

Package ‘conicfit’

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Type Package

Title Algorithms for Fitting Circles, Ellipses and Conics Based on the
Work by Prof. Nikolai Chernov

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Description Geometric circle fitting with Levenberg-Marquardt (a, b, R), Levenberg-Marquardt reduced (a, b), Landau, Spath and Chernov-Lesort. Algebraic circle fitting with Taubin, Kasa, Pratt and Fitzgibbon-Pilu-Fisher. Geometric ellipse fitting with ellipse LMG (geometric parameters) and conic LMA (algebraic parameters). Algebraic ellipse fitting with Fitzgibbon-Pilu-Fisher and Taubin.

License GPL (>= 3)

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AtoG	<i>Conversion of algebraic parameters to geometric parameters</i>
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Description

AtoG converts algebraic parameters (A, B, C, D, E, F) to geometric parameters (Center(1:2), Axes(1:2), Angle).

Usage

AtoG(ParA)

Arguments

ParA vector or array with geometric parameters (A, B, C, D, E, F)

Format

code is: -1 - degenerate cases 0 - imaginary ellipse 4 - imaginary parell lines 1 - ellipse 2 - hyperbola
3 - parabola

Value

list(ParG, exitCode)
list with algebraic parameters (Center(1:2), Axes(1:2), Angle) and exit code

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
AtoG(c(0.0551, -0.0908, 0.1588, 0.0489, -0.9669, 0.1620))
```

calculateCircle	<i>Generate points from a circle</i>
-----------------	--------------------------------------

Description

calculateCircle generates points from a circle with many options, equally spaced, randomly spaced, with noise added to the radius or limited to a segment of angle alpha.

Usage

```
calculateCircle(x, y, r, steps=50, sector=c(0, 360), randomDist=FALSE,
randomFun=runif, noiseFun = NA, ...)
```

Arguments

x	center point x
y	center point y
r	radius
steps	number of points
sector	limited circular sector
randomDist	logical, TRUE = randomly spaced
randomFun	random function for the position of the points in the circle
noiseFun	random function for the noise
...	optional parameters to pass to randomFun

Value

points	array n x 2 of point coordinates.
--------	-----------------------------------

Author(s)

Jose Gama

Examples

```
## Not run:
# 100 points from a circle at c(0,0) with radius=200
a<-calculateCircle(0,0,200,100)
plot(a[,1],a[,2],xlim=c(-250,250),ylim=c(-250,250))
par(new=T)
# 12 points from a circle at c(0,0) with radius=190, points between 0 and 90
#degrees
a<-calculateCircle(0,0,190,12,c(0,90))
plot(a[,1],a[,2],xlim=c(-250,250),ylim=c(-250,250),col='red')
par(new=T)
# 12 points from a circle at c(0,0) with radius=180, points between 0 and 180
#degrees, uniform random distribution
a<-calculateCircle(0,0,180,12,c(0,180),TRUE)
plot(a[,1],a[,2],xlim=c(-250,250),ylim=c(-250,250),col='green')
par(new=T)
# 12 points from a circle at c(0,0) with radius=170, points between 0 and 180
#degrees, normal random distribution
a<-calculateCircle(0,0,170,12,c(0,180),TRUE,rnorm)
plot(a[,1],a[,2],xlim=c(-250,250),ylim=c(-250,250),col='blue')
par(new=T)
# 12 points from a circle at c(0,0) with radius=200, points between 0 and 180
#degrees, positioned by uniform random distribution, noise=normal random
#distribution with sd=10
a<-calculateCircle(0,0,200,12,c(180,360),TRUE,noiseFun=function(x)
(x+rnorm(1,mean=0,sd=10)))
plot(a[,1],a[,2],xlim=c(-250,250),ylim=c(-250,250),col='orange')

## End(Not run)
```

calculateEllipse

Generate points from a ellipse

Description

calculateEllipse generates points from a ellipse with many options, equally spaced, randomly spaced, with noise added to the radius or limited to a segment of angle alpha.

Usage

```
calculateEllipse(x, y, a, b, angle = 0, steps = 50, sector = c(0, 360),
randomDist = FALSE, randomFun = runif, noiseFun = NA, ...)
```

Arguments

x	center point x
y	center point y
a	axis a
b	axis b
angle	tilt angle
steps	number of points
sector	limited circular sector
randomDist	logical, TRUE = randomly spaced
randomFun	random function for the position of the points in the ellipse
noiseFun	random function for the noise
...	optional parameters to pass to randomFun

Value

points	array n x 2 of point coordinates.
--------	-----------------------------------

Author(s)

Jose Gama

Examples

