

Package ‘targeted’

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Type Package

Title Targeted Inference

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Description Various methods for targeted and semiparametric inference including augmented inverse probability weighted (AIPW) estimators for missing data and causal inference (Bang and Robins (2005) <[doi:10.1111/j.1541-0420.2005.00377.x](https://doi.org/10.1111/j.1541-0420.2005.00377.x)>), variable importance and conditional average treatment effects (CATE) (van der Laan (2006) <[doi:10.2202/1557-4679.1008](https://doi.org/10.2202/1557-4679.1008)>), estimators for risk differences and relative risks (Richardson et al. (2017) <[doi:10.1080/01621459.2016.1192546](https://doi.org/10.1080/01621459.2016.1192546)>), assumption lean inference for generalized linear model parameters (Vansteelandt et al. (2022) <[doi:10.1111/rssb.12504](https://doi.org/10.1111/rssb.12504)>).

Depends R (>= 4.0), lava (>= 1.7.0)

Imports data.table, digest, futile.logger, future.apply, optimx,
progressr, methods, mets, R6, Rcpp (>= 1.0.0), survival

Suggests grf, mgcv, testthat (>= 0.11), rmarkdown, scatterplot3d,
SuperLearner (>= 2.0-28), knitr, xgboost, viridisLite

BugReports <https://github.com/kkholst/targeted/issues>

License Apache License (== 2.0)

LinkingTo Rcpp, RcppArmadillo

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aipw

AIPW estimator

Description

AIPW for the mean (and linear projections of the EIF) with missing observations

Usage

```
aipw(response_model, data, formula = ~1, missing_model, ...)
```

Arguments

```
response_model  Model for the response given covariates (ml_model or formula)
data            data.frame
formula        design specifying the OLS estimator with outcome given by the EIF
missing_model  Optional missing_model (ml_model or formula). By default will use the same
               design as the response_model.
...            arguments to cate
```

Examples

```
m <- lvm(y ~ x+z, r ~ x)
distribution(m,~ r) <- binomial.lvm()
transform(m, y0~r+y) <- function(x) { x[x[,1]==0,2] <- NA; x[,2] }
d <- sim(m,1e3,seed=1)

aipw(y0 ~ x, data=d)
```

alean

Assumption Lean inference for generalized linear model parameters

Description

Assumption lean inference via cross-fitting (Double ML). See <doi:10.1111/rssb.12504

Usage

```
alean(
  response_model,
  exposure_model,
  data,
  link = "identity",
  g_model,
  nfolds = 1,
  silent = FALSE,
  mc.cores,
  ...
)
```

Arguments

response_model formula or ml_model object (formula => glm)
 exposure_model model for the exposure
 data data.frame
 link Link function (g)
 g_model Model for $E[g(Y|A, W)|W]$
 nfolds Number of folds
 silent suppress all messages and progressbars
 mc.cores mc.cores Optional number of cores. parallel::mcmapply used instead of future
 ... additional arguments to future.apply::future_mapply

Details

Let Y be the response variable, A the exposure and W covariates. The target parameter is:

$$\Psi(P) = \frac{E(\text{Cov}[A, g\{E(Y|A, W)\} | W])}{E\{\text{Var}(A | W)\}}$$

The response_model is the model for $E(Y|A, W)$, and exposure_model is the model for $E(A|W)$. link specifies g .

Value

alean.targeted object

Author(s)

Klaus Kähler Holst

Examples

```

sim1 <- function(n, family=gaussian(), ...) {
  m <- lvm() |>
  distribution(~ y, binomial.lvm()) |>
  regression('a', value=function(l) l) |>
  regression('y', value=function(a,l) a + l)
  if (family$family=="binomial")
    distribution(m, ~a) <- binomial.lvm()
  sim(m, n)
}

library(splines)
f <- binomial()
d <- sim1(1e4, family=f)
e <- alean(response_model=ML(y ~ a + bs(1, df=3), family=binomial),
           exposure_model=ML(a ~ bs(1, df=3), family=f),
           data=d,

```

```

link = "logit", mc.cores=1, nfold=1)
e
e <- alean(response_model=ML(y ~ a + 1, family=binomial),
           exposure_model=ML(a ~ 1),
           data=d,
           link = "logit", mc.cores=1, nfold=1)
e

```

ate

*AIPW (doubly-robust) estimator for Average Treatment Effect***Description**

Augmented Inverse Probability Weighting estimator for the Average (Causal) Treatment Effect. All nuisance models are here parametric (glm). For a more general approach see the `cate` implementation. In this implementation the standard errors are correct even when the nuisance models are misspecified (the influence curve is calculated including the term coming from the parametric nuisance models). The estimate is consistent if either the propensity model or the outcome model / Q-model is correctly specified.

Usage

```

ate(
  formula,
  data = parent.frame(),
  weights,
  offset,
  family = stats::gaussian(identity),
  nuisance = NULL,
  propensity = nuisance,
  all,
  labels = NULL,
  ...
)

```

Arguments

<code>formula</code>	Formula (see details below)
<code>data</code>	<code>data.frame</code>
<code>weights</code>	optional frequency weights
<code>offset</code>	optional offset (character or vector). can also be specified in the formula.
<code>family</code>	Exponential family argument for outcome model
<code>nuisance</code>	outcome regression formula (Q-model)
<code>propensity</code>	propensity model formula

all	If TRUE all standard errors are calculated (default TRUE when exposure only has two levels)
labels	Optional treatment labels
...	Additional arguments to lower level functions

Details

The formula may either be specified as: `response ~ treatment | nuisance-formula | propensity-formula`

For example: `ate(y~a | x+z+a | x*z, data=...)`

Alternatively, as a list: `ate(list(y~a, ~x+z, ~x*z), data=...)`

Or using the nuisance (and propensity argument): `ate(y~a, nuisance=~x+z, ...)`

Value

An object of class 'ate.targeted' is returned. See [targeted-class](#) for more details about this class and its generic functions.

