu > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

## Value

Gradient or Hessian evaluated at the specified point.

logistic5\_gradient\_2 5-parameter logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 5-parameter logistic function.

## Usage

```
logistic5_gradient_2(x, theta)
```

```
logistic5_hessian_2(x, theta)
```

```
logistic5_gradient_hessian_2(x, theta)
```

## Arguments

x	numeric vector at which the function is to be evaluated.
theta	numeric vector with the five parameters in the form c(alpha, delta, eta, phi, nu).

## Details

The 5-parameter logistic function f(x; theta) is defined here as  $g(x; theta) = 1 / (1 + nu * exp(-eta * (x - phi)))^(1 / nu) f(x; theta) = alpha + delta <math>g(x; theta)$  where theta = c(alpha, delta, eta, phi, nu), eta > 0, and nu > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

This set of functions use a different parameterization from link[drda]{logistic5\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta) and nu2 = log(nu).

Note that argument theta is on the original scale and not on the log scale.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

logistic6_fn 6-parameter logistic function
--

#### Description

Evaluate at a particular set of parameters the 6-parameter logistic function.

#### Usage

logistic6\_fn(x, theta)

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the six parameters in the form c(alpha, delta, eta, phi,
	nu, xi).

## Details

The 6-parameter logistic function f(x; theta) is defined here as  $g(x; theta) = 1 / (xi + nu * exp(-eta * (x - phi)))^(1 / nu) f(x; theta) = alpha + delta g(x; theta)$  where theta = c(alpha, delta, eta, phi, nu, xi), eta > 0, nu > 0, and xi > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

Parameter alpha is the value of the function when  $x \rightarrow -Inf$ . Parameter delta affects the value of the function when  $x \rightarrow Inf$ . Parameter eta represents the steepness (growth rate) of the curve. Parameter phi is related to the mid-value of the function. Parameter nu affects near which asymptote maximum growth occurs. Parameter xi affects the value of the function when  $x \rightarrow Inf$ .

**Note**: The 6-parameter logistic function is over-parameterized and non-identifiable from data. It is available only for theoretical research.

## Value

Numeric vector of the same length of x with the values of the logistic function.

20

logistic6\_gradient 6-parameter logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 6-parameter logistic function.

## Usage

```
logistic6_gradient(x, theta)
logistic6_hessian(x, theta)
logistic6_gradient_hessian(x, theta)
```

#### Arguments

Х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the six parameters in the form c(alpha, delta, eta, phi, nu, xi).

## Details

The 6-parameter logistic function f(x; theta) is defined here as  $g(x; \text{theta}) = 1 / (xi + nu * exp(-eta * (x - phi)))^(1 / nu) f(x; \text{theta}) = alpha + delta g(x; \text{theta})$  where theta = c(alpha, delta, eta, phi, nu, xi), eta > 0, nu > 0, and xi > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

**Note**: The 6-parameter logistic function is over-parameterized and non-identifiable from data. It is available only for theoretical research.

## Value

Gradient or Hessian evaluated at the specified point.

logistic6\_gradient\_2 6-parameter logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 6-parameter logistic function.

## Usage

```
logistic6_gradient_2(x, theta)
```

logistic6\_hessian\_2(x, theta)

```
logistic6_gradient_hessian_2(x, theta)
```

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the six parameters in the form c(alpha, delta, eta, phi,
	nu, xi).

## Details

The 6-parameter logistic function f(x; theta) is defined here as

 $g(x; theta) = 1 / (xi + nu * exp(-eta * (x - phi)))^(1 / nu) f(x; theta) = alpha + delta g(x; theta) where theta = c(alpha, delta, eta, phi, nu, xi), eta > 0, nu > 0, and xi > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).$ 

This set of functions use a different parameterization from link[drda]{logistic6\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta), nu2 = log(nu), and xi2 = log(xi).

Note that argument theta is on the original scale and not on the log scale.

**Note**: The 6-parameter logistic function is over-parameterized and non-identifiable from data. It is available only for theoretical research.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

loglogistic2\_fn 2-parameter log-logistic function

#### Description

Evaluate at a particular set of parameters the 2-parameter log-logistic function.

#### Usage

loglogistic2\_fn(x, theta)

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form $c(alpha, delta, eta, phi)$ . alpha can only be equal to 0 or 1 while delta can only be equal to 1 or -1.

