

Package ‘lglasso’

October 13, 2022

Type Package

Title Longitudinal Graphical Lasso

Version 0.1.0

Description For high-dimensional correlated observations, this package carries out the L_1 penalized maximum likelihood estimation of the precision matrix (network) and the correlation parameters. The correlated data can be longitudinal data (may be irregularly spaced) with dampening correlation or clustered data with uniform correlation. For the details of the algorithms, please see the paper Jie Zhou et al. Identifying Microbial Interaction Networks Based on Irregularly Spaced Longitudinal 16S rRNA sequence data <[doi:10.1101/2021.11.26.470159](https://doi.org/10.1101/2021.11.26.470159)>.

License GPL-3

Encoding UTF-8

LazyData true

RoxygenNote 7.1.2

URL <https://github.com/jiezhou-2/lglasso>

Suggests knitr, rmarkdown

Imports stats, glasso

Depends R (>= 2.10)

NeedsCompilation no

Author Jie Zhou [aut, cre, cph],
Jiang Gui [aut],
Weston Viles [aut],
Anne Hoen [aut]

Maintainer Jie Zhou <chowstat@gmail.com>

Repository CRAN

Date/Publication 2022-01-15 08:52:46 UTC

R topics documented:

heterlongraph	2
homolograph	3
iss	3
lglasso	4
lli_homo	6
ll_homo	7
logdensity	8
mle	8
mle_alpha	10
mle_net	10
mle_tau	11
phifunction	12
sample_data	12

Index	13
--------------	-----------

heterlongraph	<i>Estimates of correlation parameters and precision matrix</i>
---------------	---

Description

Estimates of correlation parameters and precision matrix

Usage

```
heterlongraph(data, rho, type, tole, lower, upper)
```

Arguments

data	Data matrix in which the first column is subject id, the second column is the time points of observation. Columns 2 to (p+2) is the observations for p variables.
rho	Tuning parameter used in graphical lasso
type	Type of correlation function, which can take either "abs" or "sqr".
tole	Error tolerance for determination of convergence of EM algorithm
lower	Lower bound for prediction of correlation parameter tau
upper	Upper bound for prediction of correlation parameter tau

Value

S list with three components which are the final estimate of alpha, tau and precision matrix omega

Author(s)

Jie Zhou

homolograph	<i>Estimate of precision matrix and autocorrelation parameter for homogeneous model</i>
-------------	---

Description

Estimate of precision matrix and autocorrelation parameter for homogeneous model

Usage

```
homolograph(data, rho, type, tole, lower, upper)
```

Arguments

data	Data matrix in which the first column is subject id, the second column is the time points of observation. Columns 2 to (p+2) is the observations for p variables.
rho	Tuning parameter for graphical lasso
type	Type of correlation function, which can take either "abs" or "qua".
tole	Error tolerance for determination of convergence of EM algorithm
lower	Lower bound for prediction of correlation parameter tau
upper	Upper bound for prediction of correlation parameter tau

Value

A list for estimates of precision matrix and correlation parameter for given tuning parameter

Author(s)

Jie Zhou

iss	<i>Quasi covariance matrix for subject i</i>
-----	--

Description

Quasi covariance matrix for subject i

Usage

```
iss(idata, itau, type)
```

Arguments

idata	Data matrix for the subject i in which the first column is subject (cluster) id, the second column stands for the time points () of observation. Columns 2 to $(p+2)$ is the observations for p variables respectively.
itau	Correlation parameter
type	Type of correlation function, which typically take either 0, 1 or 2.

Value

Empirical quasi covariance matrix

Author(s)

Jie Zhou

lglasso

Graphical Lasso for Longitudinal Data

Description

This function implements the L_1 penalized maximum likelihood estimation for precision matrix (network) based on correlated data, e.g., irregularly spaced longitudinal data. It can be regarded as an extension of the package `glasso` (Friedman, Hastie and Tibshirani, 2008) which aims to find the sparse estimate of the network from independent continuous data.

Usage

```
lglasso(
  data,
  rho,
  heter = TRUE,
  type = 1,
  tole = 0.01,
  lower = 0.01,
  upper = 10
)
```

Arguments

data	Data matrix in which the first column is subject id, the second column is time points of observations for temporal data or site id for spatial data. Columns 3 to $(p+2)$ is the observations for p variables.
rho	Tuning parameter used in L_1 penalty

heter	Binary variable TRUE or FALSE, indicating heterogeneous model or homogeneous model is fitted. In heterogeneous model, subjects are allowed to have his/her own temporal correlation parameter τ_i ; while in homogeneous model, all the subjects are assumed to share the same temporal correlation parameter, i.e., $\tau_1 = \tau_2 = \dots = \tau_m$.
type	A positive number which specifies the correlation function. The general form of correlation function is given by $\exp(\tau t_i - t_j ^{\text{type}})$. In which $\text{type} = 0$ can be used for spatial correlation while $\text{type} > 0$ are used for temporal correlation. For latter, the default value is set to be $\text{type} = 1$.
tole	Threshold for convergence. Default value is $1e-2$. Iterations stop when maximum absolute difference between consecutive estimates of parameter change is less than <i>tole</i> .
lower	Lower bound for predicts of correlation parameter τ . Default value is $1e-2$. The estimate of $\tau(\alpha)$ will be searched in the interval $[\text{lower}, \text{upper}]$, where parameter <i>upper</i> is explained in the following.
upper	Upper bound for predicts of correlation parameter τ .