Author(s)

Klaus K. Holst

See Also

`cate`

Examples

```
m <- lvm(y ~ a+x, a~x)
distribution(m, ~y) <- binomial.lvm()
m <- ordinal(m, K=4, ~a)
transform(m, ~a) <- factor
d <- sim(m, 1e3, seed=1)
(a <- ate(y~a|a*x|x, data=d))
## ate(y~a, nuisance=~a*x, propensity=~x, ...)

# Comparison with randomized experiment
m0 <- cancel(m, a~x)
lm(y~a-1, sim(m0,2e4))

# Choosing a different contrast for the association measures
summary(a, contrast=c(2,4))
```

calibration	<i>Calibration (training)</i>
-------------	-------------------------------

Description

Calibration for multiclassification methods

Usage

```
calibration(  
  pr,  
  cl,  
  weights = NULL,  
  threshold = 10,  
  method = "bin",  
  breaks = nclass.Sturges,  
  df = 3,  
  ...  
)
```

Arguments

pr	matrix with probabilities for each class
cl	class variable
weights	counts
threshold	do not calibrate if less then 'threshold' events
method	either 'isotonic' (pava), 'logistic', 'mspline' (monotone spline), 'bin' (local constant)
breaks	optional number of bins (only for method 'bin')
df	degrees of freedom (only for spline methods)
...	additional arguments to lower level functions

Details

...

Value

An object of class 'calibration' is returned. See [calibration-class](#) for more details about this class and its generic functions.

Author(s)

Klaus K. Holst

Examples

```

sim1 <- function(n, beta=c(-3, rep(.5,10)), rho=.5) {
  p <- length(beta)-1
  xx <- lava::rmvn0(n,sigma=diag(nrow=p)*(1-rho)+rho)
  y <- rbinom(n, 1, lava::expit(cbind(1,xx)%*%beta))
  d <- data.frame(y=y, xx)
  names(d) <- c("y",paste0("x",1:p))
  return(d)
}

set.seed(1)
beta <- c(-2,rep(1,10))
d <- sim1(1e4, beta=beta)
a1 <- NB(y ~ ., data=d)
a2 <- glm(y ~ ., data=d, family=binomial)
## a3 <- randomForest(factor(y) ~ ., data=d, family=binomial)

d0 <- sim1(1e4, beta=beta)
p1 <- predict(a1, newdata=d0)
p2 <- predict(a2, newdata=d0, type="response")
## p3 <- predict(a3, newdata=d0, type="prob")

c2 <- calibration(p2, d0$y, method="isotonic")
c1 <- calibration(p1, d0$y, breaks=100)
if (interactive()) {
  plot(c1)
  plot(c2,col="red",add=TRUE)
  abline(a=0,b=1)##'
  with(c1$xy[[1]], points(pred,freq,type="b", col="red"))
}

set.seed(1)
beta <- c(-2,rep(1,10))
dd <- lava::csplit(sim1(1e4, beta=beta), k=3)
mod <- NB(y ~ ., data=dd[[1]])
p1 <- predict(mod, newdata=dd[[2]])
cal <- calibration(p1, dd[[2]]$y)
p2 <- predict(mod, newdata=dd[[3]])
pp <- predict(c1, p2)
cc <- calibration(pp, dd[[3]]$y)
if (interactive()) {##'
  plot(cal)
  plot(cc, add=TRUE, col="blue")
}

```


Description

The functions `calibration` returns an object of the class `calibration`.

An object of class 'calibration' is a list with at least the following components:

stepfun estimated step-functions (see `stepfun`) for each class

classes the unique classes

model model/method type (string)

xy list of data.frame's with predictions (`pr`) and estimated probabilities of success (only for 'bin' method)

Value

objects of the S3 class 'calibration'

S3 generics

The following S3 generic functions are available for an object of class targeted:

`predict` Apply calibration to new data.

`plot` Plot the calibration curves (reliability plot).

`print` Basic print method.

See Also

[calibration](#), [calibrate](#)

Examples

```
## See example(calibration) for examples
```

cate

Conditional Average Treatment Effect estimation

Description

Conditional Average Treatment Effect estimation via Double Machine Learning

Usage

```
cate(
  treatment,
  response_model,
  propensity_model,
  contrast = c(1, 0),
  data,
  nfold = 5,
```

```

    type = "dml2",
    silent = FALSE,
    stratify = FALSE,
    mc.cores,
    ...
  )

```

Arguments

treatment	formula specifying treatment and variables to condition on
response_model	formula or ml_model object (formula => glm)
propensity_model	formula or ml_model object (formula => glm)
contrast	treatment contrast (default 1 vs 0)
data	data.frame
nfolds	Number of folds
type	'dml1' or 'dml2'
silent	suppress all messages and progressbars
stratify	If TRUE the response_model will be stratified by treatment
mc.cores	mc.cores Optional number of cores. parallel::mcmapply used instead of future
...	additional arguments to future.apply::future_mapply

Value

cate.targeted object

Author(s)

