

# Package ‘OptimModel’

January 20, 2025

**Type** Package

**Version** 2.0-1

**Date** 2024-02-17

**Title** Perform Nonlinear Regression Using 'optim' as the Optimization Engine

**Author** Steven Novick [aut, cre]

**Maintainer** Steven Novick <Steven.Novick@takeda.com>

**Depends** R (>= 3.0.0), stats, utils, methods, Matrix

**Suggests** knitr, testthat, rmarkdown, ggplot2

**Description** A wrapper for 'optim' for nonlinear regression problems; see Nocedal J and Write S (2006, ISBN: 978-0387-30303-1). Performs ordinary least squares (OLS), iterative re-weighted least squares (IRWLS), and maximum likelihood (MLE). Also includes the robust outlier detection (ROUT) algorithm; see Motulsky, H and Brown, R (2006)<[doi:10.1186/1471-2105-7-123](https://doi.org/10.1186/1471-2105-7-123)>.

**License** GPL-2

**VignetteBuilder** knitr

**Encoding** UTF-8

**NeedsCompilation** no

**Repository** CRAN

**Date/Publication** 2024-03-12 09:20:02 UTC

## Contents

beta_model . . . . .	2
exp_2o_decay . . . . .	3
exp_decay . . . . .	5
exp_decay_pl . . . . .	6
f2djac . . . . .	7
getData . . . . .	8
get_se_func . . . . .	9
gompertz_model . . . . .	10

hill5_model . . . . .	11
hill_model . . . . .	12
hill_quad_model . . . . .	13
hill_switchpoint_model . . . . .	15
linear_model . . . . .	17
nlogLik_cauchy . . . . .	18
optim_fit . . . . .	19
optim_weights . . . . .	22
predict.optim_fit . . . . .	24
print.optim_fit . . . . .	25
residuals.optim_fit . . . . .	26
rout_fitter . . . . .	27
rout_outlier_test . . . . .	29
test_fit . . . . .	30

<b>Index</b>	<b>32</b>
--------------	-----------

---

beta_model	<i>Beta hook-effect model, gradient, starting values, and back-calculation functions</i>
------------	--

---

## Description

Five-parameter hook-effect model for dose-response curve fitting

## Usage

```
beta_model(theta, x)
```

## Arguments

theta	Vector of five parameters: $(e_{\min}, e_{\max}, \log(\delta_1), \log(\delta_2), \log(\delta_3))$ . See details.
x	Vector of concentrations for the Beta model.

## Details

The five-parameter Beta model is given by:

$$y = e_{\min} + e_{\max} \times \exp(\log(\beta(\delta_1, \delta_2)) + \delta_1 \times \log(x) + \delta_2 * \log(\text{sc} - x) - (\delta_1 + \delta_2) \times \log(\text{sc}))$$

where

$$\beta(\delta_1, \delta_2) = (\delta_1 + \delta_2)^{(\delta_1 + \delta_2)} / (\delta_1^{\delta_1} \times \delta_2^{\delta_2})$$

and

$$\text{sc} = \max(x) + \delta_3.$$

Note that the Beta model depends on the maximum x value. For a particular data set, this may be set by

```
attr(theta, "maxX") = max(x).
```

### Value

Let  $N = \text{length}(x)$ . Then

- `beta_model(theta, x)` returns a numeric vector of length  $N$ .
- `attr(beta_model, "gradient")(theta, x)` returns an  $N \times 5$  matrix.
- `attr(beta_model, "start")(x, y)` returns a numeric vector of length 5 with starting values for

$$(e_{\min}, e_{\max}, \log(\delta_1), \log(\delta_2), \log(\delta_3)).$$

- `attr(beta_model, "backsolve")(theta, y)` returns a numeric vector of length= $\text{length}(y)$  with the first  $x$  such that `beta_model(theta, x)=y`.

### Author(s)

Steven Novick

### See Also

[optim\\_fit](#), [rout\\_fitter](#)

### Examples

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(emin=0, emax=115, ldelta1=-1.5, ldelta2=9, ldelta3=11.5)
y = beta_model(theta, x) + rnorm( length(x), mean=0, sd=1 )

beta_model(theta, x)
attr(beta_model, "gradient")(theta, x)
attr(beta_model, "start")(x, y)

attr(theta, "maxX") = max(x)
attr(beta_model, "backsolve")(theta, 50)
```

---

exp\_2o\_decay

*Five-parameter second-order exponential decay, gradient, starting values, and back-calculation functions*

---

### Description

Five-parameter second-order exponential decay, gradient, starting values, and back-calculation functions.

**Usage**

```
exp_2o_decay(theta, x)
```

**Arguments**

theta            Vector of five parameters: (A, B, k1, k2, p). See details.  
x                Vector of concentrations.

**Details**

The five-parameter exponential decay model is given by:

$$y = A + B \times P \times \exp(-K1 \times x) + B \times (1 - P) \times \exp(-K2 \times x)$$

The parameter vector is (A, B, k1, k2, p) where  $A = \min y$  (min y value),  $A + B = \max y$  (max y value),  $K1 = \exp(k1)$  which is the shape parameter for first term,  $K2 = \exp(k2)$  which is the shape parameter for second term, and  $P = 1/(1 + \exp(p))$  which is the proportion of signal from the first term.

**Value**

Let  $N = \text{length}(x)$ . Then

- `exp_2o_decay(theta, x)` returns a numeric vector of length  $N$ .
- `attr(exp_2o_decay, "gradient")(theta, x)` returns an  $N \times 5$  matrix.
- `attr(exp_2o_decay, "start")(x, y)` returns a numeric vector of length 5 with starting values for (A, B, k1, k2, p).
- `attr(exp_2o_decay, "backsolve")(theta, y)` returns a numeric vector of length =  $\text{length}(y)$ .

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```
set.seed(123L)
x = 2^(-4:4)
theta = c(25, 75, log(3), log(1.2), 1/(1+exp(.7)))
y = exp_2o_decay(theta, x) + rnorm( length(x), mean=0, sd=1 )
attr(exp_2o_decay, "gradient")(theta, x)
attr(exp_2o_decay, "start")(x, y)
attr(exp_2o_decay, "backsolve")(theta, 38)
```

---

exp_decay	<i>Three-parameter exponential decay, gradient, starting values, and back-calculation functions</i>
-----------	---

---

### Description

Three-parameter exponential decay, gradient, starting values, and back-calculation functions.

