

# Package ‘DstarM’

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**Type** Package

**Title** Analyze Two Choice Reaction Time Data with the D\*M Method

**Version** 0.4.0

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**Description** A collection of functions to estimate parameters of a diffusion model via a D\*M analysis. Build in models are: the Ratcliff diffusion model, the RWiener diffusion model, and Linear Ballistic Accumulator models. Custom models functions can be specified as long as they have a density function.

**License** GPL (>= 2)

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chisq	<i>Calculates the distance between two probability densities.</i>
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### Description

Calculates the distance between two probability densities.

### Usage

chisq(tt, a, b)

battacharyya(tt, a, b)

hellinger(tt, a, b)

### Arguments

tt           the time grid on which the densities are evaluated.

a            a vector with values of the first density.

b            a vector with values of the second density.

### Value

The distance between densities a and b.

**Examples**

```

# Lets simulate a bunch of parameters and compare the three distance measures.

tt = seq(0, 5, .001)
parsMatV = cbind(.8, seq(0, 5, .5), .5, .5, .5) # differ only in drift speed
parsMatA = cbind(seq(.5, 2, .15), 2, .5, .5, .5)# differ only in boundary
# calculate densities for all these parameters
dV = apply(parsMatV, 1, function(x, tt) Voss.density(tt, x, boundary = 'upper'), tt = tt)
dA = apply(parsMatA, 1, function(x, tt) Voss.density(tt, x, boundary = 'upper'), tt = tt)
# make plots of the densities
matplot(tt, dA, xlim = c(0, .6), main = 'Densities with different Boundary',
        col = rainbow(ncol(dA)),type = 'l', lty = 1, las = 1, bty = 'n',
        xlab = 'Time', ylab = 'Density')
legend('topright', lty = 1, bty = 'n', col = rainbow(ncol(dA)),
      legend = paste('a = ', parsMatA[, 1]))
matplot(tt, dV, xlim = c(0, .6), main = 'Densities with different Drift Speed',
        col = rainbow(ncol(dV)), type = 'l', lty = 1, las = 1, bty = 'n',
        xlab = 'Time', ylab = 'Density')
legend('topright', lty = 1, bty = 'n', col = rainbow(ncol(dV)),
      legend = paste('v = ',parsMatV[, 2]))
# empty matrices for data storage
distMatV = matrix(NA, nrow = ncol(dV) - 1, ncol = 3,
                 dimnames = list(NULL, c('Chisq', 'Bhattacharyya', 'Hellinger')))
distMatA = matrix(NA, nrow = ncol(dA) - 1, ncol = 3,
                 dimnames = list(NULL, c('Chisq', 'Bhattacharyya', 'Hellinger')))
# calculate distances between densities in column i and i + 1.
# this is done using three different distance measures
for (i in 1:(ncol(dA) - 1)) {
  distMatV[i, ] = c(chisq(tt, dV[, i], dV[, i + 1]),
                  battacharyya(tt, dV[, i], dV[, i + 1]),
                  hellinger(tt, dV[, i], dV[, i + 1]))
  distMatA[i, ] = c(chisq(tt, dA[, i], dA[, i + 1]),
                  battacharyya(tt, dA[, i], dA[, i + 1]),
                  hellinger(tt, dA[, i], dA[, i + 1]))
}
# The three distance measures correlate highly for differences in Boundary
cor(distMatA)
# The battacharyya distance measures does not correlate with the others
# when calculating differences in drift speed
cor(distMatV)

```

---

chisqFit

*Calculate model fit*


---

**Description**

Calculate model fit

**Usage**

```
chisqFit(resObserved, data, DstarM = FALSE, tt = NULL, formula = NULL)
```

**Arguments**

resObserved	either output from <code>estObserved</code> or a matrix containing custom densities to calculate the fitness for.
data	A dataframe containing data.
DstarM	Logical. Should the DstarM fit measure be calculated or the traditional fit measure?
tt	time grid custom densities where calculated on. Should only be supplied if resObserved is a matrix containing custom densities
formula	Optional formula argument, for when columns names in the data are different from those used to obtain the results.

**Details**

This function allows a user to manually calculate a chi-square goodness of fit measure for model densities. This is useful for comparing a traditional analysis and a D\*M analysis. For completion, this function can also calculate a D\*M fit measure. We do not recommend usage of the D\*M measure. While the chi-square fit measure is identical to the value of the optimizer when fitting, the DstarM fit measure is not equal to that of a DstarM analysis. This is because this function calculates the DstarM fit measure on the complete distribution, not on the model distributions, as is done during the optimization.

