# Package 'NBDesign'

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Version 2.0.0
Date 2020-09-09
<b>Title</b> Design and Monitoring of Clinical Trials with Negative Binomial Endpoint
Description Calculate various functions needed for design and monitoring clinical trials with negative binomial endpoint with variable follow- up. This version has a few changes compared to the previous version 1.0.0, including (1) correct a typo in Type 1 censoring, mtbnull=bnull and (2) restructure the code to account for shape parameter equal to zero, i.e. Poisson scenario.
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NBDesign-package

 ${\tt NBDesign-package} \qquad \qquad \textit{Design and Monitoring of Clinical Trials with Negative Binomial End-}$ 

point

# Description

Calculate various functions needed for design and monitoring clinical trials with negative binomial endpoint with variable follow-up. This version has a few changes compared to the previous version 1.0.0, including (1) correct a typo in Type 1 censoring, mtbnull=bnull and (2) restructure the code to account for shape parameter equal to zero, i.e. Poisson scenario.

#### **Details**

#### The DESCRIPTION file:

Package: NBDesign
Type: Package
Version: 2.0.0
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LazyData: true
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ynegbinompowersim Two-sample sample size calculation for negative

binomial distribution with variable follow-up

ynegbinomsize Two-sample sample size calculation for negative

binomial distribution with variable follow-up

Author(s)

NA

Maintainer: NA

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negint2 A utility functon to calculate the mean exposure under different sce- narios	
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## **Description**

This will calculate the mean exposure under different scenarios: 2: fixed follow-up with drop-out, 3: variable follow-up with a maximum (maxfu), 4: variable follow-up with a maximum and drop-out

#### Usage

```
negint2(ux=0.5,fixedfu=1,type=2,u=c(0.5,0.5,1),ut=c(0.5,1.0,1.5),
    tfix=ut[length(ut)]+0.5,maxfu=10.0,tchange=c(0,0.5,1),
    ratec=c(0.15,0.15,0.15),eps=1.0e-03)
```

## **Arguments**

ux	the parameter a in $(a*t)/(1+a*t)$
fixedfu	the minimum follow-up time
type	follow-up type, type=2: fixed fu with fu time fixedfu but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring
u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the drop-out rate changes. The first element of tchange must be zero. The above rates and tchange must have the same length.
ratec	piecewise constant drop-out rate
eps	error tolerance for the numerical intergration

# **Details**

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time taumin and the maximum follow-up time taumax. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 2 follow-up  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max}, C)$ . Let f be the density of  $T_f$ . We calculate

$$\int_0^\infty t f(t) dt$$

$$\int_0^\infty \frac{at}{1+at} f(t) dt$$

where a is the ux.

and

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#### Value

```
mt mean of (a^*t)/(1+a^*t)

tt mean of t

vt variance of t
```

#### Author(s)

Xiaodong Luo

## **Examples**

```
##calculating the exposure for type 4 follow-up
exp4=negint2(ux=0.5,fixedfu=1,type=2,u=c(0.5,0.5,1),ut=c(0.5,1.0,1.5),
    tfix=2.0,maxfu=1.0,tchange=c(0,0.5,1),
    ratec=c(0.15,0.15,0.15),eps=1.0e-03)
#mean exposure
meanexp=exp4$tt
#var exposure
varexp=exp4$vt
c(meanexp,sqrt(varexp))
#mean of (ux*t)/(1+ux*t)
meanuxt=exp4$mt
```

ynegbinompower

Two-sample sample size calculation for negative binomial distribution with variable follow-up

## **Description**

This will calculate the power for the negative binomial distribution for the 2-sample case under different follow-up scenarios: 1: fixed follow-up, 2: fixed follow-up with drop-out, 3: variable follow-up with a minimum fu and a maximum fu, 4: variable follow-up with a minimum fu and a maximum fu and drop-out.

#### Usage

```
ynegbinompower(nsize=200,r0=1.0,r1=0.5,shape0=1,shape1=shape0,pi1=0.5,
    alpha=0.05,twosided=1,fixedfu=1,type=1,u=c(0.5,0.5,1),ut=c(0.5,1.0,1.5),
    tfix=ut[length(ut)]+0.5,maxfu=10.0,tchange=c(0,0.5,1),
    ratec1=c(0.15,0.15,0.15),ratec0=ratec1,eps=1.0e-03)
```

#### **Arguments**

nsize total number of subjects in two groups

r0 event rate for the controlr1 event rate for the treatment

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dispersion parameter for the control

shape0	dispersion parameter for the control
shape1	dispersion parameter for the treatment
pi1	allocation prob for the treatment
alpha	type-1 error
twosided	1: two-side, others: one-sided
fixedfu	fixed follow-up time for each patient
type	follow-up time type, type=1: fixed fu with fu time fixedfu; type=2: same as 1 but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring
u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the drop-out rate changes. The first element of tchange must be zero. The above rates and tchange must have the same length.
ratec1	piecewise constant drop-out rate for the treatment
ratec0	piecewise constant drop-out rate for the control