### Usage

```
exp_decay(theta, x)
```

### Arguments

theta	Vector of three parameters: (A, B, k). See details.
x	Vector of concentrations.

### Details

The three-parameter exponential decay model is given by:

$$y = A + B \times \exp(-Kx).$$

The parameter vector is (A, B, k) where  $A = \min y$  (minimum y value),  $A+B = \max y$  (maximum y value), and  $K = \exp(k)$  which is the shape parameter.

### Value

Let  $N = \text{length}(x)$ . Then

- `exp_decay(theta, x)` returns a numeric vector of length  $N$ .
- `attr(exp_decay, "gradient")(theta, x)` returns an  $N \times 3$  matrix.
- `attr(exp_decay, "start")(x, y)` returns a numeric vector of length 3 with starting values for (A, B, k).
- `attr(exp_decay, "backsolve")(theta, y)` returns a numeric vector of length=`length(y)`.

### Author(s)

Steven Novick

### See Also

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```

set.seed(123L)
x = 2^(-4:4)
theta = c(25, 75, log(3))
y = exp_decay(theta, x) + rnorm( length(x), mean=0, sd=1 )
attr(exp_decay, "gradient")(theta, x)
attr(exp_decay, "start")(x, y)
attr(exp_decay, "backsolve")(theta, 38)

```

---

exp_decay_pl	<i>Three-parameter exponential decay with initial plateau, gradient, starting values, and back-calculation functions</i>
--------------	--

---

**Description**

Three-parameter exponential decay with initial plateau, gradient, starting values, and back-calculation functions.

**Usage**

```
exp_decay_pl(theta, x)
```

**Arguments**

theta	Vector of four parameters: (x0, yMax, yMin, k). See details.
x	Vector of concentrations.

**Details**

The three-parameter exponential decay with initial plateau model is given by  $y = y_{\text{Max}}$  whenever  $x \leq 0$  otherwise

$$y = y_{\text{Min}} + (y_{\text{Max}} - y_{\text{Min}}) \times \exp(-K(x - X_0)) \text{ if } x > X_0,$$

where  $X_0 = \exp(x_0)$  is an inflection point between plateau and exponential decay curve,  $y_{\text{Min}} = \min y$  (min response),  $y_{\text{Max}} = \max y$  (maximum response), and  $K = \exp(k)$  is the shape parameter.

**Value**

Let  $N = \text{length}(x)$ . Then

- `exp_decay_pl(theta, x)` returns a numeric vector of length  $N$ .
- `attr(exp_decay_pl, "gradient")(theta, x)` returns an  $N \times 4$  matrix.
- `attr(exp_decay_pl, "start")(x, y)` returns a numeric vector of length 4 with starting values for (x0, yMax, yMin, k).
- `attr(exp_decay_pl, "backsolve")(theta, y)` returns a numeric vector of length=`length(y)`.

**Author(s)**

Steven Novick

**See Also**[optim\\_fit](#), [rout\\_fitter](#)**Examples**

```

set.seed(100)
x = 2^(-4:4)
theta = c(0.4, 75, 10, log(3))
y = exp_decay_pl(theta, x) + rnorm( length(x), mean=0, sd=1 )
attr(exp_decay_pl, "gradient")(theta, x)
attr(exp_decay_pl, "start")(x, y)
attr(exp_decay_pl, "backsolve")(theta, 38)

```

f2djac

*Compute derivative with respect to parameters***Description**

Compute derivative with respect to parameters.

**Usage**

```
f2djac(Func, theta, ...)
```

**Arguments**

Func	A function with theta as first argument that returns an n x 1 vector, where n represents the number of observations.
theta	A p x 1 vector of parameters.
...	Other arguments needed for function.

**Value**Returns an n x p matrix of derivatives with respect to theta. Computes  $\frac{\delta Func(\theta, \dots)}{\delta \theta}$ , where  $\theta =$  theta**Author(s)**

Steven Novick

**See Also**[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```
f = function(theta, x){ theta[1] + (theta[2]-theta[1])/(1 + (x/theta[3])^theta[4]) }
theta0 = c(0, 100, .5, 2)
x = 0:10
f2djac(f, theta0, x=x)
```

---

**getData***Extract data object from an optim fit*

---

**Description**

Extract data object from an `optim_fit` object.

**Usage**

```
getData(object)
```

**Arguments**

`object`            object of class `optim_fit`.

**Value**

Returns a data frame with elements `x` and `y`.

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each =4 )
theta = c(0, 100, log(.5), 2)
y = hill_model(theta, x) + rnorm( length(x), sd=2 )
fit = optim_fit(c(0, 100, .5, 1), f.model=hill_model, x=x, y=y)
d=getData(fit)
```



---

get_se_func	<i>Compute standard error for a function of model parameter estimates</i>
-------------	---

---

**Description**

Compute standard error for a function of model parameter estimates via the delta method.

**Usage**

```
get_se_func(object, Func, ..., level=0.95)
```

**Arguments**

object	An <code>optim_fit()</code> object
Func	Function that returns a numeric value. See details.
...	Other arguments needed for Func.
level	Confidence level for confidence interval

**Details**

Func is of the form `function(theta, ...)`. For example,  
`Func = function(theta, x){ exp(theta[1])*log(x)/theta[2] }`

**Value**

Returns a `data.frame` with a single row for the estimated Func call (Est), its standard error (SE), and a confidence interval (lower, upper).

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each =4 )
theta = c(0, 100, log(.5), 2)
y = hill_model(theta, x) + rnorm( length(x), sd=2 )
fit = optim_fit(theta, hill_model, x=x, y=y)

## Get SE for IC20 and IC40
ic.z = function(theta, z){ attr(hill_model, "backsolve")(theta, z) }
get_se_func(object=fit, Func=ic.z, z=20)
get_se_func(object=fit, Func=ic.z, z=40)
```

---

gompertz_model	<i>Four-parameter Gompertz model, gradient, starting values, and back-calculation functions</i>
----------------	---

---

### Description

Four-parameter Gompertz model, gradient, starting values, and back-calculation functions.

### Usage

```
gompertz_model(theta, x)
```

### Arguments

theta	Vector of four parameters: (A, B, m, offset). See details.
x	Vector of concentrations for the Gompertz model.

