

Package ‘pedmut’

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Title Mutation Models for Pedigree Likelihood Computations

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Description A collection of functions for modelling mutations in pedigrees with marker data, as used e.g. in likelihood computations with microsatellite data. Implemented models include equal, proportional and stepwise models, as well as random models for experimental work, and custom models allowing the user to apply any valid mutation matrix. Allele lumping is done following the lumpability criteria of Kemeny and Snell (1976), ISBN:0387901922.

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URL <https://github.com/magnusdv/pedmut>

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findStationary	<i>Find the stationary frequency distribution</i>
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Description

Finds the stationary distribution of allele frequencies, if it exists, w.r.t. a given mutation matrix.

Usage

```
findStationary(mutmat)
```

Arguments

mutmat A mutation matrix.

Value

A vector of length `ncol(mutmat)`, or `NULL`.

Examples

```
m1 = mutationMatrix("equal", alleles = 1:4, rate = 0.1)
findStationary(m1)

m2 = mutationMatrix("random", alleles = 1:3, seed = 123)
a = findStationary(m2)

a %*% m2 - a # check
```

getParams	<i>Get model parameters</i>
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Description

Extract model parameters of a mutation matrix/model.

Usage

```
getParams(mut, params = NULL, format = 1, sep = "/")
```

Arguments

mut	A <code>mutationModel()</code> or <code>mutationMatrix()</code> .
params	A vector contain some or all of the words "model", "rate", "range", "rate2", "seed". If NULL (default), all present parameters are included.
format	A numeric code indicating the wanted output format. See Value.
sep	A separator character used to paste male and female values. Ignored unless format = 3.

Value

When mut is a `mutationModel` with different male/female parameters, the output format is dictated by the format option, with the following possibilities:

1. A data frame with 2 rows labelled 'female' and 'male'.
2. A data frame with 1 row and female/male columns suffixed by .F/.M respectively.
3. A data frame with 1 row, in which female/male values are pasted together (separated with sep) if different.

If mut is a `mutationMatrix` the output always has 1 row.

Examples

```
M = mutationModel("equal", 1:2, rate = list(female = 0.2, male = 0.1))
getParams(M)
getParams(M, format = 2)
getParams(M, format = 3)
getParams(M, format = 3, sep = "|")
```

isMutationModel *Test for mutation matrix/model*

Description

Test for mutation matrix/model

Usage

```
isMutationModel(x)
isMutationMatrix(x)
```

Arguments

x Any object.

Value

TRUE or FALSE

Examples

```
mat = mutationMatrix("equal", alleles = 1:2, rate = 0.1)
isMutationMatrix(mat)

isMutationModel(mat) # FALSE (not a complete model)

mod = mutationModel(mat)
isMutationModel(mod)
```

lumpedMatrix *Combine alleles in a mutation matrix*

Description

Reduce a mutation matrix by combining a set of alleles into one "lump", if this can be done without distorting the mutation process of the remaining alleles. Such "allele lumping" can give dramatic efficiency improvements in likelihood computations with multi-allelic markers, in cases where only some of the alleles are observed in the pedigree.

Usage

```
lumpedMatrix(mutmat, lump, afreq = NULL, check = TRUE, labelSep = NULL)
lumpedModel(mutmod, lump, afreq = NULL, check = TRUE)
```

Arguments

mutmat	A mutationMatrix object, typically made with <code>mutationMatrix()</code> .
lump	A nonempty subset of the alleles (i.e., the column names of mutmat), or a list of several such subsets.
afreq	A vector with frequency vector, of the same length as the size of mutmat. If not given, the afreq attribute of the matrix is used.
check	A logical indicating if lumpability should be checked before lumping. Default: TRUE.
labelSep	((For debugging) A character used to name lumps by pasting allele labels.
mutmod	A mutationModel object, typically made with <code>mutationModel()</code> .

Value

A reduced mutation model. If the original matrix has dimensions $n \times n$, the result will be $k \times k$, where $k = n - \text{length}(\text{lump}) + 1$.

