# Package 'FADA'

January 20, 2025

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## **Description**

The functions provided in the FADA (Factor Adjusted Discriminant Analysis) package aim at performing supervised classification of high-dimensional and correlated profiles. The procedure combines a decorrelation step based on a factor modeling of the dependence among covariates and a classification method. The available methods are Lasso regularized logistic model (see Friedman et al. (2010)), sparse linear discriminant analysis (see Clemmensen et al. (2011)), shrinkage linear and diagonal discriminant analysis (see M. Ahdesmaki et al. (2010)). More methods of classification can be used on the decorrelated data provided by the package FADA.

#### **Details**

Package: FADA Type: Package Version: 1.2

Date: 2014-10-08 License: GPL (>= 2)

The functions available in this package are used in this order:

- Step 1: Decorrelation of the training dataset using a factor model of the covariance by the decorrelate.train function. The number of factors of the model can be estimated or forced.
- Step 2: If needed, decorrelation of the testing dataset by using the decorrelate.test function and the estimated factor model parameters provided by decorrelate.train.
- Step 3: Estimation of a supervised classification model using the decorrelated training dataset by the FADA function. One can choose among several classification methods (more details in the manual of FADA function).
- Step 4: If needed, computation of the error rate by the FADA function, either using a supplementary test dataset or by K-fold cross-validation.

## Author(s)

Emeline Perthame (Agrocampus Ouest, Rennes, France), Chloe Friguet (Universite de Bretagne Sud, Vannes, France) and David Causeur (Agrocampus Ouest, Rennes, France)

Maintainer: David Causeur, http://math.agrocampus-ouest.fr/infoglueDeliverLive/membres/david.causeur, mailto: david.causeur@agrocampus-ouest.fr

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#### References

Ahdesmaki, M. and Strimmer, K. (2010), Feature selection in omics prediction problems using cat scores and false non-discovery rate control. Annals of Applied Statistics, 4, 503-519.

Clemmensen, L., Hastie, T. and Witten, D. and Ersboll, B. (2011), Sparse discriminant analysis. Technometrics, 53(4), 406-413.

Friedman, J., Hastie, T. and Tibshirani, R. (2010), Regularization paths for generalized linear models via coordinate descent. Journal of Statistical Software, 33, 1-22.

Friguet, C., Kloareg, M. and Causeur, D. (2009), A factor model approach to multiple testing under dependence. Journal of the American Statistical Association, 104:488, 1406-1415.

Perthame, E., Friguet, C. and Causeur, D. (2015), Stability of feature selection in classification issues for high-dimensional correlated data, Statistics and Computing.

## **Examples**

```
### Not run
### example of an entire analysis with FADA package if a testing data set is available
### loading data
# data(data.train)
# data(data.test)
# dim(data.train$x) # 30 250
# dim(data.test$x) # 1000 250
### decorrelation of the training data set
# res = decorrelate.train(data.train) # Optimal number of factors is 3
### decorrelation of the testing data set afterward
# res2 = decorrelate.test(res,data.test)
### classification step with sda, using local false discovery rate for variable selection
### linear discriminant analysis
# FADA.LDA = FADA(res2,method="sda",sda.method="lfdr")
### diagonal discriminant analysis
# FADA.DDA = FADA(res2, method="sda", sda.method="lfdr", diagonal=TRUE)
### example of an entire analysis with FADA package if no testing data set is available
### loading data
### decorrelation step
# res = decorrelate.train(data.train) # Optimal number of factors is 3
### classification step with sda, using local false discovery rate for variable selection
### linear discriminant analysis, error rate is computed by 10-fold CV (20 replications of the CV)
# FADA.LDA = FADA(res,method="sda",sda.method="lfdr")
```

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| data.test | Test dataset simulated with the same distribution as the training |
|-----------|---|
|           | dataset data.train.   |

## **Description**

The test dataset has the same list structure as the training dataset dta. Only the numbers of rows of the x component and length of the y component are different since the test sample size is 1000.

## Usage

```
data(data.test)
```

#### **Format**

List with 2 components: x, the 1000x250 matrix of simulated explanatory variables and y, the 1000x1 grouping variable (coded 1 and 2).

## **Examples**

```
data(data.test)
dim(data.test$x) # 1000 250
data.test$y # 2 levels
```

data.train

Training data

## **Description**

Simulated training dataset. The x component is a matrix of explanatory variables, with 30 rows and 250 columns. Each row is simulated according to a multinormal distribution which mean depends on a group membership given by the y component. The variance matrix is the same within each group.