Value

If *heter*=TRUE, then a list with three components is returned which are respectively the estimate of parameter α in exponent distribution, correlation parameter τ and precision matrix ω . If *heter*=FALSE, then a list with two components is returned which are respectively the estimate of correlation parameter τ and precision matrix ω .

Author(s)

Jie Zhou

References

Jie Zhou, Jiang Gui, Weston D.Viles, Anne G.Hoen Identifying Microbial Interaction Networks Based on Irregularly Spaced Longitudinal 16S rRNA sequence data. bioRxiv 2021.11.26.470159; doi: <https://doi.org/10.1101/2021.11.26.470159>

Friedman J, Tibshirani TH and R. Glasso: Graphical Lasso: Estimation of Gaussian Graphical Models.; 2019. Accessed November 28, 2021. <https://CRAN.R-project.org/package=glasso>

Friedman J, Hastie T, Tibshirani TH, Sparse inverse covariance estimation with the graphical lasso, Biostatistics, Volume 9, Issue 3, July 2008, Pages 432–441, <https://doi.org/10.1093/biostatistics/kxm045>

Examples

```
sample_data[1:5,1:5]
dim(sample_data)
## Heterogeneous model with dampening correlation rate using the first three clusters
a=lglasso(data = sample_data[1:11,], rho = 0.7, heter=TRUE, type=1)
### Estimates of correlation parameters
a$tau
### Sub-network for the first five variables
a$omega[1:5,1:5]
```

```

### Total number of the edges in the estimated network
(length(which(a$omega!=0))-ncol(a$omega))/2
## Homogeneous model with dampening correlation rate using the first three clusters
b=lglasso(data = sample_data[1:11,], rho = 0.7,heter=FALSE,type=1)
### Estimates of correlation parameters
b$tau
### Sub-network for the first five variables
b$omega[1:5,1:5]
### Total number of the edges in the estimated network
(length(which(b$omega!=0))-ncol(b$omega))/2
## Heterogeneous model with uniform correlation rate using the first three clusters
c=lglasso(data = sample_data[1:11,], rho = 0.7,heter=TRUE,type=0)
### Estimates of correlation parameters
c$tau
### Sub-network for the first five variables
c$omega[1:5,1:5]
### Total number of the edges in the estimated network
(length(which(c$omega!=0))-ncol(c$omega))/2
## Homogeneous model with uniform correlation rate using the first three clusters
d=lglasso(data = sample_data[1:11,], rho = 0.7,heter=FALSE,type=0)
### Estimates of correlation parameters
d$tau
### Sub-network for the first five variables
d$omega[1:5,1:5]
### Total number of the edges in the estimated network
(length(which(d$omega!=0))-ncol(d$omega))/2

```

lli_homo

full log likelihood used in EBIC computation

Description

full log likelihood used in EBIC computation

Usage

```
lli_homo(idata, omega, tau, type)
```

Arguments

idata	Data matrix for the subject i in which the first column is id for subject, the second column is the time points of observation. Columns 2 to $(p+2)$ is the observations for p variables.
omega	Precision matrix
tau	Correlation parameter
type	Type of correlation function, which can take either "abs" or "qua".

Value

Value of likelihood function for subject i at given ω and τ

Author(s)

Jie Zhou

ll_homo	<i>Value of likelihood function at given parameter</i>
---------	--

Description

Value of likelihood function at given parameter

Usage

```
ll_homo(data, omega, tau, type)
```

Arguments

data	Data matrix in which the first column is subject id, the second column is the time points of observation. Columns 2 to $(p+2)$ is the observations for p variables.
omega	Precision matrix
tau	Correlation parameter
type	Type of correlation function, which can take either "abs" or "qua".

Value

Value of likelihood function at given ω and τ

Author(s)

Jie Zhou

logdensity	<i>Complete likelihood function used in EM algorithm of heterogeneous marginal graphical lasso model</i>
------------	--

Description

Complete likelihood function used in EM algorithm of heterogeneous marginal graphical lasso model

Usage

```
logdensity(idata, omega, tau, alpha, type)
```

Arguments

idata	Data matrix for the subject i in which the first column is id for subject, the second column is the time points of observation. Columns 2 to $(p+2)$ is the observations for p variables.
omega	Precision matrix
tau	Correlation parameter
alpha	Parameter in exponential distribution
type	Type of correlation function, which can take either "abs" or "qua".