#### **Details**

eps

change

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time fixedfu and the maximum follow-up time maxfu. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 1 follow-up,  $T_f = \tau_{min}$ . For type 2 follow-up,  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max}, C)$ . Let f be the density of f. Suppose that f is the number of event observed in follow-up time f for patient f with treatment assignment f in f is the number of event observed in follow-up time f for patient f in the treatment assignment f is the number of event observed in follow-up time f for patient f in the treatment assignment f in f follows a negative binomial distribution such that

error tolerance for the numerical intergration

$$P(Y_i = y \mid Z_i = j) = \frac{\Gamma(y + 1/k_j)}{\Gamma(y + 1)\Gamma(1/k_j)} \left(\frac{k_j u_i}{1 + k_j u_i}\right)^y \left(\frac{1}{1 + k_j u_i}\right)^{1/k_j},$$

where

$$\log(u_i) = \log(t_i) + \beta_0 + \beta_1 Z_i.$$

Let  $\hat{\beta}_0$  and  $\hat{\beta}_1$  be the MLE of  $\beta_0$  and  $\beta_1$ . The varaince of  $\hat{\beta}_1$  is

$$var(\hat{\beta}_1) = 1/\tilde{a}_0(r_0) + 1/\tilde{a}_1(r_1)$$

where

$$\tilde{a}_j(r) = \sum_{i=1}^n I(Z_i = j) k_j r t_i / (1 + k_j r t_i), \quad j = 0, 1,$$

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and  $k_j$ , j = 0, 1 are the dispersion parameters for control j = 0 and treatment j = 1. Note that Zhu and Lakkis (2014) use

$$a_j(r) = \sum_{i=1}^n I(Z_i = j)k_j r E(t_i) / \{1 + k_j r E(t_i)\},$$

to replace  $\tilde{a}_j(r)$ , j=0,1. Using Jensen's inequality, we can show  $a_j(r) \geq \tilde{a}_j(r)$ , which means Zhu and Lakkis's method will underestimate variance of  $\hat{\beta}_1$ , which leads to either smaller than required sample size or inflated power. For comparison, I provide sample sizes under both  $\tilde{a}_j(r)$  and  $a_j(r)$ .

Zhu and Lakkis (2014) discuss three types of the variance under the null. The first way is to set  $\tilde{r}_0 = \tilde{r}_1 = r_0$ , using event rate from the control group. The second way is to set  $\tilde{r}_0 = r_0$ ,  $\tilde{r}_1 = r_1$ , using true event rates. The third way is to set  $\tilde{r}_0 = \tilde{r}_1 = \tilde{r}$ , where  $\tilde{r} = \pi_1 r_1 + \pi_0 r_0$ , using maximum likelihood estimation.

Therefore, for each type of follow-up, there are 3 sample sizes calculated (because there are 3 varainces under the null) for with and without approximation of Zhu and Lakkis (2014).

Note that PASS14.0 provides 3 ways of null varaince with the default being the MLE. PASS does not allow different dispersion parameters between treatment and control. EAST only provides the second way of null varaince but allows for different dispersion parameters. Both of these softwares base on the approximatin method of Zhu and Lakkis (2014), which underestimate the required sample sizes.

#### Value

tildeXPWR powers (in percentage) not based on current approach, i.e. not based on the Zhu

and Lakkis's approximation

XPWR powers (in percentage) based on on the Zhu and Lakkis's approximation

tildemineffsize

minimum detectable effect sizes not based on approximation

mineffsize minimum detectable effect sizes based on approximation

Exposure mean exposure under different follow-up types with element 1 for control, ele-

ment 2 for treatment and element 3 for overall.

SDExp Sd of the exposure under different follow-up types with element 1 for control,

element 2 for treatment and column 3 for overall.

#### Author(s)

Xiaodong Luo

#### References

Zhu~H and Lakkis~H. Sample size calculation for comparing two negative binomial rates. Statistics in Medicine 2014, 33: 376-387.

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#### **Examples**

```
##calculating the sample sizes
abc=ynegbinompower(nsize=200,r0=1.0,r1=0.5,shape0=1,
        pi1=0.5,alpha=0.05,twosided=1,fixedfu=1,
        type=4, u=c(0.5,0.5,1), ut=c(0.5,1.0,1.5),
        tchange=c(0,0.5,1),
        ratec1=c(0.15, 0.15, 0.15), eps=1.0e-03)
###Zhu and Lakkis's powers (i.e. with approximation)
abc$XPWR
###Our powers (i.e. without approximation)
abc$tildeXPWR
```

ynegbinompowersim

Two-sample sample size calculation for negative binomial distribution with variable follow-up

## **Description**

This will calculate the power for the negative binomial distribution for the 2-sample case under different follow-up scenarios: 1: fixed follow-up, 2: fixed follow-up with drop-out, 3: variable follow-up with a minimum fu and a maximum fu, 4: variable follow-up with a minimum fu and a maximum fu and drop-out.