```
## Not run:
# 50 points from an ellipse at c(0,0) with axis (200, 100), angle 45 degrees
a<-calculateEllipse(0,0,200,100,45,50)
plot(a[,1],a[,2],xlim=c(-250,250),ylim=c(-250,250))
par(new=T)
# 10 points from an ellipse at c(0,0) with axis (200, 100), angle 45 degrees,
#points between 0 and 180 # degrees, normal random distribution
b<-calculateEllipse(0,0,200,100,45,10,c(0,90))
plot(b[,1],b[,2],xlim=c(-250,250),ylim=c(-250,250),col='red')
par(new=T)
# 50 points from an ellipse at c(0,0) with axis (200, 100), angle 45 degrees
a<-calculateEllipse(0,0,200,100,45,50, randomDist=TRUE,noiseFun=function(x)
(x+rnorm(1,mean=0,sd=10)))
plot(a[,1],a[,2],xlim=c(-250,250),ylim=c(-250,250),col='cyan')

## End(Not run)
```

CircleFitByKasa *Algebraic circle fit (Kasa method)*

Description

CircleFitByKasa applies the simple algebraic circle fit (Kasa method)

Usage

```
CircleFitByKasa(XY)
```

Arguments

XY array of sample data

Value

vector(a, b, R) vector with the values for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/c1/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/c1/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250));par(new=TRUE)
c3 <- CircleFitByKasa(xy)
xyc3<-calculateCircle(c3[1],c3[2],c3[3])
plot(xyc3[,1],xyc3[,2],xlim=c(-250,250),ylim=c(-250,250),col='green',type='l');par(new=TRUE)
```

CircleFitByLandau	<i>Geometric circle fit (minimizing orthogonal distances) by Landau algorithm</i>
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Description

CircleFitByLandau applies the Geometric circle fit (minimizing orthogonal distances) by Landau algorithm

Usage

```
CircleFitByLandau(XY,ParIni = NA, epsilon = 1e-06, IterMAX = 50)
```

Arguments

XY	array of sample data
ParIni	initial guess (a, b, R)
epsilon	tolerance (small threshold)
IterMAX	maximal number of iterations, with a bad initial guess it may take >100 iterations

Value

vector(a, b, R) vector with the values for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Geometric circle fit (minimizing orthogonal distances) by Landau algorithm M. Landau, "Estimation of a circular arc center and its radius", Computer Vision, Graphics and Image Processing, Vol. 38, pages 317-326, (1987)

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Geometric circle fit (minimizing orthogonal distances) by Landau algorithm M. Landau, "Estimation of a circular arc center and its radius", Computer Vision, Graphics and Image Processing, Vol. 38, pages 317-326, (1987)

Examples

```
xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250));par(new=TRUE)
c6 <- CircleFitByLandau(xy)
xyc6<-calculateCircle(c6[1],c6[2],c6[3])
plot(xyc6[,1],xyc6[,2],xlim=c(-250,250),ylim=c(-250,250),col='purple',type='l');par(new=TRUE)
```

CircleFitByPratt

Algebraic circle fit by Pratt

Description

CircleFitByPratt applies the Algebraic circle fit by Pratt

Usage

```
CircleFitByPratt(XY)
```

Arguments

XY array of sample data

Value

vector(a, b, R) vector with the values for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250));par(new=TRUE)
c2 <- CircleFitByPratt(xy)
xyc2<-calculateCircle(c2[1],c2[2],c2[3])
plot(xyc2[,1],xyc2[,2],xlim=c(-250,250),ylim=c(-250,250),col='blue',type='l');par(new=TRUE)
```

CircleFitBySpath *Geometric circle fit by Spath*

Description

CircleFitBySpath applies the Geometric circle fit by Spath

Usage

```
CircleFitBySpath(XY, ParIni = NA, epsilon = 1e-06, IterMAX = 50)
```

Arguments

XY	array of sample data
ParIni	initial guess (a, b, R)
epsilon	tolerance (small threshold)
IterMAX	maximal number of iterations, with a bad initial guess it may take >100 iterations

Value

vector(a, b, R) vector with the values for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250));par(new=TRUE)
c5 <- CircleFitBySpath(xy)
xyc5<-calculateCircle(c5[1],c5[2],c5[3])
plot(xyc5[,1],xyc5[,2],xlim=c(-250,250),ylim=c(-250,250),col='magenta',type='l');par(new=TRUE)
```