**Examples**

```
tt = seq(0, 5, .1)
pars = c(.8, 2, .5, .5, .5, # condition 1
         .8, 3, .5, .5, .5, # condition 2
         .8, 4, .5, .5, .5) # condition 3
pdfND = dbeta(tt, 10, 30)

# simulate data
allDat = simData(n = 3e3, pars = pars, tt = tt, pdfND = pdfND, return.pdf = TRUE)
truePdf = allDat$pdfUnnormalized
dat = allDat$dat
chisqFit(resObserved = truePdf, data = dat, tt = tt)
## Not run:
# estimate it
define restriction matrix
restr = matrix(1:5, 5, 3)
restr[2, 2:3] = 6:7 # allow drift rates to differ
# fix parameters for speed up
fixed = matrix(c('z1', 'a1 / 2', 'sz1', .5, 'sv1', .5), 2, 3)
resD = estDstarM(data = dat, tt = tt, restr = restr, fixed = fixed,
                 Optim = list(parallelType = 1))
resN = estND(resD, Optim = list(parallelType = 1))

res0 = estObserved(resD, resN, data = dat)
res0$fit # proper fit

## End(Not run)
```

---

Density	<i>Density function</i>
---------	-------------------------

---

**Description**

Density function

**Usage**

```
Density(rt, tt)
```

**Arguments**

rt	vector of reaction times
tt	grid to evaluate the density on

**Details**

Can be passed to the argument `densityMethod` of `estDstarM`. This function is a minimal example to use as custom smoothing function.

**Value**

a vector of length(tt)

**Examples**

```
x <- rgamma(1e5, 1, 1)
tt <- seq(0, 5, .01)
d <- Density(x, tt)
hist(x, freq = FALSE)
lines(tt, DstarM::Density(x, tt))
```

---

estCdf	<i>Estimate cumulative distribution for D*M models</i>
--------	--

---

**Description**

Estimate cumulative distribution for D\*M models

**Usage**

```
estCdf(x)
```

**Arguments**

`x` Any density function to calculate a cumulative distribution for. The code is designed for input of class `DstarM` but other input is also accepted. Other input can be either a matrix where columns represent densities or a single vector representing a density.

**Details**

Cumulative distributions functions are calculated by: `cumsum(x) / sum(x)`. This method works well enough for our purposes. The example below shows that the `ecdf` functions seems to work slightly better. However, this estimates a cdf from raw data and does not transform a pdf into a cdf and is therefore not useful for  $D \times M$  models.

**Value**

Cumulative density function(s). If the input was a matrix, a matrix of cumulative density functions is returned.

**Examples**

```
x = rnorm(1000)
xx = seq(-5, 5, .1)
approx1 = stats::ecdf(x)(xx)
approx2 = estCdf(dnorm(xx, mean(x), sd(x)))
trueCdf = pnorm(xx)
matplot(xx, cbind(trueCdf, approx1, approx2), type = c('l', 'p', 'p'),
        lty = 1, col = 1:3, pch = 1, bty = 'n', las = 1, ylab = 'Prob')
legend('topleft', legend = c('True Cdf', 'Stats Estimation', 'DstarM Estimation'),
      col = 1:3, lty = c(1, NA, NA), pch = c(NA, 1, 1), bty = 'n')
```

---

 estDstarM

*Do a  $D \times M$  analysis*


---

**Description**

Do a  $D \times M$  analysis

**Usage**

```
estDstarM(
  formula = NULL,
  data,
  tt,
  restr = NULL,
  fixed = list(),
  lower,
  upper,
```

```

  Optim = list(),
  DstarM = TRUE,
  SE = 0,
  oscPdf = TRUE,
  splits = rep(0L, (ncondition)),
  forceRestriction = TRUE,
  mg = NULL,
  h = 1,
  pars,
  fun.density = Voss.density,
  args.density = list(),
  fun.dist = chisq,
  args.dist = list(tt = tt),
  verbose = 1L,
  useRcpp = TRUE
)