## Usage

```
data(data.train)
```

## **Format**

A list with 2 components. x is a 30x250 matrix of simulated explanatory variables. y is a 30x1 grouping variable (coded 1 and 2).

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## **Examples**

```
data(data.train)
dim(data.train$x) # 30 250
data.train$y # 2 levels
hist(cor(data.train$x[data.train$y==1,])) # high dependence
hist(cor(data.train$x[data.train$y==2,]))
```

decorrelate.test

Factor Adjusted Discriminant Analysis 2: Decorrelation of a testing data set after running the decorrelate.train function on a training

data set

## **Description**

This function decorrelates the test dataset by adjusting data for the effects of latent factors of dependence, after running the decorrelate.train function on a training data set.

## Usage

```
decorrelate.test(faobject,data.test)
```

## **Arguments**

faobject An object returned by function decorrelate.train.

data.test A list containing the testing dataset, with the following component: x is a n x p

matrix of explanatory variables, where n stands for the testing sample size and

p for the number of explanatory variables.

## Value

Returns a list with the following elements:

meanclass Group means estimated after iterative decorrelation

fa.training Decorrelated training data fa.testing Decorrelated testing data

Psi Estimation of the factor model parameters: specific variance

B Estimation of the factor model parameters: loadings

factors.training

Scores of the trainings individuals on the factors

factors.testing

Scores of the testing individuals on the factors

groups Recall of group variable of training data

proba.training Internal value (estimation of individual probabilities for the training dataset) proba.testing Internal value (estimation of individual probabilities for the testing dataset)

mod.decorrelate.test

Internal value (classification model)

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#### Author(s)

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#### References

Friedman, J., Hastie, T. and Tibshirani, R. (2010), Regularization paths for generalized linear models via coordinate descent. Journal of Statistical Software, 33, 1-22.

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#### See Also

```
FADA-package FADA glmnet-package
```

## **Examples**

```
data(data.train)
data(data.test)
fa = decorrelate.train(data.train)
fa2 = decorrelate.test(fa,data.test)
names(fa2)
```

decorrelate.train

Factor Adjusted Discriminant Analysis 1: Decorrelation of the training data

## Description

This function decorrelates the training dataset by adjusting data for the effects of latent factors of dependence.

#### Usage

```
decorrelate.train(data.train, nbf = NULL, maxnbfactors=12, diagnostic.plot = FALSE,
min.err = 0.001, verbose = TRUE,EM = TRUE, maxiter = 15,...)
```

## **Arguments**

data.train A list containing the training dataset with the following components: x is the n

x p matrix of explanatory variables, where n stands for the training sample size and p for the number of explanatory variables; y is a numeric vector giving the group of each individual numbered from 1 to V

group of each individual numbered from 1 to K.

nbf Number of factors. If nbf = NULL, the number of factors is estimated. nbf can

also be set to a positive integer value. If nbf = 0, the data are not factor-adjusted.

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maxnbfactors The maximum number of factors. Default is maxnbfactors=12. diagnostic.plot

If diagnostic.plot =TRUE, the values of the variance inflation criterion are plotted for each number of factors. Default is diagnostic.plot =FALSE. This option might be helpful to manually determine the optimal number of factors.

min.err Threshold of convergence of the algorithm criterion. Default is min.err=0.001.

verbose Print out number of factors and values of the objective criterion along the itera-

tions. Default is TRUE.

EM The method used to estimate the parameters of the factor model. If EM=TRUE, pa-

rameters are estimated by an EM algorithm. Setting EM=TRUE is recommended when the number of covariates exceeds the number of observations. If EM=FALSE, the parameters are estimated by maximum-likelihood using factanal. Default

is EM=TRUE

maxiter Maximum number of iterations for estimation of the factor model.

... Other arguments that can be passed in the cv.glmnet and glmnet functions

from glmnet package. These functions are used to estimate individual group probabilities. Modifying these parameters should not affect the decorrelation procedure. However, the argument nfolds in cv.glmnet is set to 10 by default and should be reduced (minimum 3) for large datasets, in order to decrease the

computation time of decorrelation.train.

#### Value

Returns a list with the following elements:

meanclass Group means estimated after iterative decorrelation

fa. training Decorrelated training data

Psi Estimation of the factor model parameters: specific variance

B Estimation of the factor model parameters: loadings

factors.training

Scores of the trainings individuals on the factors

groups Recall of group variable of training data

proba.training Internal value (estimation of individual probabilities for the training dataset)

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Friedman, J., Hastie, T. and Tibshirani, R. (2010), Regularization paths for generalized linear models via coordinate descent. Journal of Statistical Software, 33, 1-22.