CircleFitByTaubin *Algebraic circle fit (Taubin method)*

Description

CircleFitByTaubin applies the simple algebraic circle fit (Taubin method)

Usage

```
CircleFitByTaubin(XY)
```

Arguments

XY array of sample data

Value

vector(a, b, R) vector with the values for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```

xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250));par(new=TRUE)
c1 <- CircleFitByTaubin(xy)
xyc1<-calculateCircle(c1[1],c1[2],c1[3])
plot(xyc1[,1],xyc1[,2],xlim=c(-250,250),ylim=c(-250,250),col='red',type='l');par(new=TRUE)

```

 EllipseDirectFit

Algebraic ellipse fit method by Fitzgibbon-Pilu-Fisher

Description

EllipseDirectFit applies the algebraic ellipse fit method by Fitzgibbon-Pilu-Fisher

Usage

```
EllipseDirectFit(XY)
```

Arguments

XY array of sample data

Value

vector(A,B,C,D,E,F)

vector of algebraic parameters of the fitting ellipse: $ax^2 + bxy + cy^2 + dx + ey + f = 0$

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

A. W. Fitzgibbon, M. Pilu, R. B. Fisher, 1999 Direct Least Squares Fitting of Ellipses IEEE Trans. PAMI, Vol. 21, pages 476-480

A. W. Fitzgibbon, M. Pilu, R. B. Fisher, "Direct Least Squares Fitting of Ellipses", IEEE Trans. PAMI, Vol. 21, pages 476-480 (1999) Halir R, Flusser J (1998) Proceedings of the 6th International Conference in Central Europe on Computer Graphics and Visualization, Numerically stable direct least squares fitting of ellipses (WSCG, Plzen, Czech Republic), pp 125-132.

References

- Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>
- A. W. Fitzgibbon, M. Pilu, R. B. Fisher, 1999 Direct Least Squares Fitting of Ellipses IEEE Trans. PAMI, Vol. 21, pages 476-480
- A. W. Fitzgibbon, M. Pilu, R. B. Fisher, "Direct Least Squares Fitting of Ellipses", IEEE Trans. PAMI, Vol. 21, pages 476-480 (1999) Halir R, Flusser J (1998) Proceedings of the 6th International Conference in Central Europe on Computer Graphics and Visualization, Numerically stable direct least squares fitting of ellipses (WSCG, Plzen, Czech Republic), pp 125–132.

Examples

```
xy<-calculateEllipse(0,0,200,100,45,50, randomDist=TRUE,noiseFun=function(x)
(x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250),col='magenta');par(new=TRUE)

ellipDirect <- EllipseDirectFit(xy)
ellipDirectG <- AtoG(ellipDirect)$ParG
xyDirect<-calculateEllipse(ellipDirectG[1], ellipDirectG[2], ellipDirectG[3],
ellipDirectG[4], 180/pi*ellipDirectG[5])
plot(xyDirect[,1],xyDirect[,2],xlim=c(-250,250),ylim=c(-250,250),type='l',
col='cyan');par(new=TRUE)
```

EllipseFitByTaubin *Algebraic ellipse fit by Taubin*

Description

EllipseFitByTaubin applies the Algebraic ellipse fit by Taubin

Usage

```
EllipseFitByTaubin(XY)
```

Arguments

XY array of sample data

Value

vector(A,B,C,D,E,F)
vector with the values for the ellipse

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
xy<-calculateEllipse(0,0,200,100,45,50, randomDist=TRUE,noiseFun=function(x)
(x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250),col='magenta');par(new=TRUE)

ellipTaubin <- EllipseFitByTaubin(xy)
ellipTaubinG <- AtoG(ellipTaubin)$ParG
xyTaubin<-calculateEllipse(ellipTaubinG[1], ellipTaubinG[2], ellipTaubinG[3],
ellipTaubinG[4], 180/pi*ellipTaubinG[5])
plot(xyTaubin[,1],xyTaubin[,2],xlim=c(-250,250),ylim=c(-250,250),type='l',
col='red');par(new=TRUE)
```

ellipticity

Formulas for the ellipse

Description

ellipticity ellipticity = flattening factor ellipseEccentricity eccentricity of the ellipse ellipseFocus focus of the ellipse ellipseRa radius at apoapsis (the farthest distance) ellipseRp radius at periapsis (the closest distance) ellipse.l semi-latus rectum l