### Details

The four parameter Gompertz model is given by:

$$y = A + (B - A) \times \exp(-\exp(m(x - \text{offset}))), \text{ where}$$

$A = \min y$  (minimum y value),  $A + (B - A) \exp(-\exp(-m * \text{offset}))$  is the maximum y value, m is the shape parameter, and offset shifts the curve, relative to the concentration x.

### Value

Let  $N = \text{length}(x)$ . Then

- `gompertz_model(theta, x)` returns a numeric vector of length N.
- `gompertz_model(hill_model, "gradient")(theta, x)` returns an N x 4 matrix.
- `attr(gompertz_model, "start")(x, y)` returns a numeric vector of length 4 with starting values for (A, B, m, offset).
- `attr(gompertz_model, "backsolve")(theta, y)` returns a numeric vector of length=length(y).

### Author(s)

Steven Novick

### See Also

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```

set.seed(100)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y = gompertz_model(theta, x) + rnorm( length(x), mean=0, sd=1 )
attr(gompertz_model, "gradient")(theta, x)
attr(gompertz_model, "start")(x, y)
attr(gompertz_model, "backsolve")(theta, 50)

```

---

hill5_model	<i>Five-parameter Hill model, gradient, starting values, and back-calculation functions</i>
-------------	---

---

**Description**

Five-parameter Hill model, gradient, starting values, and back-calculation functions.

**Usage**

```
hill5_model(theta, x)
```

**Arguments**

theta	Vector of five parameters: ( $e_{\min}$ , $e_{\max}$ , $\log.ic50$ , $m$ , $\log.sym$ ). See details.
x	Vector of concentrations for the five-parameter Hill model.

**Details**

The five parameter Hill model is given by:

$$y = e_{\min} + \frac{e_{\max} - e_{\min}}{1 + \exp(m \log(x) - m \log.ic50)^{\exp(\log.sym)}}$$

$e_{\min} = \min y$  (minimum y value),  $e_{\max} = \max y$  (maximum y value),  $\log.ic50 = \log(ic50)$ ,  $m$  is the shape parameter, and  $\log.sym = \log(\text{symmetry parameter})$ .

Note:  $ic50$  is defined such that  $hill5\_model(theta, ic50) = e_{\min} + (e_{\max} - e_{\min})/2^{\exp(\log.sym)}$

**Value**

Let  $N = \text{length}(x)$ . Then

- `hill5_model(theta, x)` returns a numeric vector of length  $N$ .
- `attr(hill5_model, "gradient")(theta, x)` returns an  $N \times 5$  matrix.
- `attr(hill5_model, "start")(x, y)` returns a numeric vector of length 5 with starting values for ( $e_{\min}$ ,  $e_{\max}$ ,  $\log.ic50$ ,  $m$ ,  $\log.sym$ ).
- `attr(hill5_model, "backsolve")(theta, y)` returns a numeric vector of length= $\text{length}(y)$ .

**Author(s)**

Steven Novick

**See Also**[optim\\_fit](#), [rout\\_fitter](#)**Examples**

```

set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2, log(10))
y = hill5_model(theta, x) + rnorm( length(x), mean=0, sd=1 )
attr(hill5_model, "gradient")(theta, x)
attr(hill5_model, "start")(x, y)
attr(hill5_model, "backsolve")(theta, 50)

```

---

hill_model	<i>Four-parameter Hill model, gradient, starting values, and back-calculation functions</i>
------------	---

---

**Description**

Four-parameter Hill model, gradient, starting values, and back-calculation functions.

**Usage**

```
hill_model(theta, x)
```

**Arguments**

**theta** Vector of four parameters:  $(e_{\min}, e_{\max}, \text{lec50}, m)$ . See details.  
**x** Vector of concentrations for the Hill model.

**Details**

The four parameter Hill model is given by:

$$y = e_{\min} + \frac{(e_{\max} - e_{\min})}{(1 + \exp(m \log(x) - m * \text{lec50}))}, \text{ where}$$

$e_{\min} = \min y$  (minimum y value),  $e_{\max} = \max y$  (maximum y value),  $\text{lec50} = \log(\text{ec5})$ , and  $m$  is the shape parameter. Note:  $\text{ec50}$  is defined such that  $\text{hill.model}(\text{theta}, \text{ec50}) = .5 * (e_{\min} + e_{\max})$ .

**Value**

Let  $N = \text{length}(x)$ . Then

- `hill_model(theta, x)` returns a numeric vector of length  $N$ .
- `attr(hill_model, "gradient")(theta, x)` returns an  $N \times 4$  matrix.
- `attr(hill_model, "start")(x, y)` returns a numeric vector of length 4 with starting values for  $(e_{\min}, e_{\max}, \text{lec50}, m)$ .
- `attr(hill_model, "backsolve")(theta, y)` returns a numeric vector of length  $= \text{length}(y)$ .

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y = hill_model(theta, x) + rnorm( length(x), mean=0, sd=1 )
attr(hill_model, "gradient")(theta, x)
attr(hill_model, "start")(x, y)
attr(hill_model, "backsolve")(theta, 50)
```

---

hill_quad_model	<i>Five-parameter Hill model with quadratic component, gradient, starting values, and back-calculation functions</i>
-----------------	--

---

**Description**

Five-parameter Hill model with quadratic component, gradient, starting values, and back-calculation functions.

**Usage**

```
hill_quad_model(theta, x)
```

**Arguments**

theta	Vector of five parameters: (A, B, a, b, c). See details.
x	Vector of concentrations for the five-parameter Hill model with quadratic component.

**Details**

The five parameter Hill model with quadratic component is given by:

$$y = A + \frac{B - A}{(1 + \exp(-(a + bz + cz^2)))}, \text{ where } z = \log(x)$$

$A = \min y$  ( minimum y value),  $B = \max y$  (maximum y value), (a, b, c) are quadratic parameters for  $\log(x)$ .

Notes:

1. If  $c = 0$ , this model is equivalent to the four-parameter Hill model (hill.model).
2. The ic50 is defined such that  $a + bz + cz^2 = 0$ . If the roots of the quadratic equation are real, then the ic50 is given by  $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ .

**Value**

Let  $N = \text{length}(x)$ . Then

- `hill_quad_model(theta, x)` returns a numeric vector of length  $N$ .
- `attr(hill_quad_model, "gradient")(theta, x)` returns an  $N \times 5$  matrix.
- `attr(hill_quad_model, "start")(x, y)` returns a numeric vector of length 5 with starting values for (A, B, a, b, c).