22

#### Details

The 2-parameter log-logistic function f(x; theta) is defined here as

 $g(x; theta) = x^{eta} / (x^{eta} + phi^{eta}) f(x; theta) = alpha + delta g(x; theta) where x >= 0, theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0. Only eta and phi are free to vary (therefore the name) while vector c(alpha, delta) is constrained to be either c(0, 1) (monotonically increasing curve) or c(1, -1) (monotonically decreasing curve).$ 

This function allows values other than  $\{0, 1, -1\}$  for alpha and delta but will coerce them to their proper constraints.

#### Value

Numeric vector of the same length of x with the values of the log-logistic function.

loglogistic2\_gradient 2-parameter log-logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 2-parameter log-logistic function.

## Usage

```
loglogistic2_gradient(x, theta, delta)
```

loglogistic2\_hessian(x, theta, delta)

```
loglogistic2_gradient_hessian(x, theta, delta)
```

#### Arguments

Х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the two parameters in the form c(eta, phi).
delta	value of delta parameter (either 1 or -1).

## Details

The 2-parameter log-logistic function f(x; theta) is defined here as  $g(x; \text{theta}) = x^{\text{eta}} / (x^{\text{eta}} + \text{phi}^{\text{eta}}) f(x; \text{theta}) = \text{alpha} + \text{delta } g(x; \text{theta})$ 

```
where x \ge 0, theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0. Only eta and phi are free to vary (therefore the name), while c(alpha, delta) are constrained to be either c(0, 1) (monotonically increasing curve) or c(1, -1) (monotonically decreasing curve).
```

#### Value

Gradient or Hessian evaluated at the specified point.

```
loglogistic2_gradient_2
```

2-parameter log-logistic function gradient and Hessian

### Description

Evaluate at a particular set of parameters the gradient and Hessian of the 2-parameter log-logistic function.

## Usage

```
loglogistic2_gradient_2(x, theta, delta)
```

loglogistic2\_hessian\_2(x, theta, delta)

loglogistic2\_gradient\_hessian\_2(x, theta, delta)

#### Arguments

x	numeric vector at which the function is to be evaluated.
theta	numeric vector with the two parameters in the form c(eta, phi).
delta	value of delta parameter (either 1 or -1).

#### Details

The 2-parameter log-logistic function f(x; theta) is defined here as  $g(x; \text{theta}) = x^{\text{eta}} / (x^{\text{eta}} + \text{phi}^{\text{eta}}) f(x; \text{theta}) = \text{alpha} + \text{delta } g(x; \text{theta})$ 

where  $x \ge 0$ , theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0. Only eta and phi are free to vary (therefore the name), while c(alpha, delta) are constrained to be either c(0, 1) (monotonically increasing curve) or c(1, -1) (monotonically decreasing curve).

This set of functions use a different parameterization from link[drda]{loglogistic2\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta) and phi2 = log(phi).

Note that argument theta is on the original scale and not on the log scale.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

loglogistic4\_fn *4-parameter log-logistic function* 

#### Description

Evaluate at a particular set of parameters the 4-parameter log-logistic function.

## Usage

```
loglogistic4_fn(x, theta)
```

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

## Details

```
The 4-parameter log-logistic function f(x; \text{theta}) is defined here as g(x; \text{theta}) = x^{\text{eta}} / (x^{\text{eta}} + \text{phi}^{\text{eta}}) f(x; \text{theta}) = \text{alpha} + \text{delta } g(x; \text{theta}) where x \ge 0, theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0.
```

## Value

Numeric vector of the same length of x with the values of the log-logistic function.

loglogistic4\_gradient 4-parameter log-logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 4-parameter log-logistic function.

## Usage

```
loglogistic4_gradient(x, theta)
```

```
loglogistic4_hessian(x, theta)
```

loglogistic4\_gradient\_hessian(x, theta)

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

## Details

```
The 4-parameter log-logistic function f(x; \text{theta}) is defined here as g(x; \text{theta}) = x^{\text{table}} / (x^{\text{table}} + \text{phi}^{\text{table}}) f(x; \text{theta}) = alpha + delta <math>g(x; \text{theta}) where x \ge 0, theta = c(alpha, delta, eta, phi), eta > 0, and phi > 0.
```

#### Value

Gradient or Hessian evaluated at the specified point.

loglogistic4\_gradient\_2

4-parameter log-logistic function gradient and Hessian

#### Description

Evaluate at a particular set of parameters the gradient and Hessian of the 4-parameter log-logistic function.