See Also

`mutationModel()`, `mutationMatrix()`

Examples

```
### Example 1: Lumping a mutation matrix
mat = mutationMatrix("eq", alleles = 1:5,
                    afreq = rep(0.2, 5), rate = 0.1)
mat

# Lump alleles 3, 4 and 5
mat2 = lumpedMatrix(mat, lump = 3:5)
mat2

# Example 2: Full model, proportional
mutrate = list(male = 0.1, female = 0.2)
mod = mutationModel("prop", alleles = 1:4,
                    rate = mutrate, afreq = c(.1,.2,.3,.4))
mod

# Lump alleles 3 and 4
mod2 = lumpedModel(mod, lump = 3:4)
mod2
```

maxRate	<i>Upper limits for overall mutation rate for the stepwise reversible model.</i>
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Description

Upper limits for overall mutation rate for the stepwise reversible model.

Usage

```
maxRate(alleles, afreq, range)
```

Arguments

alleles	A character vector with allele labels.
afreq	A numeric vector of allele frequencies.
range	A positive number.

Value

A vector of two numbers named UW and UB. The first of these is the maximum overall mutation rate for a well-defined stepwise reversible mutation matrix with the given input. The latter (UB) is the upper limit of the overall mutation rate under the additional restraint that the model is bounded by afreq.

Author(s)

Thore Egeland.

model_properties	<i>Mutation model properties</i>
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Description

Functions for checking various properties of a mutation model, including stationarity, reversibility and lumpability.

Usage

```
isStationary(mutmat, afreq = NULL)
```

```
isReversible(mutmat, afreq = NULL)
```

```
isBounded(mutmat, afreq = NULL)
```

```
isLumpable(mutmat, lump)
```

```
alwaysLumpable(mutmat)
```

Arguments

mutmat	A <code>mutationMatrix()</code> or a <code>mutationModel()</code> .
afreq	A vector with allele frequencies, of the same length as the size of mutmat.
lump	A nonempty subset of the colnames of mutmat (i.e. the allele labels).

Details

The function `isBounded()` checks that a mutation model is *bounded* by the allele frequencies, i.e., that `mutmat[i, j] <= afreq[j]` whenever `i` is not equal to `j`.

For each of these functions, if `mutmat` is a `mutationModel` object, i.e., with male and female components, the output is TRUE if and only if both components satisfy the property in question.

Value

Each of these functions returns TRUE or FALSE.

Examples

```
# "proportional" models are stationary and reversible
afr = c(0.2, 0.3, 0.5)
m_prop = mutationMatrix(model = "prop", alleles = 1:3, afreq = afr, rate = 0.1)
stopifnot(isStationary(m_prop, afr), isReversible(m_prop, afr))

# "equal" model is stationary and reversible only when freqs are equal
m_eq = mutationMatrix(model = "eq", alleles = 1:3, rate = 0.1)
stopifnot(isStationary(m_eq, rep(1/3, 3)), isReversible(m_eq, rep(1/3, 3)))
stopifnot(!isStationary(m_eq, afr), !isReversible(m_eq, afr))

# "equal" and "proportional" models allow allele lumping
stopifnot(isLumpable(m_eq, lump = 1:2))
stopifnot(isLumpable(m_prop, lump = 1:2))

# In fact lumpable for any allele subset
stopifnot(alwaysLumpable(m_eq), alwaysLumpable(m_prop))
```

mutationMatrix

Mutation matrix

Description

Construct mutation matrices for pedigree likelihood computations.

Usage

```

mutationMatrix(
  model = c("custom", "equal", "proportional", "random", "onestep", "stepwise",
    "trivial"),
  matrix = NULL,
  alleles = NULL,
  afreq = NULL,
  rate = NULL,
  seed = NULL,
  rate2 = NULL,
  range = NULL
)

validateMutationMatrix(mutmat, alleles = NULL)

```

Arguments

model	A string: either "custom", "equal", "proportional", "random", "stepwise" or "onestep".
matrix	When model is "custom", this must be a square matrix with nonnegative real entries and row sums equal to 1.
alleles	A character vector (or coercible to character) with allele labels. Required in all models, except "custom" if matrix has dimnames.
afreq	A numeric vector of allele frequencies. Required in model "proportional".
rate	A number between 0 and 1. Required in models "equal", "proportional", "stepwise" and "onestep".
seed	A single number. Optional parameter in the "random" model, passed on to <code>set.seed()</code> .
rate2	A number between 0 and 1. The mutation rate between integer alleles and microvariants. Required in the "stepwise" model.
range	A positive number. The relative probability of mutating n+1 steps versus mutating n steps. Required in the "stepwise" model.
mutmat	An object of class <code>mutationMatrix</code> .