Friguet, C., Kloareg, M. and Causeur, D. (2009), A factor model approach to multiple testing under dependence. Journal of the American Statistical Association, 104:488, 1406-1415.

Perthame, E., Friguet, C. and Causeur, D. (2015), Stability of feature selection in classification issues for high-dimensional correlated data, Statistics and Computing.

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## See Also

FADA-package FADA glmnet-package factanal

## **Examples**

```
data(data.train)

res0 = decorrelate.train(data.train,nbf=3) # when the number of factors is forced

res1 = decorrelate.train(data.train) # when the optimal number of factors is unknown

FADA

Factor Adjusted Discriminant Analysis 3-4: Supervised classification
```

## Description

This function performs supervised classification on factor-adjusted data.

on decorrelated data

## Usage

```
\label{eq:FADA} FADA(faobject, K=10,B=20, nbf.cv = NULL, method = c("glmnet", "sda", "sparseLDA"), sda.method = c("lfdr", "HC"), alpha=0.1, ...)
```

## Arguments

| faobject   | An object returned by function decorrelate.train or decorrelate.test.   |
|------------|---|
| K          | Number of folds to estimate classification error rate, only when no testing data is provided. Default is K=10.  |
| В          | Number of replications of the cross-validation. Default is B=20.  |
| nbf.cv     | Number of factors for cross validation to compute error rate, only when no testing data is provided. By default, nbf = NULL and the number of factors is estimated for each fold of the cross validation. nbf can also be set to a positive integer value. If nbf = 0, the data are not factor-adjusted.  |
| method     | The method used to perform supervised classification model. 3 options are available. If method = "glmnet", a Lasso penalized logistic regression is performed using <b>glmnet</b> R package. If method = "sda", a LDA or DDA (see diagonal argument) is performed using Shrinkage Discriminant Analysis using <b>sda</b> R package. If method = "sparseLDA", a Lasso penalized LDA is performed using <b>SparseLDA</b> R package. |
| sda.method | The method used for variable selection, only if method="sda". If sda.method="lfdr", variables are selected through CAT scores and False Non Discovery Rate control. If sda.method="HC", the variable selection method is Higher Cristicism Thresholding.  |
| alpha      | The proportion of the HC objective to be observed, only if method="sda" and sda.method="HC". Default is 0.1.  |

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... Some arguments to tune the classification method. See the documentation of the chosen method (glmnet, sda or sda) for more informations about these parame-

ters.

## Value

Returns a list with the following elements:

| method       | Recall of the classification method   |
|--------------|---|
| selected     | A vector containing index of the selected variables   |
| proba.train  | A matrix containing predicted group frequencies of training data.   |
| proba.test   | A matrix containing predicted group frequencies of testing data, if a testing data set has been provided  |
| predict.test | A matrix containing predicted classes of testing data, if a testing data set has been provided  |
| cv.error     | A numeric value containing the average classification error, computed by cross validation, if no testing data set has been provided   |
| cv.error.se  | A numeric value containing the standard error of the classification error, computed by cross validation, if no testing data set has been provided                                 |
| mod          | The classification model performed. The class of this element is the class of a model returned by the chosen method. See the documentation of the chosen method for more details. |

## Author(s)

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#### References

Ahdesmaki, M. and Strimmer, K. (2010), Feature selection in omics prediction problems using cat scores and false non-discovery rate control. Annals of Applied Statistics, 4, 503-519.

Clemmensen, L., Hastie, T. and Witten, D. and Ersboll, B. (2011), Sparse discriminant analysis. Technometrics, 53(4), 406-413.

Friedman, J., Hastie, T. and Tibshirani, R. (2010), Regularization paths for generalized linear models via coordinate descent. Journal of Statistical Software, 33, 1-22.

Friguet, C., Kloareg, M. and Causeur, D. (2009), A factor model approach to multiple testing under dependence. Journal of the American Statistical Association, 104:488, 1406-1415.

Perthame, E., Friguet, C. and Causeur, D. (2015), Stability of feature selection in classification issues for high-dimensional correlated data, Statistics and Computing.

#### See Also

FADA, decorrelate.train, decorrelate.test, sda, sda-package, glmnet-package

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## Examples

```
data(data.train)
data(data.train)
data(data.test)

# When testing data set is provided
res = decorrelate.train(data.train)
res2 = decorrelate.test(res, data.test)
classif = FADA(res2,method="sda",sda.method="lfdr")

### Not run
# When no testing data set is provided
# Classification error rate is computed by a K-fold cross validation.
# res = decorrelate.train(data.train)
# classif = FADA(res, method="sda",sda.method="lfdr")
```

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