If the quadratic roots are real-valued, `attr(hill_quad_model, "backsolve")(theta, y)` returns a numeric vector of length=2.

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=3 )      ## Dose
theta = c(0, 100, 2, 1, -0.5)        ## Model parameters
y = hill_quad_model(theta, x) + rnorm( length(x), mean=0, sd=5 )

## Generate data
hill_quad_model(theta, x)
attr(hill_quad_model, "gradient")(theta, x)
attr(hill_quad_model, "start")(x, y)
attr(hill_quad_model, "backsolve")(theta, 50)
```

---

 hill\_switchpoint\_model

*Five-parameter Hill model with switch point component, gradient, starting values, and back-calculation functions*

---

## Description

Five-parameter Hill model with switch point component, gradient, starting values, and back-calculation functions.

## Usage

```
hill_switchpoint_model(theta, x)
```

## Arguments

theta	Vector of five parameters: ( $e_{\min}$ , $e_{\max}$ , $\text{lec50}$ , $m$ , $\text{lsp}$ ). See details.
x	Vector of concentrations for the five-parameter Hill model with switch point component.

## Details

The five parameter Hill model with switch point component is given by:

$$y = e_{\min} + \frac{e_{\max} - e_{\min}}{1 + \exp(m \times f(\exp(\text{lsp}), x) \times (\log(x) - \log(\text{ic50})))}, \text{ where}$$

$e_{\min} = \min y$  (minimum y value),  $e_{\max} = \max y$  (maximum y value),  $\log(\text{ic50}) = \log(\text{ic50})$ ,  $m$  is the shape parameter, and  $f(s, x)$  is the switch point function.

The function  $f(s, x) = (s - x)/(s + x) = 2/(1 + x/s) - 1$ . This function is constrained to be between -1 and +1 with  $s > 0$ .

Notes:

1. At  $x = 0$ ,  $f(s, x) = 1$ , which reduces to `hill_model(theta[1:4], 0)`.
2. The `hill_switchpoint_model()` is more flexible compared to `hill_quad_model()`.
3. When the data does not contain a switchpoint, then `lsp` should be a large value so that  $f(\exp(\text{lsp}), x)$  will be near 1 for all  $x$ .

## Value

Let  $N = \text{length}(x)$ . Then

- `hill_switchpoint_model(theta, x)` returns a numeric vector of length  $N$ .
- `attr(hill_switchpoint_model, "gradient")(theta, x)` returns an  $N \times 5$  matrix.
- `attr(hill_switchpoint_model, "start")(x, y)` returns a numeric vector of length 5 with starting values for ( $e_{\min}$ ,  $e_{\max}$ ,  $\text{lec50}$ ,  $m$ ,  $\text{lsp}$ ).

Because `hill_switchpoint_model()` can be fitted to biphasic data with a hook-effect, `attr(hill_switchpoint_model, "backsolve")(theta, y0)` returns the first  $x$  that satisfies  $y_0 = \text{hill\_switchpoint\_model}(theta, x)$

**Author(s)**

Steven Novick

**See Also**[optim\\_fit](#), [rout\\_fitter](#)**Examples**

```

set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=3 )      ## Dose
## Create model with no switchpoint term
theta = c(0, 100, log(.5), 2)
y = hill_model(theta, x) + rnorm( length(x), mean=0, sd=5 )

## fit0 and fit return roughly the same r-squared and sigma values.
## Note that BIC(fit0) < BIC(fit), as it should be.
fit0 = optim_fit(NULL, hill_model, x=x, y=y)
fit = optim_fit(c(coef(fit0), lsp=0), hill_switchpoint_model, x=x, y=y)
fit = optim_fit(NULL, hill_switchpoint_model, x=x, y=y)

## Generate data from hill.quad.model() with a biphasic (hook-effect) profile
set.seed(123L)
theta = c(0, 100, 2, 1, -0.5)          ## Model parameters
y = hill_quad_model(theta, x) + rnorm( length(x), mean=0, sd=5 )

## fit.qm and fit.sp return nearly identical fits
fit.qm = optim_fit(theta, hill_quad_model, x=x, y=y)
fit.sp = optim_fit(NULL, hill_switchpoint_model, x=x, y=y, ntry=50)

plot(log(x+0.01), y)
lines(log(x+0.01), fitted(fit.qm))
lines(log(x+0.01), fitted(fit.sp), col="red")

## Generate data from hill.switchback.model()
set.seed(123)
theta = c(0, 100, log(0.25), -3, -2)
y = hill_switchpoint_model(theta, x) + rnorm( length(x), mean=0, sd=5 )
plot( log(x+0.01), y )

## Note that this model cannot be fitted by hill.quad.model()
fit = optim_fit(NULL, hill_switchpoint_model, x=x, y=y, ntry=50,
                start.method="fixed", until.converge=FALSE)
pred = predict(fit, x=exp(seq(log(0.01), log(16), length=50)), interval='confidence')

plot(log(x+0.01), y, main="Fitted curve with 95% confidence bands")
lines(log(pred[, 'x']+0.01), pred[, 'y.hat'], col='black')
lines(log(pred[, 'x']+0.01), pred[, 'lower'], col='red', lty=2)
lines(log(pred[, 'x']+0.01), pred[, 'upper'], col='red', lty=2)

## Other functions

```



```
hill_switchpoint_model(theta, x)
attr(hill_switchpoint_model, "gradient")(theta, x)
attr(hill_switchpoint_model, "start")(x, y)
attr(hill_switchpoint_model, "backsolve")(theta, 50)
```

---

linear_model	<i>Linear model, gradient, and starting values</i>
--------------	--

---

### Description

Linear model, gradient, and starting values.

### Usage

```
linear_model(theta, x)
```

### Arguments

theta	Vector of model parameters intercept and slope. See details.
x	Matrix, possibly from <code>model.matrix()</code> .

### Details

The linear model is given by:

$$y = x * \theta, \text{ where}$$

x is a matrix, possibly generated from `model.matrix()`  $\theta$  is a vector of linear parameters

### Value

Let  $N = \text{nrow}(x)$ . Then

- `linear_model(theta, x)` returns a numeric vector of length  $N$ .
- `attr(linear_model, "gradient")(theta, x)` returns  $x$ .
- `attr(linear_model, "start")(x, y)` returns `solve(t(x) * x) * t(x) * y`

### Author(s)

Steven Novick

### See Also

[optim\\_fit](#), [rout\\_fitter](#)

**Examples**