Usage

```
ellipticity(minorAxis,majorAxis)
```

Arguments

```
minorAxis    minor ellipse axis
majorAxis    major ellipse axis
```

Value

```
scalar result
```

Author(s)

Jose Gama

SourceWikipedia Ellipse http://en.wikipedia.org/wiki/Ellipse#Mathematical_definitions_and_properties**References**Wikipedia Ellipse http://en.wikipedia.org/wiki/Ellipse#Mathematical_definitions_and_properties

`estimateInitialGuessCircle`*Estimate Initial Guess Circle values*

Description`estimateInitialGuessCircle` estimates initial guess values for the center and radius of the circle**Usage**`estimateInitialGuessCircle(XY)`**Arguments**`XY` array of sample data**Value**

vector(a, b, R) vector with the estimates for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Examples

```
xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
estimateInitialGuessCircle(xy)
```

fit.conicLMA

Fitting a conic to a given set of points (Implicit method)

Description

fit.conicLMA fits a conic to a given set of points (Implicit method) using algebraic parameters.
 Conic: $Ax^2 + Bxy + Cy^2 + Dx + Ey + F = 0$

Usage

```
fit.conicLMA(XY, ParAini, LambdaIni, epsilonP = 1e-10, epsilonF = 1e-13,
  IterMAX = 2e+06)
```

Arguments

XY	array of sample data
ParAini	initial parameter vector c(A,B,C,D,E,F)
LambdaIni	initial value of the control parameter Lambda
epsilonP	tolerance (small threshold)
epsilonF	tolerance (small threshold)
IterMAX	maximum number of (main) iterations, usually 10-20 will suffice

Value

```
list(ParA, RSS, iters)
```

list with algebraic parameters (Center(1:2), Axes(1:2), Angle), Residual Sum of Squares and number of iterations

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

N. Chernov and H. Ma, 2011 Least squares fitting of quadratic curves and surfaces In: Computer Vision, Editor S. R. Yoshida, Nova Science Publishers; pp. 285-302.

References

- Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>
- N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.
- N. Chernov and H. Ma, 2011 Least squares fitting of quadratic curves and surfaces In: Computer Vision, Editor S. R. Yoshida, Nova Science Publishers; pp. 285-302.

Examples

```
XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
ParAini <- matrix(c(0.2500,0, 1.0000, 0, 0, -1.0000),ncol=1)
LambdaIni=0.1
fit.conicLMA(XY,ParAini,LambdaIni)
```

fit.ellipseLMG	<i>Fitting an ellipse using Implicit method</i>
----------------	---

Description

fit.ellipseLMG Fits an ellipse to a given set of points (Implicit method) using geometric parameters. Conic:

Usage

```
fit.ellipseLMG(XY,ParGini,LambdaIni = 1, epsilon = 1e-06, IterMAX = 200,
L = 200)
```

Arguments

XY	array of sample data
ParGini	initial parameter vector c(Center(1:2), Axes(1:2), Angle)
LambdaIni	initial value of the control parameter Lambda
epsilon	tolerance (small threshold)
IterMAX	maximum number of (main) iterations, usually 10-20 will suffice
L	boundary for major/minor axis

Value

```
list(ParG,RSS,ifers,TF)
```

list with geometric parameters (A,B,C,D,E,F), Residual Sum of Squares, number of iterations and TF==TRUE if the method diverges

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

N. Chernov and H. Ma, 2011 Least squares fitting of quadratic curves and surfaces In: Computer Vision, Editor S. R. Yoshida, Nova Science Publishers; pp. 285-302.

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

N. Chernov and H. Ma, 2011 Least squares fitting of quadratic curves and surfaces In: Computer Vision, Editor S. R. Yoshida, Nova Science Publishers; pp. 285-302.