# Usage

```
ynegbinompowersim(nsize=200,r0=1.0,r1=0.5,shape0=1,shape1=shape0,pi1=0.5,
   alpha=0.05, two sided=1, fixed fu=1, type=1, u=c(0.5, 0.5, 1), ut=c(0.5, 1.0, 1.5),
   tfix=ut[length(ut)]+0.5, maxfu=10.0, tchange=c(0,0.5,1),
   ratec1=c(0.15,0.15,0.15),ratec0=ratec1,rn=10000)
```

## **Arguments**

nsize	total number of subjects in two groups
r0	event rate for the control
r1	event rate for the treatment
shape0	dispersion parameter for the control
shape1	dispersion parameter for the treatment
pi1	allocation prob for the treatment
alpha	type-1 error

twosided 1: two-side, others: one-sided fixedfu fixed follow-up time for each patient

follow-up time type, type=1: fixed fu with fu time fixedfu; type=2: same as type

1 but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring 8 ynegbinompowersim

u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the drop-out rate changes. The first element of tchange must be zero. The above rates and tchange must have the same length.
ratec1	piecewise constant drop-out rate for the treatment
ratec0	piecewise constant drop-out rate for the control
rn	Number of repetitions

#### **Details**

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time fixedfu and the maximum follow-up time maxfu. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 1 follow-up,  $T_f = \tau_{min}$ . For type 2 follow-up,  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max}, C)$ . Let f be the density of f. Suppose that f is the number of event observed in follow-up time f for patient f with treatment assignment f in f is the number of event observed in follow-up time f for patient f in the treatment assignment f is the number of event observed in follow-up time f for patient f in the treatment assignment f in f follows a negative binomial distribution such that

$$P(Y_i = y \mid Z_i = j) = \frac{\Gamma(y + 1/k_j)}{\Gamma(y + 1)\Gamma(1/k_j)} \left(\frac{k_j u_i}{1 + k_j u_i}\right)^y \left(\frac{1}{1 + k_j u_i}\right)^{1/k_j},$$

where  $k_j$ , j = 0, 1 are the dispersion parameters for control j = 0 and treatment j = 1 and

$$\log(u_i) = \log(t_i) + \beta_0 + \beta_1 Z_i.$$

The data will be gnerated according to the above model. Note that the piecewise exponential distribution and the piecewise uniform distribution are genrated using R package PWEALL functions "rpwe" and "rpwu", respectively.

The parameters in the model are estimated by MLE using the R package MASS function "glm.nb".

#### Value

power simulation power (in percentage)