```

set.seed(123)
d = data.frame( Group=factor(rep(LETTERS[1:3], each=5)), age=rnorm(15, mean=20, sd=3) )
d$y = c(80, 100, 120)[unclass(d$Group)] - 3*d$age + rnorm(nrow(d), mean=0, sd=5)

X = model.matrix(~Group+age, data=d) ## This is the "x" in linear.model()
theta = c(80, 20, 40, -3) ## Intercept, effect for B, effect for C, slope for age
linear_model(theta, x=X)
attr(linear_model, "gradient")(theta, x=X)
attr(linear_model, "start")(x=X, y=d$y)

```

---

nlogLik\_cauchy

*Negative log-likelihood function for Cauchy regression*


---

**Description**

The negative log-likelihood function for Cauchy regression, for use with `rou_t_fitter`. Usually not called by the end user.

**Usage**

```
nlogLik_cauchy(theta, x, y, f.model, lbs)
```

**Arguments**

theta	Parameters for <code>f.model</code> and an extra parameter for the scale parameter; e.g., <code>f.model=hill.model</code>
x	Explanatory variable(s). Can be vector, matrix, or data.frame
y	Response variable.
f.model	Name of mean model function.
lbs	Logical. <code>lbs = log both sides</code> . See details.

**Details**

The function provides the negative log-likelihood for Cauchy regression

Let  $\mu = f.model(theta[1:(p-1)], x)$  and  $\sigma = \exp(theta[p])$ , where  $p = \text{number of parameters in } theta$ .

The Cauchy likelihood is

$$L = \prod \frac{1}{\pi\sigma} \left(1 + \left(\frac{y_i - \mu_i}{\sigma}\right)^2\right)^{-1}$$

.

The function returns  $\log(L)$ .

If `lbs == TRUE`, then  $\mu$  is replaced with  $\log(\mu)$ .

**Value**

Returns a single numerical value.

**Author(s)**

Steven Novick

**See Also**

[rout\\_fitter](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(emin=0, emax=100, lec50=log(.5), m=2)
y = hill_model(theta, x) + rnorm( length(x), mean=0, sd=2 )

theta1 = c(theta, lsigma=log(2))
nlogLik_cauchy(theta1, x=x, y=y, f.model=hill_model, lbs=FALSE)

## Cauchy regression via maximum likelihood
optim( theta1, nlogLik_cauchy, x=x, y=y, f.model=hill_model, lbs=FALSE )
```

---

optim\_fit

*Fit Model with optim*

---

**Description**

Fit nonlinear model using the `optim` function in the **stats** library. This defaults to Ordinary Least Squares (OLS) The other options are Iterative Reweighted Least Squares (IRWLS), and Maximum Likelihood Estimator (MLE).

**Usage**

```
optim_fit( theta0, f.model, gr.model=NULL, x, y, wts,
           fit.method=c("ols", "irwls", "mle"),
           var.method=c("hessian", "normal", "robust"),
           phi0=NULL, phi.fixed=TRUE, conf.level = 0.95, tol = 1e-3,
           n.start=1000, ntry=1, start.method=c("fixed", "random"),
           until.converge=TRUE, check.pd.tol = 1e-8, ...)

robust_fit(theta0, f.model, gr.model=NULL, x, y, wts=c("huber", "tukey"),
           var.method=c("hessian", "normal", "robust"), conf.level=.95, tol=1e-3, ...)
```

**Arguments**

theta0	starting values. Alternatively, if given as NULL, theta0 can be computed within <code>optim_fit()</code> if a starting values function is supplied as <code>attr(f.model, "start")</code> , as a function of x and y.
f.model	Name of mean model function.
gr.model	If specified, name of the partial derivative of f.model with respect to its parameter argument. If not specified, <code>f2djac</code> will approximate the derivative. Alternatively, the gradient of f.model can be specified as <code>attr(f.model, "gradient")</code>
x	Explanatory variable(s). Can be vector, matrix, or data.frame
y	Response variable.
fit.method	"ols" for ordinary least squares, "irls" for iterative re-weighted least squares, "mle" for maximum likelihood.
wts	For <code>optim_fit()</code> , can be a numeric vector or a function. Functions supplied in the library are <code>weights_varIdent</code> , <code>weights_tukey_bw</code> , <code>weights_huber</code> , <code>weights_varExp</code> , <code>weights_varPower</code> , and <code>weights_varConstPower</code> . For <code>robust_fit()</code> , choices are a character string of "huber" for <code>weights_huber</code> and "tukey" for <code>weights_tukey_bw</code>
var.method	Method to compute variance-covariance matrix of estimated model parameters. Choices are "hessian" to use the hessian inverse, "normal" to use the so-called 'folk-lore' theorem estimator, and "robust" to use a sandwich-variance estimator. When <code>fit.method = "mle"</code> , <code>var.method = "hessian"</code> and cannot be overridden.
phi0	Not meaningful for <code>fit.method = "ols"</code> . Starting value(s) for variance parameters (for weights).
phi.fixed	Not meaningful for <code>fit.method = "ols"</code> . If set to TRUE, the variance parameter(s) remain fixed at the given starting value, phi0. Otherwise, the variance parameter(s) are estimated.
conf.level	Confidence level of estimated parameters.
tol	Tolerance for optim algorithm.
n.start	Number of starting values to generate (see details).
ntry	Maximum number of calls to <code>optim_fit()</code> .
start.method	Parameter
until.converge	Logical (TRUE/FALSE) indicating when algorithm should stop.
check.pd.tol	absolute tolerance for determining whether a matrix is positive definite. Refer to <code>test_fit</code> .
...	Other arguments to passed to <code>optim</code> . See <code>?optim</code> . For example, <code>lower=</code> , <code>upper=</code> , <code>method=</code>

**Details**

`optim_fit()` is a wrapper for `stats::optim()`, specifically for non-linear regression. The Default algorithm is ordinary least squares (ols) using `method="BFGS"` or `"L-BFGS-B"`, if `lower=` and `upper=` are specified. These can easily be overridden.

The assumed model is:

$$y = f.model(\theta, x) + g(\theta, \phi, x)\sigma\epsilon, \text{ where } \epsilon \sim N(0, 1).$$

Usually the function  $g(\cdot) = 1$ .

With the exception of `weights.tukey.bw` and `weights.huber`, the weights functions are equivalent to  $g(\theta, \phi, x)$ .