Examples

```
XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
ParGini <- matrix(c(0,0,2,1,0),ncol=1)
LambdaIni=0.1
fit.ellipseLMG(XY,ParGini,LambdaIni)
```

fitbookstein

Linear ellipse fit using bookstein constraint

Description

fitbookstein Linear ellipse fit using bookstein constraint

conic2parametric Diagonalise A - find Q, D such at $A = Q' * D * Q$

fitggk Linear least squares with the Euclidean-invariant constraint $\text{Trace}(A) = 1$

Usage

```
fitbookstein(x)
```

Arguments

x array of sample data

Value

```
list(z, a, b, alpha)
list with fitted ellipse parameters
```

Author(s)

Jose Gama

Source

Richard Brown, May 28, 2007 <http://www.mathworks.com/matlabcentral/fileexchange/15125-fitellipse-m/content/demo/html/ellipsedemo.html>

References

Richard Brown, May 28, 2007 <http://www.mathworks.com/matlabcentral/fileexchange/15125-fitellipse-m/content/demo/html/ellipsedemo.html>

W. Gander, G. H. Golub, R. Strebler, 1994 Least-Squares Fitting of Circles and Ellipses BIT Numerical Mathematics, Springer

GtoA

Conversion of geometric parameters to algebraic parameters

Description

GtoA converts geometric parameters (A, B, C, D, E, F) to algebraic parameters (Center(1:2), Axes(1:2), Angle).

Usage

GtoA(ParG)

Arguments

ParG list with geometric parameters (A, B, C, D, E, F)

Value

ParA vector or array with algebraic parameters (Center(1:2), Axes(1:2), Angle)

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
GtoA(c(0,0,20,60,45))
```

JmatrixLMA

Compute the Jacobian matrix using algebraic parameters

Description

JmatrixLMA Computes the Jacobian matrix(Implicit method) using algebraic parameters

Usage

```
JmatrixLMA(XY,Para,XYproj)
```

Arguments

XY	array of sample data
Para	initial parameter vector c(Center(1:2), Axes(1:2), Angle)
XYproj	corresponding n projection points on the conic

Value

list(Res,J) list with the Residual Sum of Squares and the Jacobian matrix

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```

XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
ParA <- matrix(c(0.250000000000000,0,1,0,0,-1),nrow=1)
XYproj=matrix(c(0.394467220216675,0.980356518335872,0.833315950425981,
0.909063326557293,1.40466123643977,0.711850899213363,
1.70601340510202,0.521899957274429,1.89925244997324,0.313384799914835,
1.06482258038841,0.846485805004280,1.95308457257492,
0.215325713960169,1.91319150256275,0.291418202297698),8,2,byrow=TRUE)
JmatrixLMA(XY,ParA,XYproj)

```

JmatrixLMG

Compute the Jacobian matrix using geometric parameters

Description

JmatrixLMG Computes the Jacobian matrix (Implicit method) using geometric parameters

Usage

```
JmatrixLMG(XY,A,XYproj)
```

Arguments

XY	array of sample data
A	initial parameter vector c(Xc,Yc,a,b,alpha)
XYproj	corresponding n projection points on the conic

Value

list(Res,J) list with the Residual Sum of Squares and the Jacobian matrix

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```

XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
A <- matrix(c(0,0,2,1,0),ncol=1)
XYproj=matrix(c(0.394467220216675,0.980356518335872,0.833315950425981,
0.909063326557293,1.40466123643977,0.711850899213363,
1.70601340510202,0.521899957274429,1.89925244997324,0.313384799914835,
1.06482258038841,0.846485805004280,1.95308457257492,
0.215325713960169,1.91319150256275,0.291418202297698),8,2,byrow=TRUE)
JmatrixLMG(XY,A,XYproj)

```

LMcircleFit	<i>Geometric circle fit (minimizing orthogonal distances) based on the Levenberg-Marquardt method</i>
-------------	---

Description

LMcircleFit applies a Geometric circle fit (minimizing orthogonal distances) based on the standard Levenberg-Marquardt scheme

Usage

```
LMcircleFit(XY, ParIni, LambdaIni = 1, epsilon = 1e-06, IterMAX = 50)
```

Arguments

XY	array of sample data
ParIni	initial guess (a, b, R)
LambdaIni	initial value for the correction factor lambda
epsilon	tolerance (small threshold)
IterMAX	maximum number of (main) iterations, usually 10-20 will suffice

Value

vector(a, b, R) vector with the estimates for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250));par(new=TRUE)
c4 <- LMcircleFit(xy)
xyc4<-calculateCircle(c4[1],c4[2],c4[3])
plot(xyc4[,1],xyc4[,2],xlim=c(-250,250),ylim=c(-250,250),col='cyan',type='l')
```

LMreducedCircleFit	<i>Geometric circle fit (minimizing orthogonal distances) based on the Levenberg-Marquardt method</i>
--------------------	---