#### Author(s)

Xiaodong Luo

#### **Examples**

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```
ratec1 = c(0.15, 0.15, 0.15), rn = 10) \\ \#\#Power \\ abc\$power
```

ynegbinomsize

Two-sample sample size calculation for negative binomial distribution with variable follow-up

# Description

This will calculate the sample size for the negative binomial distribution for the 2-sample case under different follow-up scenarios: 1: fixed follow-up, 2: fixed follow-up with drop-out, 3: variable follow-up with a minimum fu and a maximum fu, 4: variable follow-up with a minimum fu and a maximum fu and drop-out.

## Usage

#### **Arguments**

r0	event rate for the control
r1	event rate for the treatment
shape0	dispersion parameter for the control
shape1	dispersion parameter for the treatment
pi1	allocation prob for the treatment
alpha	type-1 error
twosided	1: two-side, others: one-sided
beta	tyep-2 error
fixedfu	fixed follow-up time for each patient
type	follow-up time type, type=1: fixed fu with fu time fixedfu; type=2: same as 1 but subject to censoring; type=3: depending on entry time, minimum fu is fixedfu and maximum fu is maxfu; type=4: same as 3 but subject to censoring
u	recruitment rate
ut	recruitment interval, must have the same length as u
tfix	fixed study duration, often equals to recruitment time plus minimum follow-up fixedfu
maxfu	maximum follow-up time, should not be greater than tfix
tchange	a strictly increasing sequence of time points starting from zero at which the

drop-out rate changes. The first element of tchange must be zero.

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ratec1 piecewise constant drop-out rate for the treatment. The rate and tchange must

have the same length.

ratec0 piecewise constant drop-out rate for the control. The rate and tchange must

have the same length.

eps error tolerance for the numerical intergration

#### **Details**

Let  $\tau_{min}$  and  $\tau_{max}$  correspond to the minimum follow-up time fixedfu and the maximum follow-up time maxfu. Let  $T_f$ , C, E and R be the follow-up time, the drop-out time, the study entry time and the total recruitment period(R is the last element of ut). For type 1 follow-up,  $T_f = \tau_{min}$ . For type 2 follow-up,  $T_f = min(C, \tau_{min})$ . For type 3 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max})$ . For type 4 follow-up,  $T_f = min(R + \tau_{min} - E, \tau_{max}, C)$ . Let f be the density of f. Suppose that f is the number of event observed in follow-up time f for patient f with treatment assignment f in f is the number of event observed in follow-up time f for patient f in the treatment assignment f in f is the number of event observed in follow-up time f for patient f in the treatment assignment f in f

$$P(Y_i = y \mid Z_i = j) = \frac{\Gamma(y + 1/k_j)}{\Gamma(y + 1)\Gamma(1/k_j)} \left(\frac{k_j u_i}{1 + k_j u_i}\right)^y \left(\frac{1}{1 + k_j u_i}\right)^{1/k_j},$$

where

$$\log(u_i) = \log(t_i) + \beta_0 + \beta_1 Z_i.$$

Let  $\hat{\beta}_0$  and  $\hat{\beta}_1$  be the MLE of  $\beta_0$  and  $\beta_1$ . The varaince of  $\hat{\beta}_1$  is

$$\operatorname{var}(\hat{\beta}_1) = 1/\tilde{a}_0(r_0) + 1/\tilde{a}_1(r_1)$$

where

$$\tilde{a}_j(r) = \sum_{i=1}^n I(Z_i = j) k_j r t_i / (1 + k_j r t_i), \quad j = 0, 1,$$

and  $k_j$ , j = 0, 1 are the dispersion parameters for control j = 0 and treatment j = 1. Note that Zhu and Lakkis (2014) use

$$a_j(r) = \sum_{i=1}^n I(Z_i = j)k_j r E(t_i) / \{1 + k_j r E(t_i)\},$$

to replace  $\tilde{a}_j(r)$ , j=0,1. Using Jensen's inequality, we can show  $a_j(r) \geq \tilde{a}_j(r)$ , which means Zhu and Lakkis's method will underestimate variance of  $\hat{\beta}_1$ , which leads to either smaller than required sample size or inflated power. For comparison, I provide sample sizes under both  $\tilde{a}_j(r)$  and  $a_j(r)$ .

Zhu and Lakkis (2014) discuss three types of the variance under the null. The first way is to set  $\tilde{r}_0 = \tilde{r}_1 = r_0$ , using event rate from the control group. The second way is to set  $\tilde{r}_0 = r_0$ ,  $\tilde{r}_1 = r_1$ , using true event rates. The third way is to set  $\tilde{r}_0 = \tilde{r}_1 = \tilde{r}$ , where  $\tilde{r} = \pi_1 r_1 + \pi_0 r_0$ , using maximum likelihood estimation.

Therefore, for each type of follow-up, there are 3 sample sizes calculated (because there are 3 varainces under the null) for with and without approximation of Zhu and Lakkis (2014).

Note that PASS14.0 provides 3 ways of null varaince with the default being the MLE. PASS does not allow different dispersion parameters between treatment and control. EAST only provides the second way of null varaince but allows for different dispersion parameters. Both of these softwares base on the approximatin method of Zhu and Lakkis (2014), which underestimate the required sample sizes.

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## Value

tildeXN sample sizes based on current approach, i.e. not based on the Zhu and Lakkis's

approximation

XN sample sizes based on the Zhu and Lakkis's approximation

Exposure mean exposure under different follow-up types with element 1 for control, ele-

ment 2 for treatment and element 3 for overall.

SDExp Sd of the exposure under different follow-up types with element 1 for control,

element 2 for treatment and column 3 for overall.

#### Author(s)

Xiaodong Luo

#### References

Zhu~H and Lakkis~H. Sample size calculation for comparing two negative binomial rates. Statistics in Medicine 2014, 33: 376-387.

# **Examples**

```
##calculating the sample sizes
abc=ynegbinomsize(r0=1.0,r1=0.5,shape0=1,pi1=0.5,alpha=0.05,twosided=1,
    beta=0.2,fixedfu=1,type=4,u=c(0.5,0.5,1),ut=c(0.5,1.0,1.5),
    tfix=1.5,maxfu=1,tchange=c(0,0.5,1),ratec1=c(0.15,0.15,0.15),
    eps=1.0e-03)
###Zhu and Lakkis's sample sizes (i.e. with approximation)
abc$XN
###Our sample sizes (i.e. without approximation)
abc$tildeXN
```

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