Note that `robust_fit()` is a convenience function to simplify the model call with `fit.method = "irwls"`, `phi0 = NULL`, and `phi.fixed = TRUE`.

**Algorithms:**

1. OLS. Minimize  $\text{sum}( (y - f.model(\theta, x))^2 )$
2. IRWLS. Minimize  $\text{sum}( g(\theta, \phi, x) * (y - f.model(\theta, x))^2 )$ , where  $g(\theta, \phi, x)$  act as weights. See section on Variance functions below for more details on  $g(\cdot)$ .
3. MLE. Minimize the  $-\log(\text{Likelihood})$ . See section on Variance functions below for more details on  $g(\cdot)$ .

**Variance functions:**

Weights are given by some variance function. Some common variance functions are supplied.

See `weights_varIdent`, `weights_varExp`, `weights_varPower`, `weights_varConstPower`, `weights_tukey_bw`, `weights_huber`.

User-specified variance functions can be provided for weighted regression.

**Value**

The returned object is a list with the following components and attributes:

`coefficients` = estimated model coefficients

`value`, `counts`, `convergence` = returns from `optim()`

`message` = character, indicating problem if any. otherwise=NULL

`hessian` = hessian matrix of the objective function (e.g., sum of squares)

`fit.method` = chosen `fit.method` (e.g., "ols")

`var.method` = chosen `var.method` (e.g., "hessian")

`call` = `optim.fit()` function call

`fitted`, `residuals` = model mean and model residuals

`r.squared`, `bic` = model statistics

`df` = error degrees of freedom =  $N - p$ , where  $N$  = # of observations and  $p$  = # of parameters

`dims` = list containing the values of  $N$  and  $p$

`sigma` = estimated standard deviation parameter

`varBeta` = estimated variance-covariance matrix for the coefficients

`beta` = data.frame summary of the fit

`attr(object, "weights")` = weights

`attr(object, "w.func")` = weights model for the variance

`attr(object, "var.param")` = variance parameter values

`attr(object, "converge.pls")` = logical indicating if IRWLS algorithm converged.

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#), [rout\\_outlier\\_test](#), [beta\\_model](#), [exp\\_2o\\_decay](#), [exp\\_decay\\_pl](#), [gompertz\\_model](#), [hill\\_model](#), [hill5\\_model](#), [hill\\_quad\\_model](#), [hill\\_switchpoint\\_model](#), [linear\\_model](#), [weights\\_huber](#), [weights\\_tukey\\_bw](#), [weights\\_varConstPower](#), [weights\\_varExp](#), [weights\\_varIdent](#), [weights\\_varPower](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y1 = hill_model(theta, x) + rnorm( length(x), sd=2 )
y2 = hill_model(theta, x) + rnorm( length(x), sd=.1*hill_model(theta, x) )
wts = runif( length(y1) )
fit1=optim_fit(theta, hill_model, x=x, y=y1)
fit2=optim_fit(theta, hill_model, x=x, y=y1, wts=weights_varIdent)
fit3=optim_fit(theta, hill_model, x=x, y=y1, wts=wts)
fit4=optim_fit(theta, hill_model, attr(hill_model, "gradient"), x=x, y=y1, wts=wts)

fit5=optim_fit(NULL, hill_model, x=x, y=y2, wts=weights_varPower, fit.method="irwls")
fit6=optim_fit(theta, hill_model, x=x, y=y2, wts=weights_varPower, fit.method="mle")

fit7=optim_fit(theta, hill_model, x=x, y=y2, wts=weights_varPower, fit.method="irwls",
               phi0=0.5, phi.fixed=FALSE)
fit8=optim_fit(theta, hill_model, x=x, y=y2, wts=weights_varPower, fit.method="mle",
               phi0=0.5, phi.fixed=FALSE)

fit9a=optim_fit(theta, hill_model, x=x, y=y1, wts=weights_tukey_bw, fit.method="irwls",
                phi0=4.685, phi.fixed=TRUE)

fit9b=robust_fit(theta, hill_model, x=x, y=y1, wts="tukey")
```

---

 optim\_weights

*Weight functions for optim\_fit*


---

**Description**

Weight functions for `optim_fit`. May be used when `fit.method=="irwls"` or `fit.method=="mle"`. Generally, not called by the user.

**Usage**

```
weights_varIdent(phi, mu)
weights_varExp(phi, mu)
weights_varPower(phi, mu)
```

```
weights_varConstPower(phi, mu)
weights_tukey_bw(phi = 4.685, resid)
weights_huber(phi=1.345, resid)
```

### Arguments

phi	Variance parameter(s)
mu	Vector of means
resid	Vector of model residuals

### Details

- `weights_varIdent` returns a vector of ones.
- `weights_varExp` returns  $\exp(\phi * \mu)$
- `weights_varPower` returns  $|\mu|^\phi$
- `weights_varConstPower` returns  $\phi_1 + |\mu|^{\phi_2}$  where  $\phi_i = \phi[i]$
- `weights_tukey_bw` is a Tukey bi-weight function. Let

$$r = \frac{|\text{resid}|}{\text{mad}(\text{resid}, \text{center}=\text{TRUE})}$$

Then this function returns

$$\left(1 - \left(\frac{r}{\phi}\right)^2\right)^2 \text{ whenever } r \leq \phi \text{ and } 0 \text{ o.w.}$$

For this the user should use `phi.fixed=TRUE` in the `optim_fit` function.

- `weights_huber` is a Huber weighting function that returns  $\min(1, \phi/r)$ , where  $r = |\text{resid}|/\text{sig}$  and  $\text{sig} = \text{mad}(\text{resid}, \text{center} = \text{TRUE})$ . For this the user should use `phi.fixed = TRUE` in the `optim_fit` function.

### Value

A vector of numeric weights.

### Author(s)

Steven Novick

### See Also

[optim\\_fit](#), [rout\\_fitter](#)

---

predict.optim\_fit      *Predicted values for optim\_fit objects*

---

### Description

Provides predicted values, standard errors, confidence intervals and prediction intervals for `optim_fit` objects.

### Usage