#### Usage

```
loglogistic4_gradient_2(x, theta)
```

```
loglogistic4_hessian_2(x, theta)
```

loglogistic4\_gradient\_hessian\_2(x, theta)

#### Arguments

Х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the four parameters in the form c(alpha, delta, eta, phi).

## Details

The 4-parameter log-logistic function f(x; theta) is defined here as  $g(x; \text{theta}) = x^{\text{eta}} / (x^{\text{eta}} + \text{phi}^{\text{eta}}) f(x; \text{theta}) = \text{alpha} + \text{delta } g(x; \text{theta})$  where  $x \ge 0$ , theta = c(alpha, delta, eta, phi, nu), eta > 0, and phi > 0.

This set of functions use a different parameterization from link[drda]{loglogistic4\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta) and phi2 = log(phi).

Note that argument theta is on the original scale and not on the log scale.

loglogistic5\_fn

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

loglogistic5\_fn 5-parameter log-logistic function

## Description

Evaluate at a particular set of parameters the 5-parameter log-logistic function.

## Usage

```
loglogistic5_fn(x, theta)
```

## Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the five parameters in the form c(alpha, delta, eta, phi, nu).

## Details

The 5-parameter log-logistic function f(x; theta) is defined here as g(x; theta) = (x^eta / (x^eta + nu \* phi^eta))^(1 / nu) f(x; theta) = alpha + delta g(x; theta)

where x >= 0, theta = c(alpha, delta, eta, phi, nu), eta > 0, phi > 0, and nu > 0.

Parameter alpha is the value of the function when x = 0. Parameter delta is the (signed) height of the curve. Parameter eta represents the steepness (growth rate) of the curve. Parameter phi is related to the mid-value of the function. Parameter nu affects near which asymptote maximum growth occurs.

#### Value

Numeric vector of the same length of x with the values of the log-logistic function.

loglogistic5\_gradient 5-parameter log-logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 5-parameter log-logistic function.

## Usage

```
loglogistic5_gradient(x, theta)
loglogistic5_hessian(x, theta)
```

loglogistic5\_gradient\_hessian(x, theta)

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the five parameters in the form c(alpha, delta, eta, phi, nu).

## Details

The 5-parameter log-logistic function f(x; theta) is defined here as  $g(x; \text{theta}) = (x^{eta} / (x^{eta} + nu * phi^{eta}))^{(1 / nu)} f(x; \text{theta}) = alpha + delta g(x; \text{theta})$  where  $x \ge 0$ , theta = c(alpha, delta, eta, phi, nu), eta > 0, phi > 0, and nu > 0.

## Value

Gradient or Hessian evaluated at the specified point.

loglogistic5\_gradient\_2

5-parameter log-logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 5-parameter log-logistic function.

## loglogistic6\_fn

## Usage

```
loglogistic5_gradient_2(x, theta)
loglogistic5_hessian_2(x, theta)
loglogistic5_gradient_hessian_2(x, theta)
```

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the five parameters in the form c(alpha, delta, eta, phi, nu).

## Details

The 5-parameter log-logistic function f(x; theta) is defined here as

 $g(x; theta) = (x^eta / (x^eta + nu * phi^eta))^(1 / nu) f(x; theta) = alpha + delta g(x; theta)$ 

where  $x \ge 0$ , theta = c(alpha, delta, eta, phi, nu), eta > 0, phi > 0, and nu > 0.

This set of functions use a different parameterization from link[drda]{loglogistic5\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta), phi2 = log(phi), and nu2 = log(nu).

Note that argument theta is on the original scale and not on the log scale.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

loglogistic6\_fn 6-parameter log-logistic function

#### Description

Evaluate at a particular set of parameters the 6-parameter log-logistic function.

#### Usage

```
loglogistic6_fn(x, theta)
```

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the six parameters in the form c(alpha, delta, eta, phi,
	nu, xi).

The 6-parameter log-logistic function f(x; theta) is defined here as

 $g(x; theta) = (x^eta / (xi * x^eta + nu * phi^eta))^(1 / nu) f(x; theta) = alpha + delta g(x; theta) where x >= 0, theta = c(alpha, delta, eta, phi, nu, xi), eta > 0, phi > 0, nu > 0, and xi > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).$ 

Parameter alpha is the value of the function when x = 0. Parameter delta affects the value of the function when  $x \rightarrow Inf$ . Parameter eta represents the steepness (growth rate) of the curve. Parameter phi is related to the mid-value of the function. Parameter nu affects near which asymptote maximum growth occurs. Parameter xi affects the value of the function when  $x \rightarrow Inf$ .