Klaus Kähler Holst

Examples

```

sim1 <- function(n=1e4,
                seed=NULL,
                return_model=FALSE, ...) {
  suppressPackageStartupMessages(require("lava"))
  if (!is.null(seed)) set.seed(seed)
  m <- lava::lvm()
  regression(m, ~a) <- function(z1,z2,z3,z4,z5)
    cos(z1)+sin(z1*z2)+z3+z4+z5^2
  regression(m, ~u) <- function(a,z1,z2,z3,z4,z5)
    (z1+z2+z3)*a + z1+z2+z3 + a
  distribution(m, ~a) <- binomial.lvm()
  if (return_model) return(m)
  lava::sim(m, n, p=par)
}

d <- sim1(200)

```

```
e <- cate(a ~ z1+z2+z3, response=u~., data=d)
e
```

cate_link

Conditional Relative Risk estimation

Description

Conditional average treatment effect estimation via Double Machine Learning

Usage

```
cate_link(
  treatment,
  link = "identity",
  response_model,
  propensity_model,
  importance_model,
  contrast = c(1, 0),
  data,
  nfolds = 5,
  type = "dml1",
  ...
)
```

Arguments

treatment	formula specifying treatment and variables to condition on
link	Link function
response_model	SL object
propensity_model	SL object
importance_model	SL object
contrast	treatment contrast (default 1 vs 0)
data	data.frame
nfolds	Number of folds
type	'dml1' or 'dml2'
...	additional arguments to SuperLearner

Value

cate.targeted object

Author(s)

Klaus Kähler Holst & Andreas Nordland

Examples

```
# Example 1:
sim1 <- function(n=1e4,
                 seed=NULL,
                 return_model=FALSE, ...){
  suppressPackageStartupMessages(require("lava"))
  if (!is.null(seed)) set.seed(seed)
  m <- lava::lvm()
  distribution(m, ~x) <- gaussian.lvm()
  distribution(m, ~v) <- gaussian.lvm(mean = 10)
  distribution(m, ~a) <- binomial.lvm("logit")
  regression(m, "a") <- function(v, x){.1*v + x}
  distribution(m, "y") <- gaussian.lvm()
  regression(m, "y") <- function(a, v, x){v+x+a*x+a*v*v}
  if (return_model) return(m)
  lava::sim(m, n = n)
}

if (require("SuperLearner",quietly=TRUE)) {
  d <- sim1(n = 1e3, seed = 1)
  e <- cate_link(data=d,
                 type = "dm12",
                 treatment = a ~ v,
                 response_model = y~ a*(x + v + I(v^2)),
                 importance_model = SL(D_ ~ v + I(v^2)),
                 nfolds = 10)
  summary(e) # the true parameters are c(1,1)
}
```

cross_validated-class *cross_validated class object*

Description

The functions `cv` returns an object of the type `cross_validated`.

An object of class 'cross_validated' is a list with at least the following components:

cv An array with the model score(s) evaluated for each fold, repetition, and model estimates (see [estimate.default](#))

names Names (character vector) of the models

rep number of repetitions of the CV

folds Number of folds of the CV

Value

objects of the S3 class 'cross_validated'

S3 generics

The following S3 generic functions are available for an object of class cross_validated:

coef Extract average model scores from the cross-validation procedure.

print Basic print method.

summary Summary of the cross-validation procedure.'

See Also

[cv](#)

Examples

```
## See example(cv) for examples
```

crr

Conditional Relative Risk estimation

Description

Conditional Relative Risk estimation via Double Machine Learning

Usage

```
crr(
  treatment,
  response_model,
  propensity_model,
  importance_model,
  contrast = c(1, 0),
  data,
  nfolds = 5,
  type = "dml1",
  ...
)
```

Arguments

treatment formula specifying treatment and variables to condition on

response_model SL object

propensity_model
SL object

importance_model	SL object
contrast	treatment contrast (default 1 vs 0)
data	data.frame
nfolds	Number of folds
type	'dml1' or 'dml2'
...	additional arguments to SuperLearner

Value

cate.targeted object

Author(s)

Klaus Kähler Holst & Andreas Nordland

Examples

```

sim1 <- function(n=1e4,
                seed=NULL,
                return_model=FALSE, ...){
  suppressPackageStartupMessages(require("lava"))
  if (!is.null(seed)) set.seed(seed)
  m <- lava::lvm()
  distribution(m, ~x) <- gaussian.lvm()
  distribution(m, ~v) <- gaussian.lvm(mean = 10)
  distribution(m, ~a) <- binomial.lvm("logit")
  regression(m, "a") <- function(v, x){.1*v + x}
  distribution(m, "y") <- gaussian.lvm()
  regression(m, "y") <- function(a, v, x){v+x+a*x+a*v*v}
  if (return_model) return(m)
  lava::sim(m, n = n)
}

d <- sim1(n = 2e3, seed = 1)
if (require("SuperLearner",quietly=TRUE)) {
  e <- crr(data=d,
           type = "dml2",
           treatment = a ~ v,
           response_model = ML(y~ a*(x + v + I(v^2))),
           importance_model = ML(D_ ~ v + I(v^2)),
           propensity_model = ML(a ~ x + v + I(v^2), family=binomial),
           nfolds = 2)
  summary(e) # the true parameters are c(1,1)
}

```

Description

Generic cross-validation function

Usage

```
cv(
  models,
  data,
  response = NULL,
  nfolds = 5,
  rep = 1,
  weights = NULL,
  modelscore,
  seed = NULL,
  shared = NULL,
  args.pred = NULL,
  args.future = list(),
  mc.cores,
  ...
)
```

Arguments

models	List of fitting functions
data	data.frame or matrix
response	Response variable (vector or name of column in data).
nfolds	Number of folds (default 5. K=0 splits in 1:n/2, n/2:n with last part used for testing)
rep	Number of repetitions (default 1)
weights	Optional frequency weights
modelscore	Model scoring metric (default: MSE / Brier score). Must be a function with arguments: response, prediction, weights, ...
seed	Random seed (argument parsed to future_Apply::future_lapply)
shared	Function applied to each fold with results send to each model
args.pred	Optional arguments to prediction function (see details below)
args.future	Arguments to future.apply::future_mapply
mc.cores	Optional number of cores. parallel::mcmapply used instead of future
...	Additional arguments parsed to models in models

Details

models should be list of objects of class `ml_model`. Alternatively, each element of models should be a list with a fitting function and a prediction function.