```
## S3 method for class 'optim_fit'
predict(object, x, se.fit=FALSE,
        interval=c("none", "confidence", "prediction"), K = 1, level = 0.95,...)
```

### Arguments

<code>object</code>	An object resulting from <code>optim_fit</code> .
<code>x</code>	If supplied, a vector, data.frame, or matrix of Explanatory variables.
<code>se.fit</code>	Logical. Should standard errors be returned? Requires that 'x' is supplied.
<code>interval</code>	If equal to 'confidence', returns a 100*level% confidence interval for the mean response. If equal to 'prediction', returns a 100*level% prediction interval for the mean of the next K observations. Requires that 'x' is supplied.
<code>K</code>	Only used for prediction interval. Number of observations in the mean for the prediction interval.
<code>level</code>	Confidence/prediction interval level.
<code>...</code>	mop up additional arguments.

### Value

Returns a vector (if `interval='none'`). Otherwise returns a data.frame with possible columns 'x', 'y.hat', 'se.fit', 'lower', and 'upper'.

### Author(s)

Steven Novick

### See Also

[optim\\_fit](#)



**Examples**

```
set.seed(123L)

x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y1 = hill_model(theta, x) + rnorm( length(x), sd=2 )

fit1=optim_fit(theta, hill_model, x=x, y=y1)
fitted(fit1)
predict(fit1)
predict(fit1, x=x)
predict(fit1, x=seq(0, 1, by=.1), se.fit=TRUE)
predict(fit1, x=seq(0, 1, by=.1), interval="conf")
predict(fit1, x=seq(0, 1, by=.1), interval="pred")
```

---

print.optim_fit	<i>Prints optim_fit objects</i>
-----------------	---------------------------------

---

**Description**

Provides a nice printed summary of optim\_fit objects.

**Usage**

```
## S3 method for class 'optim_fit'
print(x, digits=4,...)
```

**Arguments**

x	An object resulting from optim_fit().
digits	Number of digits to print for output.
...	other arguments not used by this function.

**Value**

No Return Value.

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#)

## Examples

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y1 = hill_model(theta, x) + rnorm( length(x), sd=2 )

fit1=optim_fit(theta, hill_model, x=x, y=y1)
print(fit1)
fit1
```

---

residuals.optim\_fit    *Residuals for optim\_fit objects*

---

## Description

Provides raw and studentized residuals for `optim_fit` objects.

## Usage

```
## S3 method for class 'optim_fit'
residuals(object, type=c("raw", "studentized"),...)
```

## Arguments

<code>object</code>	An object resulting from <code>optim_fit()</code> .
<code>type</code>	'raw' or 'studentized' residuals.
<code>...</code>	mop up additional arguments.

## Value

Returns a numeric vector.

## Author(s)

Steven Novick

## See Also

[optim\\_fit](#)

**Examples**

```

set.seed(123)

x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y1 = hill_model(theta, x) + rnorm( length(x), sd=2 )

fit1=optim_fit(theta, hill_model, x=x, y=y1)
residuals(fit1)
residuals(fit1, type="s")

```

rout\_fitter

*Fit Model with ROUT***Description**

The `rout_fitter` method in R fits nonlinear regression using the ROUT method as described in the reference below. The starting point is to fit a robust nonlinear regression approach assuming the Lorentzian distribution. An adaptive method then proceeds. The False Discovery Rate is used to detect outliers and the method fits in an iterative fashion.

The `rout_fitter` function provides a wrapper algorithm to the `optim` function in package **stats**.

**Usage**

```

rout_fitter(theta0 = NULL, f.model, x, y, lbs = FALSE, ntry = 0, tol = 1e-3,
            Q = 0.01, check.pd.tol = 1e-8, ...)

```

**Arguments**

<code>theta0</code>	a numeric vector of starting values. Alternatively, if given as <code>NULL</code> , <code>theta0</code> can be computed within <code>[rout.fitter()]</code> if a starting values function is supplied as <code>attr(f.model, "start")</code> , as a function of <code>x</code> and <code>y</code> . If <code>theta0</code> is user supplied, the last entry of <code>theta0</code> should be <code>log(sigma)</code> , where <code>sigma</code> = residual standard deviation. Otherwise, <code>log(sigma)</code> will be estimated and appended to the results from <code>attr(f.model, "start")</code> .
<code>f.model</code>	Name of mean model function. See details below.
<code>x</code>	Explanatory variable(s). Can be a numeric vector, a matrix, or a data.frame.
<code>y</code>	a numeric vector for the response variable.
<code>lbs</code>	Parameter
<code>ntry</code>	Parameter
<code>tol</code>	Tolerance for <code>optim</code> algorithm.
<code>Q</code>	The test size for ROUT testing.
<code>check.pd.tol</code>	absolute tolerance for determining whether a matrix is positive definite. Refer to <code>test_fit</code> .
<code>...</code>	Other arguments to passed to <code>optim</code> . See <code>?optim</code> . For example, <code>lower=</code> , <code>upper=</code> , <code>method=</code>

## Details

[`rout.fitter()`] is a wrapper for [`optim()`], specifically for Cauchy likelihood linear and non-linear regression. The Default algorithm uses `method="BFGS"` or `"L-BFGS-B"`, if `lower=` and `upper=` arguments are specified. These can easily be overridden using the `"..."`.

The assumed model is:

$$y = \text{f.model}(\theta, x) + \sigma * \epsilon, \text{ where } \epsilon \sim \text{Cauchy}(0, 1).$$

After the Cauchy likelihood model is fitted to data, the residuals are interrogated to determine which observations might be outliers. An FDR correction is made to p-values (for outlier testing) through the `p.adjust(method="fdr")` function of the **stats** package.

The package supports several mean model functions for the `f.model` parameter. This includes `beta_model`, `exp_2o_decay`, `exp_decay_pl`, `gompertz_model`, `hill_model`, `hill_quad_model`, `hill_switchpoint_model`, `hill5_model` and `linear_model`.

## Value

An object with class `"rout_fit"` is returned that gives a list with the following components and attributes:

`par` = estimated Cauchy model coefficients. The last term is `log(sigma)`

`value`, `counts`, `convergence` = returns from [`optim()`]

`message` = character, indicating problem if any. otherwise = `NULL`

`hessian` = hessian matrix of the objective function (e.g., sum of squares)

`Converge` = logical value to indicate hessian is positive definite

`call` = [`rout.fitter()`] function call

`residuals` = model residuals

`rsdr` = robust standard deviation from ROUT method

`sresiduals` = `residuals/rsdr`

`outlier` = logical vector. TRUE indicates observation is an outlier via hypothesis testing with unadjusted p-values.