Details

Descriptions of the models:

- `custom` : Allows any mutation matrix to be provided by the user, in the `matrix` parameter.
- `equal` : All mutations equally likely; probability $1 - rate$ of no mutation.
- `proportional` : Mutation probabilities are proportional to the target allele frequencies.
- `random` : This produces a matrix of random numbers, where each row is normalised so that it sums to 1.

- **onestep**: A mutation model for microsatellite markers, allowing mutations only to the nearest neighbours in the allelic ladder. For example, '10' may mutate to either '9' or '11', unless '10' is the lowest allele, in which case '11' is the only option. This model is not applicable to loci with non-integral microvariants.
- **stepwise**: A common model in forensic genetics, allowing different mutation rates between integer alleles (like '16') and non-integer "microvariants" like '9.3'). Mutations also depend on the size of the mutation if the parameter 'range' differs from 1.
- **trivial**: The identity matrix; i.e. no mutations are possible.

Value

A square matrix with entries in $[0, 1]$, with the allele labels as both colnames and rownames.

Examples

```
mutationMatrix(alleles = 1:3, model = "equal", rate = 0.05)
```

mutationModel

Mutation models

Description

Constructor for the class mutationModel. An object of this class is essentially a list of two mutation matrices, named "female" and "male".

Usage

```
mutationModel(
  model,
  alleles = NULL,
  afreq = NULL,
  matrix = NULL,
  rate = NULL,
  rate2 = NULL,
  range = NULL,
  seed = NULL,
  validate = TRUE
)
```

```
validateMutationModel(mutmod, alleles = NULL)
```

```
sexEqual(mutmod)
```

Arguments

model	Either: <ul style="list-style-type: none"> • a mutationModel object (returned unchanged after validation) • a single mutationMatrix object (will be applied to both genders) • a list of two mutationMatrix objects, named "female" and "male" • a single model name (see <code>mutationMatrix()</code> for valid options) • a list of two model names, named "female" and "male"
alleles	A character vector with allele labels; passed on to <code>mutationMatrix()</code> .
afreq	A numeric vector of allele frequencies; passed on to <code>mutationMatrix()</code> .
matrix	A matrix, or a list of two (named "female" and "male")
rate	A numeric mutation rate, or a list of two (named "female" and "male")
rate2	A numeric mutation rate, or a list of two (named "female" and "male"). Required in the "stepwise" model; see <code>mutationMatrix()</code> for details.
range	A positive number, or a list of two (named "female" and "male"). Required in the "stepwise" model; see <code>mutationMatrix()</code> for details.
seed	An integer, or a list of two (named "female" and "male").
validate	A logical, by default TRUE.
mutmod	A mutationModel object.

Value

An object of class `mutationModel`. This is a list of two `mutationMatrix` objects, named "female" and "male", and the following attributes:

- `sexEqual` : TRUE if both genders have identical models, otherwise FALSE
- `alwaysLumpable` : TRUE if both genders have models that are lumpable for any allele subset, otherwise FALSE

Examples

```
# "Equal" model, same parameters for both genders
M1 = mutationModel("eq", alleles = 1:2, rate = 0.1)
M1

# Different mutation rates
M2 = mutationModel("eq", alleles = 1:2, rate = list(male = 0.1, female = 0.01))
M2

stopifnot(identical(M1$male, M1$female), identical(M2$male, M1$male))

# A custom mutation matrix:
mat = matrix(c(0,0,1,1), ncol = 2, dimnames = list(1:2, 1:2))
M3 = mutationModel(model = "custom", matrix = mat)

# Under the hood arguments are passed to `mutationMatrix()`.
# Alternatively, this can be done explicitly in the `model` argument
```

```
M4 = mutationModel(model = mutationMatrix("custom", matrix = mat))
stopifnot(identical(M3, M4))

# The latter strategy is needed e.g. in pedtools::marker(), which gives the
# user access to `model`, but not `matrix`.
```

mutRate	<i>Overall mutation rate</i>
---------	------------------------------

Description

Calculate the overall mutation rate at a locus, given a mutation model and a set of allele frequencies.