The response argument can optionally be a named list where the name is then used as the name of the response argument in models. Similarly, if data is a named list with a single `data.frame`/matrix then this name will be used as the name of the data/design matrix argument in models.

Value

An object of class `'cross_validated'` is returned. See [cross_validated-class](#) for more details about this class and its generic functions.

Author(s)

Klaus K. Holst

Examples

```
f0 <- function(data,...) lm(...,data=data)
f1 <- function(data,...) lm(Sepal.Length~Species,data=data)
f2 <- function(data,...) lm(Sepal.Length~Species+Petal.Length,data=data)
x <- cv(list(m0=f0,m1=f1,m2=f2),rep=10, data=iris, formula=Sepal.Length~.)
x
```

design	<i>Extract design matrix</i>
--------	------------------------------

Description

Extract design matrix from `data.frame` and formula

Usage

```
design(formula, data, intercept = FALSE, rm_envir = FALSE, ...)
```

Arguments

formula	formula
data	<code>data.frame</code>
intercept	If FALSE (default) an intercept is not included
rm_envir	Remove environment
...	additional arguments (e.g, specials such weights, offsets, subset)

Value

An object of class `'design'`

Author(s)

Klaus Kähler Holst

`expand.list`*Create a list from all combination of input variables*

Description

Similar to `expand.grid` function, this function creates all combinations of the input arguments but returns the result as a list.

Usage

```
expand.list(...)
```

Arguments

```
...          input variables
```

Value

list

Author(s)

Klaus Kähler Holst

Examples

```
expand.list(x=2:4, z=c("a","b"))
```

`ML`*ML model*

DescriptionWrapper for `ml_model`**Usage**

```
ML(formula, model = "glm", ...)
```

Arguments

```
formula      formula  
model        model (sl, rf, pf, glm, ...)  
...          additional arguments to model object
```

Details

model 'sl' (SuperLearner::SuperLearner) args: SL.library, cvControl, f<aamily, method example:
 model 'grf' (grf::regression_forest) args: num.trees, mtry, sample.weights, sample.fraction, min.node.size,
 ... example:
 model 'grf.binary' (grf::probability_forest) args: num.trees, mtry, sample.weights, ... example:
 model 'glm' args: family, weights, offset, ...

 ml_model

R6 class for prediction models

Description

Provides standardized estimation and prediction methods

Public fields

info Optional information/name of the model
 formals List with formal arguments of estimation and prediction functions
 formula Formula specifying response and design matrix
 args additional arguments specified during initialization

Active bindings

fit Active binding returning estimated model object

Methods**Public methods:**

- [ml_model\\$new\(\)](#)
- [ml_model\\$estimate\(\)](#)
- [ml_model\\$predict\(\)](#)
- [ml_model\\$update\(\)](#)
- [ml_model\\$print\(\)](#)
- [ml_model\\$response\(\)](#)
- [ml_model\\$design\(\)](#)
- [ml_model\\$opt\(\)](#)
- [ml_model\\$clone\(\)](#)

Method `new()`: Create a new prediction model object

Usage:

```
ml_model$new(
  formula = NULL,
  estimate,
  predict = stats::predict,
  predict.args = NULL,
  info = NULL,
  specials,
  response.arg = "y",
  x.arg = "x",
  ...
)
```

Arguments:

formula formula specifying outcome and design matrix

estimate function for fitting the model (must be a function response, 'y', and design matrix, 'x'. Alternatively, a function with a single 'formula' argument)

predict prediction function (must be a function of model object, 'object', and new design matrix, 'newdata')

predict.args optional arguments to prediction function

info optional description of the model

specials optional additional terms (weights, offset, id, subset, ...) passed to 'estimate'

response.arg name of response argument

x.arg name of design matrix argument

... optional arguments to fitting function

Method estimate(): Estimation method*Usage:*

```
ml_model$estimate(data, ..., store = TRUE)
```

Arguments:

data data.frame

... Additional arguments to estimation method

store Logical determining if estimated model should be stored inside the class.

Method predict(): Prediction method*Usage:*

```
ml_model$predict(newdata, ..., object = NULL)
```

Arguments:

newdata data.frame

... Additional arguments to prediction method

object Optional model fit object

Method update(): Update formula*Usage:*

```
ml_model$update(formula, ...)
```

Arguments:

formula formula or character which defines the new response
... Additional arguments to lower level functions

Method print(): Print method

Usage:

```
ml_model$print(...)
```

Arguments:

... Additional arguments to lower level functions

Method response(): Extract response from data

Usage:

```
ml_model$response(data, ...)
```

Arguments:

data data.frame

... additional arguments to 'design'

Method design(): Extract design matrix (features) from data

Usage:

```
ml_model$design(data, ...)
```

Arguments:

data data.frame

... additional arguments to 'design'

Method opt(): Get options

Usage:

```
ml_model$opt(arg, ...)
```

Arguments:

arg name of option to get value of

... additional arguments to lower level functions

Method clone(): The objects of this class are cloneable with this method.