Description

LMreducedCircleFit applies a Geometric circle fit (minimizing orthogonal distances) based on the standard Levenberg-Marquardt scheme in the "reduced" (a,b) parameter space

Usage

```
LMreducedCircleFit(XY, ParIni, LambdaIni = 1, epsilon = 1e-06,
IterMAX = 50)
```

Arguments

XY	array of sample data
ParIni	initial guess (a, b)
LambdaIni	initial value for the correction factor lambda
epsilon	tolerance (small threshold)
IterMAX	maximum number of (main) iterations, usually 10-20 will suffice

Value

vector(a, b, R) vector with the estimates for the circle: center (a,b) and radius R

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/c1/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/c1/>

Nikolai Chernov, 2010 Circular and linear regression: Fitting circles and lines by least squares Chapman & Hall/CRC, Monographs on Statistics and Applied Probability, Volume 117

Examples

```
xy<-calculateCircle(0,0,200,50,randomDist=TRUE,noiseFun=function(x) (x+rnorm(1,mean=0,sd=50)))
plot(xy[,1],xy[,2],xlim=c(-250,250),ylim=c(-250,250));par(new=TRUE)
c7 <- LMreducedCircleFit(xy)
xyc7<-calculateCircle(c7[1],c7[2],c7[3])
plot(xyc7[,1],xyc7[,2],xlim=c(-250,250),ylim=c(-250,250),col='pink',type='l')
```

Residuals.ellipse *Projecting a given set of points onto an ellipse*

Description

Residuals.ellipse projects a given set of points onto an ellipse and computing the distances from the points to the ellipse

Usage

```
Residuals.ellipse(XY,ParG)
```

Arguments

XY	array of sample data
ParG	vector 5x1 of the ellipse parameters (Center(1:2), Axes(1:2), Angle)

Value

list(Res,J) list with the Residual Sum of Squares and the Jacobian matrix

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

Examples

```
XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
ParG <- matrix(c(0,0,2,1,0),ncol=1)
Residuals.ellipse(XY,ParG)
```

Residuals.hyperbola *Projecting a given set of points onto an hyperbola*

Description

Residuals.hyperbola projects a given set of points onto an hyperbola and computing the distances from the points to the hyperbola

Usage

```
Residuals.hyperbola(XY,ParG)
```

Arguments

XY	array of sample data
ParG	vector 5x1 of the hyperbola parameters (Center(1:2), Axes(1:2), Angle)

Value

```
list(RSS, XYproj)
```

list with the Residual Sum of Squares and the array of coordinates of projections

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

Examples

```
XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
ParG <- matrix(c(0,0,2,1,0),ncol=1)
Residuals.hyperbola(XY,ParG)
```

Residuals.parabola *Projecting a given set of points onto an parabola*

Description

Residuals.parabola projects a given set of points onto an parabola and computing the distances from the points to the parabola

Usage

```
Residuals.parabola(XY,ParG)
```

Arguments

XY	array of sample data
ParG	vector 4x1 of the parabola parameters (Vertex(1:2), p, Angle)

Value

```
list(RSS, XYproj)
```

list with the Residual Sum of Squares and the array of coordinates of projections

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

Examples

```
XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
ParG <- matrix(c(0,0,2,1,0),ncol=1)
Residuals.parabola(XY,ParG)
```

 ResidualsG

Projecting a given set of points onto an ellipse

Description

ResidualsG projects a given set of points onto an ellipse and computing the distances from the points to the ellipse

Usage

```
ResidualsG(XY,ParG)
```

Arguments

XY	array of sample data
ParG	vector 5x1 of the ellipse parameters (Center(1:2), Axes(1:2), Angle)

Value

```
list(RSS, XYproj)
```

list with the Residual Sum of Squares and the array of coordinates of projections

Author(s)

Jose Gama

Source

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

References

Nikolai Chernov, 2014 Fitting ellipses, circles, and lines by least squares <http://people.cas.uab.edu/~mosya/cl/>

N. Chernov, Q. Huang, and H. Ma, 2014 Fitting quadratic curves to data points British Journal of Mathematics & Computer Science, 4, 33-60.

Examples

```
XY <- matrix(c(1,7,2,6,5,8,7,7,9,5,3,7,6,2,8,4),8,2,byrow=TRUE)
ParG <- matrix(c(0,0,2,1,0),ncol=1)
ResidualsG(XY,ParG)
```

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