`outlier.adj` = logical vector. TRUE indicates observation is an outlier via hypothesis testing with FDR-adjust p-values.

`at tr(object, "Q")` = test size for outlier detection

## Author(s)

Steven Novick

## References

Motulsky, H.J. and Brown, R.E. (2006) Detecting Outliers When Fitting Data with Nonlinear Regression: A New Method Based on Robust Nonlinear Regression and the False Discovery Rate. *BMC Bioinformatics*, 7, 123.

**See Also**

[optim\\_fit](#), [rout\\_outlier\\_test](#), [beta\\_model](#), [exp\\_2o\\_decay](#), [exp\\_decay\\_pl](#), [gompertz\\_model](#), [hill\\_model](#), [hill5\\_model](#), [hill\\_quad\\_model](#), [hill\\_switchpoint\\_model](#), [linear\\_model](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y = hill_model(theta, x) + rnorm( length(x), sd=2 )

rout_fitter(NULL, hill_model, x=x, y=y)
rout_fitter(c( theta, log(2) ), hill_model, x=x, y=y)

ii = sample( 1:length(y), 2 )
y[ii] = hill_model(theta, x[ii]) + 5.5*2 + rnorm( length(ii), sd=2 )

rout_fitter(c( theta, log(2) ), hill_model, x=x, y=y, Q=0.01)
rout_fitter(c( theta, log(2) ), hill_model, x=x, y=y, Q=0.05)
rout_fitter(c( theta, log(2) ), hill_model, x=x, y=y, Q=0.0001)

## Use optim method="L-BFGS-B"
rout_fitter(NULL, hill_model, x=x, y=y, Q=0.01, lower=c(-2, 95, NA, 0.5), upper=c(5, 110, NA, 4) )
```

---

rout\_outlier\_test      *ROUT Outlier Testing*

---

**Description**

Perform ROUT outlier testing on `rout.fitter` object.

**Usage**

```
rout_outlier_test(fit, Q = 0.01)
```

**Arguments**

`fit`                    A ‘`rout.fitter`’ object from the `rout_fitter` function.

`Q`                        Test size for ROUT outlier detection.

**Details**

`rout_outlier_test()` is typically called from `rout_fitter()`, but may also be called directly by the user.

**Value**

outlier = logical vector. TRUE indicates observation is an outlier via hypothesis testing with unadjusted p-values.

outlier.adj = logical vector. TRUE indicates observation is an outlier via hypothesis testing with FDR-adjusted p-values.

attr(object, "Q") = test size for outlier detection

**Author(s)**

Steven Novick

**See Also**

[rout\\_fitter](#)

**Examples**

```
set.seed(123L)

x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y = hill_model(theta, x) + rnorm( length(x), sd=2 )

ii = sample( 1:length(y), 2 )
y[ii] = hill_model(theta, x[ii]) + 5.5*2 + rnorm( length(ii), sd=2 )

fit = rout_fitter(c( theta, log(2) ), hill_model, x=x, y=y, Q=0.01)
rout_outlier_test(fit, Q=0.001)
```

---

test\_fit

*Test Fit Parameters*

---

**Description**

Test if estimated parameters optimize the regression system (i.e., minimize sums of squares, maximize likelihood).

**Usage**

```
test_fit(obj, check.pd.tol = 1e-8)
```

**Arguments**

obj                    An optim\_fit object

check.pd.tol        absolute tolerance for determining whether a matrix is positive definite.

**Details**

The function checks if `optim` convergence has been reached and also checks if the cholesky decomposition of the Hessian matrix is positive definite. The latter is an indication that optimization has been reached. Sometimes the `chol` decomposition check doesn't work and to enforce that constraint we use the `check.pd.tol` to make sure all the eigenvalues are larger than this minimum threshold.

**Value**

Returns a TRUE or FALSE as to whether or not hessian component of the object is Positive Definite.

**Author(s)**

Steven Novick

**See Also**

[optim\\_fit](#)

**Examples**

```
set.seed(123L)
x = rep( c(0, 2^(-4:4)), each=4 )
theta = c(0, 100, log(.5), 2)
y1 = hill_model(theta, x) + rnorm( length(x), sd=2 )
wts = runif( length(y1) )
fit1=optim_fit(theta, hill_model, x=x, y=y1)
test_fit(fit1)
```

# Index

## \* Derivative

f2djac, 7

## \* Nonlinear

beta\_model, 2

exp\_2o\_decay, 3

exp\_decay, 5

exp\_decay\_pl, 6

gompertz\_model, 10

hill5\_model, 11

hill\_model, 12

hill\_quad\_model, 13

hill\_switchpoint\_model, 15

linear\_model, 17

nlogLik\_cauchy, 18

optim\_fit, 19

optim\_weights, 22

predict.optim\_fit, 24

print.optim\_fit, 25

residuals.optim\_fit, 26

rout\_fitter, 27

rout\_outlier\_test, 29

test\_fit, 30

## \* Standard Error

get\_se\_func, 9

## \* delta method

get\_se\_func, 9

beta\_model, 2, 22, 29

exp\_2o\_decay, 3, 22, 29

exp\_decay, 5

exp\_decay\_pl, 6, 22, 29

f2djac, 7

get\_se\_func, 9

getData, 8

gompertz\_model, 10, 22, 29

hill5\_model, 11, 22, 29

hill\_model, 12, 22, 29

hill\_quad\_model, 13, 22, 29

hill\_switchpoint\_model, 15, 22, 29

linear\_model, 17, 22, 29

nlogLik\_cauchy, 18

optim\_fit, 3–5, 7–10, 12–14, 16, 17, 19,  
22–26, 29, 31

optim\_weights, 22

predict.optim\_fit, 24

print.optim\_fit, 25

residuals.optim\_fit, 26

robust\_fit (optim\_fit), 19

rout\_fitter, 3–5, 7–10, 12–14, 16, 17, 19,  
23, 27, 30

rout\_outlier\_test, 22, 29, 29

test\_fit, 30

weights\_huber, 22

weights\_huber (optim\_weights), 22

weights\_tukey\_bw, 22

weights\_tukey\_bw (optim\_weights), 22

weights\_varConstPower, 22

weights\_varConstPower (optim\_weights),  
22

weights\_varExp, 22

weights\_varExp (optim\_weights), 22

weights\_varIdent, 22

weights\_varIdent (optim\_weights), 22

weights\_varPower, 22

weights\_varPower (optim\_weights), 22