Usage:

```
ml_model$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

Author(s)

Klaus Kähler Holst

Examples

```

data(iris)
rf <- function(formula, ...)
ml_model$new(formula, info="grf::probability_forest",
  estimate=function(x,y, ...) grf::probability_forest(X=x, Y=y, ...),
  predict=function(object, newdata)
    predict(object, newdata)$predictions, ...)

args <- expand.list(num.trees=c(100,200), mtry=1:3,
  formula=c(Species ~ ., Species ~ Sepal.Length + Sepal.Width))
models <- lapply(args, function(par) do.call(rf, par))

x <- models[[1]]$clone()
x$estimate(iris)
predict(x, newdata=head(iris))

# Reduce Ex. timing
a <- targeted::cv(models, data=iris)
cbind(coef(a), attr(args, "table"))

ff <- ml_model$new(estimate=function(y,x) lm.fit(x=x, y=y),
  predict=function(object, newdata) newdata%*%object$coefficients)
## tmp <- ff$estimate(y, x=x)
## ff$predict(x)

```

 NB

Naive Bayes

Description

Naive Bayes Classifier

Usage

```

NB(
  formula,
  data,
  weights = NULL,
  kernel = FALSE,
  laplace.smooth = 0,
  prior = NULL,
  ...
)

```

Arguments

formula Formula with syntax: response ~ predictors | weights

<code>data</code>	<code>data.frame</code>
<code>weights</code>	optional frequency weights
<code>kernel</code>	If TRUE a kernel estimator is used for numeric predictors (otherwise a gaussian model is used)
<code>laplace.smooth</code>	Laplace smoothing
<code>prior</code>	optional prior probabilities (default estimated from data)
<code>...</code>	additional arguments to lower level functions

Value

An object of class 'NB' is returned. See [NB-class](#) for more details about this class and its generic functions.

Author(s)

Klaus K. Holst

Examples

```
data(iris)
m2 <- NB(Species ~ Sepal.Width + Petal.Length, data=iris)
pr2 <- predict(m2, newdata=iris)
```

NB-class

NB class object

Description

The functions [NB](#) returns an object of the type NB.

An object of class 'NB' is a list with at least the following components:

prior Matrix with prior probabilities, i.e. marginal class probabilities $\Pr(\text{class})$

pcond list of matrices with conditional probabilities of the features given the classes (one list element per class), $\Pr(x|\text{class})$

classes Names (character vector) of the classes

xvar number of repetitions of the CV

xmodel Number of folds of the CV

model Number of folds of the CV

Value

objects of the S3 class 'NB'

S3 generics

The following S3 generic functions are available for an object of class NB:

`predict` Predict class probabilities for new features data.
`print` Basic print method.

See Also

[NB](#), [NB2](#)

Examples

```
## See example(NB) for examples
```

nondom	<i>Find non-dominated points of a set</i>
--------	---

Description

Find the non-dominated point of a set (minima of a point set).

Usage

```
nondom(x, ...)
```

Arguments

<code>x</code>	matrix
<code>...</code>	additional arguments to lower level functions

Details

A point x dominates y if it is never worse and at least in one case strictly better. Formally, let f_i denote the i th coordinate of the condition (objective) function, then for all i : $f_i(x) \leq f_i(y)$ and there exists j : $f_j(x) < f_j(y)$.

Based on the algorithm of Kung et al. 1975.

Value

matrix

Author(s)

Klaus Kähler Holst

Examples

```

rbind(
  c(1.0, 0.5),
  c(0.0, 1.0),
  c(1.0, 0.0),
  c(0.5, 1.0),
  c(1.0, 1.0),
  c(0.8, 0.8)) |> nondom()

```

pava

Pooled Adjacent Violators Algorithm

Description

Pooled Adjacent Violators Algorithm

Usage

```
pava(y, x = numeric(0), weights = numeric(0))
```

Arguments

y	response variable
x	(optional) predictor vector (otherwise y is assumed to be a priori sorted according to relevant predictor)
weights	weights (optional) weights

Value

List with index (idx) of jump points and values (value) at each jump point.

Author(s)

Klaus K. Holst

Examples

```

x <- runif(5e3, -5, 5)
pr <- lava::expit(-1 + x)
y <- rbinom(length(pr), 1, pr)
pv <- pava(y, x)
plot(pr ~ x, cex=0.3)
with(pv, lines(sort(x)[index], value, col="red", type="s"))

```

predict.density *Prediction for kernel density estimates*

Description

Kernel density estimator predictions

Usage

```
## S3 method for class 'density'
predict(object, xnew, ...)
```

Arguments

object	density object
xnew	New data on which to make predictions for
...	additional arguments to lower level functions

Author(s)

Klaus K. Holst

predict.NB *Predictions for Naive Bayes Classifier*

Description

Naive Bayes Classifier predictions

Usage

```
## S3 method for class 'NB'
predict(object, newdata, expectation = NULL, threshold = c(0.001, 0.001), ...)
```

Arguments

object	density object
newdata	new data on which to make predictions
expectation	Variable to calculate conditional expectation wrt probabilities from NB classifier
threshold	Threshold parameters. First element defines the threshold on the probabilities and the second element the value to set those truncated probabilities to.
...	Additional arguments to lower level functions

Author(s)

Klaus K. Holst

RATE *Responder Average Treatment Effect*

Description

Estimation of the Average Treatment Effect among Responders

Usage