Value

Value of complete likelihood function at given value of omega, tau and alpha

Author(s)

Jie Zhou

mle	<i>Maximum Likelihood Estimate of Precision Matrix and Correlation Parameters for Given Network</i>
-----	---

Description

Maximum Likelihood Estimate of Precision Matrix and Correlation Parameters for Given Network

Usage

```
mle(
  data,
  network,
  heter = TRUE,
  type = 1,
  tole = 0.01,
  lower = 0.01,
  upper = 10
)
```

Arguments

data	Data matrix in which the first column is subject id, the second column is time points of observations for temporal data or site id for spatial data. Columns 3 to (p+2) is the observations for p variables.
network	The network selected by function <code>lglasso</code>
heter	Binary variable TRUE or FALSE, indicating heterogeneous model or homogeneous model is fitted. In heterogeneous model, subjects are allowed to have his/her own temporal correlation parameter τ_i ; while in homogeneous model, all the subjects are assumed to share the same temporal correlation parameter, i.e., $\tau_1 = \tau_2 = \dots = \tau_m$.
type	A positive number which specify the correlation function. The general form of correlation function is given by $\exp(\tau t_i - t_j ^{type})$. in which $type=0$ can be used for spatial correlation while $type>0$ are used for temporal correlation. For latter, the default value is set to be $type=1$.
tole	Threshold for convergence. Default value is $1e-2$. Iterations stop when maximum absolute difference between consecutive estimates of parameter change is less than <code>tole</code> .
lower	Lower bound for predicts of correlation parameter τ . Default value is $1e-2$. The estimate of $\tau(\alpha)$ will be searched in the interval <code>[lower, upper]</code> , where parameter <code>upper</code> is explained in the following.
upper	Upper bound for predicts of correlation parameter τ .

Value

A list which include the maximum likelihood estimate of precision matrix, correlation parameter τ . If `heter=TRUE`, the output also include the estimate of α where $\tau = \exp(\alpha)$

Author(s)

Jie Zhou

mle_alpha	<i>Maximum likelihood estimate of correlation parameter for given structure of precision matrix</i>
-----------	---

Description

Maximum likelihood estimate of correlation parameter for given structure of precision matrix

Usage

```
mle_alpha(data, alpha0, omega, type, tole, lower, upper)
```

Arguments

data	Data matrix in which the first column is subject id, the second column is the time points of observation. Columns 2 to (p+2) is the observations for p variables.
alpha0	Initial value for the parameter in exponential distribution
omega	Fixed value for precision matrix
type	Type of correlation function, which can take either "abs" or "qua".
tole	Error tolerance for determination of convergence of EM algorithm
lower	Lower bound for prediction of correlation parameter tau
upper	Upper bound for prediction of correlation parameter tau

Author(s)

Jie Zhou

mle_net	<i>Title</i>
---------	--------------

Description

Title

Usage

```
mle_net(data, priori)
```

Arguments

data	A Longitudinal data set
priori	Given structure of precision matrix

Value

The maximum likelihood estimation

Author(s)

Jie Zhou

mle_tau	<i>Estiamte of precision matrix and autocorrelaton parameter for homogeneous model</i>
---------	--

Description

Estiamte of precision matrix and autocorrelaton parameter for homogeneous model

Usage

```
mle_tau(data, omega, type, lower, upper)
```

Arguments

data	Data matrix in which the first column is subject id, the second column is the time points of observation. Columns 2 to (p+2) is the observations for p variables.
omega	The maximum likelihood estiamte of precision matrix
type	Type of correlation function, which can take either "abs" or "qua".
lower	Lower bound for prediction of correlation parameter tau
upper	Upper bound for prediction of correlation parameter tau

Value

A list for estimates of precision matrix and correlation parameter for given tuning parameter

Author(s)

Jie Zhou

phifunction	<i>Construct the temporal component fo correlation function</i>
-------------	---

Description

Construct the temporal component fo correlation function

Usage

```
phifunction(t, tau, type = 1)
```

Arguments

t	Time points of observations
tau	correlation parameter
type	The type of correlation function, which typically take either 0,1 or 2.

Value

A square matrix with dimension equal to the length of vector t

Author(s)

Jie Zhou

sample_data	<i>Sample Data</i>
-------------	--------------------

Description

The sample data are subset of a larger longitudinal data set from an ongoing large-scale prospective project. There are 13 cluster are involved in the sample data.

Usage

```
sample_data
```

Format

A 100-by-22 matrix

Column 1 Cluster id;

Column 2 Time points of observations;

Columns 3-22 Observations for 20 microbes.

Index

* datasets

sample_data, 12

heterlongraph, 2

homolongraph, 3

iss, 3

lglasso, 4

ll_homo, 7

lli_homo, 6

logdensity, 8

mle, 8

mle_alpha, 10

mle_net, 10

mle_tau, 11

phifunction, 12

sample_data, 12