**Note**: The 6-parameter log-logistic function is over-parameterized and non-identifiable from data. It is available only for theoretical research.

## Value

Numeric vector of the same length of x with the values of the log-logistic function.

loglogistic6\_gradient 6-parameter log-logistic function gradient and Hessian

#### Description

Evaluate at a particular set of parameters the gradient and Hessian of the 6-parameter log-logistic function.

#### Usage

```
loglogistic6_gradient(x, theta)
```

```
loglogistic6_hessian(x, theta)
```

loglogistic6\_gradient\_hessian(x, theta)

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the six parameters in the form c(alpha, delta, eta, phi, nu, xi).

#### Details

The 6-parameter log-logistic function f(x; theta) is defined here as g(x; theta) = (x^eta / (xi \* x^eta + nu \* phi^eta))^(1 / nu) f(x; theta) = alpha + delta g(x; theta) where x >= 0, theta = c(alpha, delta, eta, phi, nu, xi), eta > 0, phi > 0, nu > 0, and xi > 0. When delta is positive (negative) the curve is monotonically increasing (decreasing).

**Note**: The 6-parameter log-logistic function is over-parameterized and non-identifiable from data. It is available only for theoretical research.

#### 30

#### Value

Gradient or Hessian evaluated at the specified point.

loglogistic6\_gradient\_2

6-parameter log-logistic function gradient and Hessian

## Description

Evaluate at a particular set of parameters the gradient and Hessian of the 6-parameter log-logistic function.

## Usage

```
loglogistic6_gradient_2(x, theta)
```

```
loglogistic6_hessian_2(x, theta)
```

```
loglogistic6_gradient_hessian_2(x, theta)
```

#### Arguments

х	numeric vector at which the function is to be evaluated.
theta	numeric vector with the six parameters in the form $c(alpha, delta, eta, phi, nu, xi)$ .

#### Details

The 6-parameter log-logistic function f(x; theta) is defined here as  $g(x; \text{ theta}) = (x^\text{eta} / (xi * x^\text{eta} + nu * phi^\text{eta}))^(1 / nu) f(x; \text{ theta}) = alpha + delta g(x; \text{ theta})$  where  $x \ge 0$ , theta = c(alpha, delta, eta, phi, nu, xi), eta > 0, phi > 0, nu > 0, and xi > 0.

This set of functions use a different parameterization from link[drda]{loglogistic6\_gradient}. To avoid the non-negative constraints of parameters, the gradient and Hessian computed here are for the function with eta2 = log(eta), phi2 = log(phi), nu2 = log(nu), and xi2 = log(xi).

Note that argument theta is on the original scale and not on the log scale.

**Note**: The 6-parameter log-logistic function is over-parameterized and non-identifiable from data. It is available only for theoretical research.

## Value

Gradient or Hessian of the alternative parameterization evaluated at the specified point.

Area above the curve

#### Description

Evaluate the normalized area above the curve (NAAC).

## Usage

naac(object, xlim, ylim)

#### Arguments

object	fit object as returned by drda.
xlim	numeric vector of length 2 with the lower and upped bound of the integration interval. Default is $c(-10, 10)$ for the logistic function or $c(0, 1000)$ for the log-logistic function.
ylim	numeric vector of length 2 with the lower and upped bound of the allowed function values. Default is $c(0, 1)$ .

#### Details

The area under the curve (AUC) is the integral of the chosen model y(x; theta) with respect to x.

In real applications the response variable is usually contained within a known interval. For example, if our response represents relative viability against a control compound, the curve is expected to be between 0 and 1. Let ylim = c(yl, yu) represent the admissible range of our function y(x; theta), that is yl is its lower bound and yu its upper bound. Let xlim = c(xl, xu) represent the admissible range of the predictor variable x. For example, when x represent the dose, the boundaries are the minimum and maximum doses we can administer.

To make the AUC value comparable between different compounds and/or studies, this function sets a hard constraint on both the x variable and the function y. The intervals can always be changed if needed.

The integral calculated by this function is of the piece-wise function f(x; theta) defined as

f(x; theta) = yl, if y(x; theta) < yl
f(x; theta) = y(x; theta), if yl <= y(x; theta) <= yu
f(x; theta) = yu, if y(x; theta) > yu

The AUC is finally normalized by its maximum possible value, that is the area of the rectangle with width xu - xl and height yu - yl.