```
RATE(
  response,
  post.treatment,
  treatment,
  data,
  family = gaussian(),
  M = 5,
  pr.treatment,
  treatment.level,
  SL.args.response = list(family = gaussian(), SL.library = c("SL.mean", "SL.glm")),
  SL.args.post.treatment = list(family = binomial(), SL.library = c("SL.mean", "SL.glm")),
  preprocess = NULL,
  efficient = TRUE,
  ...
)
```

Arguments

<code>response</code>	Response formula (e.g, $Y \sim D * A$)
<code>post.treatment</code>	Post treatment marker formula (e.g., $D \sim W$)
<code>treatment</code>	Treatment formula (e.g, $A \sim 1$)
<code>data</code>	<code>data.frame</code>
<code>family</code>	Exponential family for response (default gaussian)
<code>M</code>	Number of folds in cross-fitting ($M=1$ is no cross-fitting)
<code>pr.treatment</code>	(optional) Randomization probability of treatment.
<code>treatment.level</code>	Treatment level in binary treatment (default 1)
<code>SL.args.response</code>	Arguments to SuperLearner for the response model
<code>SL.args.post.treatment</code>	Arguments to SuperLearner for the post treatment indicator
<code>preprocess</code>	(optional) Data preprocessing function
<code>efficient</code>	If TRUE, the estimate will be efficient. If FALSE, the estimate will be a simple plug-in estimate.
<code>...</code>	Additional arguments to lower level functions

Value

estimate object

Author(s)

Andreas Nordland, Klaus K. Holst

RATE.surv

Responder Average Treatment Effect

Description

Estimation of the Average Treatment Effect among Responders for Survival Outcomes

Usage

```
RATE.surv(
  response,
  post.treatment,
  treatment,
  censoring,
  tau,
  data,
  M = 5,
  pr.treatment,
  call.response,
  args.response = list(),
  SL.args.post.treatment = list(family = binomial(), SL.library = c("SL.mean", "SL.glm")),
  call.censoring,
  args.censoring = list(),
  preprocess = NULL,
  ...
)
```

Arguments

response	Response formula (e.g., $\text{Surv}(\text{time}, \text{event}) \sim D + W$).
post.treatment	Post treatment marker formula (e.g., $D \sim W$).
treatment	Treatment formula (e.g., $A \sim 1$).
censoring	Censoring formula (e.g., $\text{Surv}(\text{time}, \text{event} == 0) \sim D + A + W$).
tau	Time-point of interest, see Details.
data	data.frame.
M	Number of folds in cross-fitting (M=1 is no cross-fitting).
pr.treatment	(optional) Randomization probability of treatment.

`call.response` Model call for the response model (e.g. "mets::phreg").
`args.response` Additional arguments to the response model.
`SL.args.post.treatment`
 Additional arguments to SuperLearner for the post treatment indicator model.
`call.censoring` Similar to `call.response`.
`args.censoring` Similar to `args.response`.
`preprocess` (optional) Data pre-processing function.
`...` Additional arguments to lower level data pre-processing functions.

Details

Estimation of

$$\frac{P(T \leq \tau | A = 1) - P(T \leq \tau | A = 0)}{E[D | A = 1]}$$

under right censoring based on plug-in estimates of $P(T \leq \tau | A = a)$ and $E[D | A = 1]$.

An efficient one-step estimator of $P(T \leq \tau | A = a)$ is constructed using the efficient influence function

$$\frac{I\{A = a\}}{P(A = a)} \left(\frac{\Delta}{S_0^c(\tilde{T} | X)} I\{\tilde{T} \leq \tau\} + \int_0^\tau \frac{S_0(u | X) - S_0(\tau | X)}{S_0(u | X) S_0^c(u | X)} dM_0^c(u | X) \right) + \left(1 - \frac{I\{A = a\}}{P(A = a)} \right) F_0(\tau | A = a, W) - P(T \leq \tau | A = a)$$

An efficient one-step estimator of $E[D | A = 1]$ is constructed using the efficient influence function

$$\frac{A}{P(A = 1)} (D - E[D | A = 1, W]) + E[D | A = 1, W] - E[D | A = 1].$$

Value

estimate object

Author(s)

Andreas Nordland, Klaus K. Holst

riskreg

Risk regression

Description

Risk regression with binary exposure and nuisance model for the odds-product.

Let A be the binary exposure, V the set of covariates, and Y the binary response variable, and define $p_a(v) = P(Y = 1 | A = a, V = v)$, $a \in \{0, 1\}$.

The **target parameter** is either the *relative risk*

$$RR(v) = \frac{p_1(v)}{p_0(v)}$$

or the *risk difference*

$$RD(v) = p_1(v) - p_0(v)$$

We assume a target parameter model given by either

$$\log\{RR(v)\} = \alpha^t v$$

or

$$\operatorname{arctanh}\{RD(v)\} = \alpha^t v$$

and similarly a working linear **nuisance model** for the *odds-product*

$$\phi(v) = \log\left(\frac{p_0(v)p_1(v)}{(1-p_0(v))(1-p_1(v))}\right) = \beta^t v$$

.

A **propensity model** for $E(A = 1|V)$ is also fitted using a logistic regression working model

$$\operatorname{logit}\{E(A = 1 | V = v)\} = \gamma^t v.$$

If both the odds-product model and the propensity model are correct the estimator is efficient. Further, the estimator is consistent in the union model, i.e., the estimator is double-robust in the sense that only one of the two models needs to be correctly specified to get a consistent estimate.

Usage