Usage

```
mutRate(mut, afreq = NULL)
```

Arguments

mut	A mutationModel() or mutationMatrix() .
afreq	A vector of allele frequencies.

Details

The mutation rate is found by the formula $1 - \text{sum}(\text{diag}(\text{mut}) * \text{afreq})$.

If mut is a [mutationModel\(\)](#), the rate is calculated separately for the male and female matrices.

Value

A single number, or (if mut is a [mutationModel\(\)](#) and the female and male rates differ) a list of two numbers, named "female" and "male".

Examples

```
m = mutationMatrix("stepwise", alleles = 1:4, afreq = c(.1,.2,.3,.4),
  rate = 0.01, rate2 = 1e-6, range = 0.1)
r = mutRate(m)

stopifnot(all.equal(r, 0.01))
```

 stabilize

Stabilization of mutation matrix

Description

Produces a mutation matrix close to the input `mutmat`, for which the given frequency vector is the stationary distribution. Several methods for doing this are described by Simonsson and Mostad (2016); only the "PM" method is included here.

Usage

```
stabilize(mutmat, afreq = NULL, method = "PM", details = FALSE)
```

Arguments

<code>mutmat</code>	A mutation matrix.
<code>afreq</code>	A vector of allele frequencies
<code>method</code>	Either "DP", "RM" or "PM". Currently only "PM" is implemented.
<code>details</code>	A logical. If TRUE, the complete Familias output is included.

Details

This function is based on, and reuses code from, the `stabilize()` method of the Familias R package.

Value

An object of the same class the input `mutmat`; either a matrix, a `mutationMatrix` or a `mutationModel`.

Author(s)

Petter Mostad, Thore Egeland, Ivar Simonsson, Magnus D. Vigeland

References

Simonsson, Mostad: Stationary Mutation models. (FSI: Genetics, 2016).

Examples

```
afreq = c(.2, .3, .5)
m = mutationMatrix("stepwise", alleles = 1:3, afreq = afreq,
                  rate = 0.1, rate2 = 0.01, range = 0.1)
m
stabilize(m, afreq = c(.3,.3,.4))

### Example with full model (i.e., male and female)
```

```
M = mutationModel("stepwise", alleles = 1:3, afreq = afreq,
                  rate = list(male = 0.1, female = 0.2),
                  rate2 = 0.01, range = 0.1)

M
stabilize(M)
```

stepwiseReversible *Reversible stepwise mutation model*

Description

A reversible stepwise mutation model is created following the approach of Dawid et al. (2002).

Usage

```
stepwiseReversible(alleles, afreq, rate, range, maxRateOnly = FALSE)
```

Arguments

alleles	A vector of integer integers.
afreq	A numeric vector of allele frequencies.
rate	A numeric mutation rate.
range	A positive number.
maxRateOnly	A logical, by default FALSE. See Value.

Details

For the stepwise reversible model, the mutation rate $r_{i,j}$, $i \neq j$ is proportional to the overall mutation rate λ for given values of the range, the allele frequency p_i and n , the number of alleles. Hence, one can determine bounds UW and UB so that the model is well defined if $\lambda \leq UW$ and bounded, i.e., $r_{i,j} \leq p_j$, $i \neq j$, if $\lambda \leq UB$. The bounds UW and UB are computed.

Value

A reversible stepwise mutation model with overall mutation rate equal to rate.

If `maxRateOnly` is TRUE, the function returns a vector of two numbers named `UW` and `UB`. The first of these is the maximum overall mutation rate for a well-defined stepwise reversible mutation matrix with the given input. The latter (`UB`) is the maximum rate under the additional restraint that the model is bounded by `afreq`.

Author(s)

Thore Egeland.

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