The normalized area above the curve (NAAC) is simply NAAC = 1 - NAUC.

#### Value

Numeric value representing the normalized area above the curve.

naac

#### nauc

#### See Also

nauc for the Normalized Area Under the Curve (NAUC).

#### Examples

```
drda_fit <- drda(response ~ log_dose, data = voropm2)
naac(drda_fit)
naac(drda_fit, xlim = c(6, 8), ylim = c(0.2, 0.5))</pre>
```

nauc

Area under the curve

#### Description

Evaluate the normalized area under the curve (NAUC).

#### Usage

nauc(object, xlim, ylim)

## Arguments

object	fit object as returned by drda.
xlim	numeric vector of length 2 with the lower and upped bound of the integration interval. Default is $c(-10, 10)$ for the logistic function or $c(0, 1000)$ for the log-logistic function.
ylim	numeric vector of length 2 with the lower and upped bound of the allowed function values. Default is $c(0, 1)$ .

## Details

The area under the curve (AUC) is the integral of the chosen model y(x; theta) with respect to x.

In real applications the response variable is usually contained within a known interval. For example, if our response represents relative viability against a control compound, the curve is expected to be between 0 and 1. Let ylim = c(yl, yu) represent the admissible range of our function y(x; theta), that is yl is its lower bound and yu its upper bound. Let xlim = c(xl, xu) represent the admissible range of the predictor variable x. For example, when x represent the dose, the boundaries are the minimum and maximum doses we can administer.

To make the AUC value comparable between different compounds and/or studies, this function sets a hard constraint on both the x variable and the function y. The intervals can always be changed if needed.

The integral calculated by this function is of the piece-wise function f(x; theta) defined as f(x; theta) = yl, if y(x; theta) < yl

f(x; theta) = y(x; theta), if yl <= y(x; theta) <= yu

f(x; theta) = yu, if y(x; theta) > yu

The AUC is finally normalized by its maximum possible value, that is the area of the rectangle with width xu - xl and height yu - yl.

## Value

Numeric value representing the normalized area under the curve.

#### See Also

naac for the Normalized Area Above the Curve (NAAC).

## Examples

```
drda_fit <- drda(response ~ log_dose, data = voropm2)
nauc(drda_fit)
nauc(drda_fit, xlim = c(6, 8), ylim = c(0.2, 0.5))</pre>
```

Model fit plotting

plot.drda

# Description

Plot maximum likelihood curves fitted with drda.

#### Usage

## S3 method for class 'drda'
plot(x, ...)

## Arguments

х	drda object as returned by the link[drda]{drda} function.
	other drda objects or parameters to be passed to the plotting functions. See 'Details'.

## Details

This function provides a scatter plot of the observed data, overlaid with the maximum likelihood curve fit. If multiple fit objects from the same family of models are given, they will all be placed in the same plot.

Accepted plotting arguments are:

**base** character string with the base used for printing the values on the x axis. Accepted values are 10 for base 10, 2 for base 2, e for base e, or n (default) for no log-scale printing.

col curve color(s). By default, up to 9 color-blind friendly colors are provided.

xlab, ylab axis labels.

xlim, ylim the range of x and y values with sensible defaults.

**level** level of confidence intervals (default is 0.95). Set to zero or a negative value to disable confidence intervals.

midpoint if TRUE (default) shows guidelines associated with the curve mid-point.

## voropm2

plot\_data if TRUE (default) shows in the plot the data points used for fitting.

legend\_show if TRUE (default) shows the legend.

**legend\_location** character string with custom legend position. See link[graphics]{legend} for possible keywords.

legend custom labels for the legend model names.

**show** If TRUE (default) a figure is plotted, otherwise the function returns a list with values to create the figure manually.

## Value

If argument show is TRUE, no return value. If argument show is FALSE, a list with all plotting data.

voropm2

Vorinostat in OPM-2 cell-line dataset

#### Description

A dataset containing dose-response data of drug Vorinostat tested ex-vivo on the OPM-2 cell-line.