```
riskreg(
  formula,
  nuisance = ~1,
  propensity = ~1,
  target = ~1,
  data,
  weights,
  type = "rr",
  optimal = TRUE,
  std.err = TRUE,
  start = NULL,
  mle = FALSE,
  ...
)
```

Arguments

formula	formula (see details below)
nuisance	nuisance model (formula)
propensity	propensity model (formula)
target	(optional) target model (formula)
data	data.frame
weights	optional weights

type	type of association measure (rd og rr)
optimal	If TRUE optimal weights are calculated
std.err	If TRUE standard errors are calculated
start	optional starting values
mle	Semi-parametric (double-robust) estimate or MLE (TRUE gives MLE)
...	additional arguments to unconstrained optimization routine (nlminb)

Details

The 'formula' argument should be given as response ~ exposure | target-formula | nuisance-formula or response ~ exposure | target | nuisance | propensity

E.g., `riskreg(y ~ a | 1 | x+z | x+z, data=...)`

Alternatively, the model can specified using the target, nuisance and propensity arguments: `riskreg(y ~ a, target=~1, nuisance=~x+z, ...)`

The `riskreg_fit` function can be used with matrix inputs rather than formulas.

Value

An object of class 'riskreg.targeted' is returned. See [targeted-class](#) for more details about this class and its generic functions.

Author(s)

Klaus K. Holst

References

Richardson, T. S., Robins, J. M., & Wang, L. (2017). On modeling and estimation for the relative risk and risk difference. *Journal of the American Statistical Association*, 112(519), 1121–1130. <http://dx.doi.org/10.1080/01621459.2016.1192546>

Examples

```
m <- lvm(a[-2] ~ x,
        z ~ 1,
        lp.target[1] ~ 1,
        lp.nuisance[-1] ~ 2*x)
distribution(m,~a) <- binomial.lvm("logit")
m <- binomial.rr(m, "y", "a", "lp.target", "lp.nuisance")
d <- sim(m,5e2,seed=1)

I <- model.matrix(~1, d)
X <- model.matrix(~1+x, d)
with(d, riskreg_mle(y, a, I, X, type="rr"))

with(d, riskreg_fit(y, a, nuisance=X, propensity=I, type="rr"))
riskreg(y ~ a | 1, nuisance=~x , data=d, type="rr")
```

```

## Model with same design matrix for nuisance and propensity model:
with(d, riskreg_fit(y, a, nuisance=X, type="rr"))

## a <- riskreg(y ~ a, target=~z, nuisance=~x, propensity=~x, data=d, type="rr")
a <- riskreg(y ~ a | z, nuisance=~x, propensity=~x, data=d, type="rr")
a
predict(a, d[1:5,])

riskreg(y ~ a, nuisance=~x, data=d, type="rr", mle=TRUE)

```

riskreg_cens

Binary regression models with right censored outcomes

Description

Binary regression models with right censored outcomes

Usage

```

riskreg_cens(
  response,
  censoring,
  treatment = NULL,
  prediction = NULL,
  data,
  newdata,
  tau,
  type = "risk",
  M = 1,
  call.response = "phreg",
  args.response = list(),
  call.censoring = "phreg",
  args.censoring = list(),
  preprocess = NULL,
  efficient = TRUE,
  control = list(),
  ...
)

```

Arguments

response	Response formula (e.g., $\text{Surv}(\text{time}, \text{event}) \sim D + W$).
censoring	Censoring formula (e.g., $\text{Surv}(\text{time}, \text{event} == 0) \sim D + A + W$).
treatment	Optional treatment model (<code>ml_model</code>)
prediction	Optional prediction model (<code>ml_model</code>)
data	<code>data.frame</code> .

<code>newdata</code>	Optional data.frame. In this case the uncentered influence function evaluated in 'newdata' is returned with nuisance parameters obtained from 'data'.
<code>tau</code>	Time-point of interest, see Details.
<code>type</code>	"risk", "treatment", "rmst", "brier"
<code>M</code>	Number of folds in cross-fitting (M=1 is no cross-fitting).
<code>call.response</code>	Model call for the response model (e.g. "mets::phreg").
<code>args.response</code>	Additional arguments to the response model.
<code>call.censoring</code>	Similar to call.response.
<code>args.censoring</code>	Similar to args.response.
<code>preprocess</code>	(optional) Data pre-processing function.
<code>efficient</code>	If FALSE an IPCW estimator is returned
<code>control</code>	See details
<code>...</code>	Additional arguments to lower level data pre-processing functions.

Details

The one-step estimator depends on the calculation of an integral wrt. the martingale process corresponding to the counting process $N(t) = I(C > \min(T, \tau))$. This can be decomposed into an integral wrt the counting process, $dN_c(t)$ and the compensator $d\Lambda_c(t)$ where the latter term can be computational intensive to calculate. Rather than calculating this integral in all observed time points, we can make a coarser evaluation which can be controlled by setting `control=(sample=N)`. With `N=0` the (computational intensive) standard evaluation is used.##'

Value

estimate object

Author(s)

Klaus K. Holst, Andreas Nordland

scoring

Predictive model scoring

Description

Predictive model scoring

Usage

```
scoring(
  response,
  ...,
  type = "quantitative",
  levels = NULL,
  metrics = NULL,
  weights = NULL,
  names = NULL,
  messages = 1
)
```

Arguments

response	Observed response
...	model predictions (continuous predictions or class probabilities (matrices))
type	continuous or categorical response (the latter is automatically chosen if response is a factor, otherwise a continuous response is assumed)
levels	(optional) unique levels in response variable
metrics	which metrics to report
weights	optional frequency weights
names	optional names of models comments (given as ..., alternatively these can be named arguments)
messages	controls amount of messages/warnings (0: none)

Value

Numeric matrix of dimension $m \times p$, where m is the number of different models and p is the number of model metrics

Examples

```
data(iris)
set.seed(1)
dat <- csplit(iris,2)
g1 <- NB(Species ~ Sepal.Width + Petal.Length, data=dat[[1]])
g2 <- NB(Species ~ Sepal.Width, data=dat[[1]])
pr1 <- predict(g1, newdata=dat[[2]], wide=TRUE)
pr2 <- predict(g2, newdata=dat[[2]], wide=TRUE)
table(colnames(pr1)[apply(pr1,1,which.max)], dat[[2]]$Species)
table(colnames(pr2)[apply(pr2,1,which.max)], dat[[2]]$Species)
scoring(dat[[2]]$Species, pr1=pr1, pr2=pr2)
## quantitative response:
scoring(response=1:10, prediction=rnorm(1:10))
```

SL	<i>SuperLearner wrapper for ml_model</i>
----	--

Description

SuperLearner wrapper for ml_model

Usage

```
SL(
  formula = ~.,
  ...,
  SL.library = c("SL.mean", "SL.glm"),
  binomial = FALSE,
  data = NULL
)
```

Arguments

formula	Model design
...	Additional arguments for SuperLearner::SuperLearner
SL.library	character vector of prediction algorithms
binomial	boolean specifying binomial or gaussian family (default FALSE)
data	Optional data.frame

Value

ml_model object

Author(s)

Klaus Kähler Holst

softmax	<i>Softmax transformation</i>
---------	-------------------------------

Description

Softmax transformation

Usage

```
softmax(x, log = FALSE, ref = TRUE, ...)
```

Arguments

x	Input matrix (e.g., linear predictors of multinomial logistic model)
log	Return on log-scale (default FALSE)
ref	Add reference level (add 0 column to x)
...	Additional arguments to lower level functions

Value

Numeric matrix of dimension $n \times p$, where $n = \text{nrow}(x)$ and $p = \text{ncol}(x) + (\text{ref} == \text{TRUE})$

solve_ode

Solve ODE

Description

Solve ODE with Runge-Kutta method (RK4)

Usage

```
solve_ode(ode_ptr, input, init, par = 0)
```

Arguments

ode_ptr	pointer (externalptr) to C++ function or an R function
input	Input matrix. 1st column specifies the time points
init	Initial conditions
par	Parameters defining the ODE (parsed to ode_ptr)

Details

The external point should be created with the function `targeted::specify_ode`.

Value

Matrix with solution

Author(s)

Klaus Kähler Holst

See Also

`specify_ode`

Examples

```
example(specify_ode)
```

specify_ode

*Specify Ordinary Differential Equation (ODE)***Description**

Define compiled code for ordinary differential equation.

Usage

```
specify_ode(code, fname = NULL, pname = c("dy", "x", "y", "p"))
```

Arguments

code	string with the body of the function definition (see details)
fname	Optional name of the exported C++ function
pname	Vector of variable names (results, inputs, states, parameters)

Details

The model (code) should be specified as the body of of C++ function. The following variables are defined by default (see the argument pname)

dy Vector with derivatives, i.e. the rhs of the ODE (the result).

x Vector with the first element being the time, and the following elements additional exogenous input variables,

y Vector with the dependent variable

p Parameter vector

$y'(t) = f_p(x(t), y(t))$ All variables are treated as Armadillo (<http://arma.sourceforge.net/>) vectors/matrices.

As an example consider the *Lorenz Equations* $\frac{dx_t}{dt} = \sigma(y_t - x_t)$ $\frac{dy_t}{dt} = x_t(\rho - z_t) - y_t$ $\frac{dz_t}{dt} = x_t y_t - \beta z_t$

We can specify this model as `ode <- 'dy(0) = p(0)*(y(1)-y(0)); dy(1) = y(0)*(p(1)-y(2)); dy(2) = y(0)*y(1)-p(2)*y(2);'` `dy <- specify_ode(ode)`

As an example of model with exogenous inputs consider the following ODE: $y'(t) = \beta_0 + \beta_1 y(t) + \beta_2 y(t)x(t) + \beta_3 x(t) \cdot t$ This could be specified as `mod <- 'double t = x(0); dy = p(0) + p(1)*y + p(2)*x(1)*y + p(3)*x(1)*t;'` `dy <- specify_ode(mod)##'`

Value

pointer (externalptr) to C++ function

Author(s)

Klaus Kähler Holst

See Also

`solve_ode`

targeted-class *targeted class object*

Description

The functions `riskreg` and `ate` returns an object of the type `targeted`.

An object of class 'targeted' is a list with at least the following components:

estimate An estimate object with the target parameter estimates (see `estimate.default`)

opt Object returned from the applied optimization routine

npar number of parameters of the model (target and nuisance)

type String describing the model

Value

objects of the S3 class 'targeted'

S3 generics

The following S3 generic functions are available for an object of class `targeted`:

`coef` Extract target coefficients of the estimated model.

`vcov` Extract the variance-covariance matrix of the target parameters.

`IC` Extract the estimated influence function.

`print` Print estimates of the target parameters.

`summary` Extract information on both target parameters and estimated nuisance model.'

See Also

`riskreg`, `ate`

Examples

```
## See example(riskreg) for examples
```

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