#### Usage

voropm2

#### Format

A data frame with 45 rows and 4 variables:

response viability measures normalized using positive and negative controls

dose drug concentrations (nM) used for testing

log\_dose natural logarithm of variable dose

weight random weights included only for package demonstration

# Index

\* datasets voropm2, 35 as.data.frame, 3 drda, 3, 7, 32, 33 effective\_dose, 7 formula, 3 gompertz\_fn, 8 gompertz\_gradient, 9 gompertz\_gradient\_2, 10 gompertz\_gradient\_hessian (gompertz\_gradient), 9 gompertz\_gradient\_hessian\_2 (gompertz\_gradient\_2), 10 gompertz\_hessian (gompertz\_gradient), 9 gompertz\_hessian\_2 (gompertz\_gradient\_2), 10 loggompertz\_fn, 11 loggompertz\_gradient, 11 loggompertz\_gradient\_2, 12 loggompertz\_gradient\_hessian (loggompertz\_gradient), 11 loggompertz\_gradient\_hessian\_2 (loggompertz\_gradient\_2), 12 loggompertz\_hessian (loggompertz\_gradient), 11 loggompertz\_hessian\_2 (loggompertz\_gradient\_2), 12 logistic2\_fn, 13 logistic2\_gradient, 14 logistic2\_gradient\_2, 14 logistic2\_gradient\_hessian (logistic2\_gradient), 14 logistic2\_gradient\_hessian\_2 (logistic2\_gradient\_2), 14

logistic2\_hessian (logistic2\_gradient), 14 logistic2\_hessian\_2 (logistic2\_gradient\_2), 14 logistic4\_fn, 15 logistic4\_gradient, 16 logistic4\_gradient\_2, 17 logistic4\_gradient\_hessian (logistic4\_gradient), 16 logistic4\_gradient\_hessian\_2 (logistic4\_gradient\_2), 17 logistic4\_hessian (logistic4\_gradient), 16 logistic4\_hessian\_2 (logistic4\_gradient\_2), 17 logistic5\_fn, 18 logistic5\_gradient, 18 logistic5\_gradient\_2, 19 logistic5\_gradient\_hessian (logistic5\_gradient), 18 logistic5\_gradient\_hessian\_2 (logistic5\_gradient\_2), 19 logistic5\_hessian (logistic5\_gradient), 18 logistic5\_hessian\_2 (logistic5\_gradient\_2), 19 logistic6\_fn, 20 logistic6\_gradient, 21 logistic6\_gradient\_2, 21 logistic6\_gradient\_hessian (logistic6\_gradient), 21 logistic6\_gradient\_hessian\_2 (logistic6\_gradient\_2), 21 logistic6\_hessian (logistic6\_gradient), 21 logistic6\_hessian\_2 (logistic6\_gradient\_2), 21 loglogistic2\_fn, 22 loglogistic2\_gradient, 23

## INDEX

loglogistic2\_gradient\_2, 24 loglogistic2\_gradient\_hessian (loglogistic2\_gradient), 23 loglogistic2\_gradient\_hessian\_2 (loglogistic2\_gradient\_2), 24 loglogistic2\_hessian (loglogistic2\_gradient), 23 loglogistic2\_hessian\_2 (loglogistic2\_gradient\_2), 24 loglogistic4\_fn, 25 loglogistic4\_gradient, 25 loglogistic4\_gradient\_2, 26 loglogistic4\_gradient\_hessian (loglogistic4\_gradient), 25 loglogistic4\_gradient\_hessian\_2 (loglogistic4\_gradient\_2), 26 loglogistic4\_hessian (loglogistic4\_gradient), 25 loglogistic4\_hessian\_2 (loglogistic4\_gradient\_2), 26 loglogistic5\_fn, 27 loglogistic5\_gradient, 28 loglogistic5\_gradient\_2, 28 loglogistic5\_gradient\_hessian (loglogistic5\_gradient), 28 loglogistic5\_gradient\_hessian\_2 (loglogistic5\_gradient\_2), 28 loglogistic5\_hessian (loglogistic5\_gradient), 28 loglogistic5\_hessian\_2 (loglogistic5\_gradient\_2), 28 loglogistic6\_fn, 29 loglogistic6\_gradient, 30 loglogistic6\_gradient\_2, 31 loglogistic6\_gradient\_hessian (loglogistic6\_gradient), 30 loglogistic6\_gradient\_hessian\_2 (loglogistic6\_gradient\_2), 31 loglogistic6\_hessian (loglogistic6\_gradient), 30 loglogistic6\_hessian\_2 (loglogistic6\_gradient\_2), 31

model.frame,6

na.fail,*3* naac, 32,*34* nauc, *33*, 33 options, *3* plot.drda, 34 terms, *6* voropm2, 35