```

### Arguments

formula	A formula object of the form: binary response ~ reaction time + condition1 * condition2 * ... conditionN.
data	A dataframe for looking up data specified in formula. For backwards compatibility this can also be with: a column named <code>rt</code> containing response times in ms, a column named <code>response</code> containing at most 2 response options, and an optional column named <code>condition</code> containing a numeric index as to which conditions observations belong.
tt	A time grid on which the density function will be evaluated. Should be larger than the highest observed reaction time.
restr	A restriction matrix where each column depicts one condition. The number of rows should match the number of parameters (and be equal to the length of lower). The contents of <code>restr</code> should be numbers, identical numbers means that these parameters (either within or between condition) will be constrained. Different numbers means parameters will not be constrained.
fixed	A matrix that allows for fixing parameters to certain values.
lower	Should be a vector containing lower bounds for each parameter. Has a default if <code>fun.density == Voss.density</code> .
upper	Should be a vector containing upper bounds for each parameter. Has a default if <code>fun.density == Voss.density</code> .
Optim	a named list with identical arguments to <code>DEoptim.control</code> . In addition, if <code>verbose == TRUE</code> <code>Optim\$steptol</code> can be a vector, i.e. <code>c(200, 50, 10)</code> means: Do 200 iterations then check for convergence, do 50 iterations then check for convergence, check every 10 iterations for convergence until <code>itermax</code> is reached. Defaults to <code>Optim = list(reltol = 1e-6, itermax = 1e3, steptol = 50, CR = .9, trace = 0, parallelType = 0)</code> .
DstarM	If TRUE a D*M analysis is done, otherwise the Chi square distance between data and model is minimized.

SE	positive value, how many standard error to add to the variance to relax the variance restriction a bit.
oscPdf	Logical, if TRUE check for oscillations in calculated densities and remove densities with oscillations.
splits	Numeric vector determining which conditions have an equal nondecision density. Identical values in two positions indicate that the conditions corresponding to the indices of those values have an identical nondecision distribution.
forceRestriction	if TRUE the variance restriction is enforced.
mg	Supply a data density, useful if a uniform kernel approximation does not suffice. Take care that densities of response categories within conditions are degenerate and therefore integrate to the proportion a category was observed (and not to 1).
h	bandwidth of a uniform kernel used to generate data based densities.
pars	Optional parameter vector to supply if one wishes to evaluate the objective function in a given parameter vector. Only used if <code>itermax</code> equal zero.
fun.density	Function used to calculate densities. See details.
args.density	A names list containing additional arguments to be send to <code>fun.density</code> .
fun.dist	Function used to calculate distances between densities. Defaults to a chi-square distance.
args.dist	A named list containing additional arguments to be send to <code>fun.dist</code> .
verbose	Numeric, should intermediate output be printed? Defaults to 1, higher values result in more progress output. Estimation will speed up if set to 0. If set to TRUE, <code>Optim\$trace</code> will be forced to 0, hereby disabling the build in printing of <code>DEoptim</code> . To enable the printing of <code>DEoptim</code> , set <code>verbose</code> to 0 and specify <code>Optim\$trace</code> . <code>Optim</code> . If set to 1, ETA refers to the expected maximum time until completion (when the iterations limit is reached).
useRcpp	Logical, setting this to true will make the objective function use an Rcpp implementation of <code>Voss.density</code> with the distance function <code>chisq</code> . This gains speed at the cost of flexibility.

## Details

Response options will be alphabetically sorted and the first response option will be treated as the 'lower' option. This means that if the observed proportion of the first response options is higher, the drift speed will most likely be negative.

`fun.density` allows a user to specify a custom density function. This function must (at least) take the following arguments: `t`: a vector specifying at which time points to calculate the density `pars`: a parameter vector `boundary`: character 'upper' or 'lower' specifying for which response option the density will be calculated. `DstarM`: Logical, if TRUE the density should not describe the nondecision density, if FALSE it should describe the nondecision density. Any additional arguments can be passed to `fun.density` via the argument `args.density`. If one intends to use a custom density function it is recommended to test the function first with `testFun`. When specifying a custom density function it is probably also necessary to change the lower and upper bounds of the parameter space.



For purposes of speed, the function can be run in parallel by providing the argument `Optim = list(parallelType = 1)`. See [DEoptim.control](#) for details. Also, for Ratcliff models the objective function has been rewritten in Rcpp. This limits some functionality but does result in a faster estimation. Usage of Rcpp can be enabled via `useRcpp = TRUE`.

When `verbose` is set to 1, the ETA is an estimated of the time it takes to execute ALL iterations. Convergence can (and is usually) reached before then.

## Value

Returns a list of class `DstarM.fitD` that contains:

<code>Bestvals</code>	Named numeric vector. Contains the best parameter estimates.
<code>fixed</code>	Numeric vector. Contains the best parameter estimates.
<code>GlobalOptimizer</code>	List. All output from the call to <a href="#">DEoptim</a>
<code>Debug</code>	List. contains the number of <code>DEoptim</code> iterations, the number of function evaluation of the objective function, and the maximum number of iterations.
<code>note</code>	String. A possible note that is used for summary purposes
<code>tt</code>	Numeric vector. Contains the time grid used.
<code>g.hat</code>	Numeric matrix. Named columns represent the (possibly smoothed) densities of the data distribution of each condition-response pair.
<code>modelDist</code>	Numeric matrix. Named columns represent the densities of the model evaluated at grid <code>tt</code> with parameters <code>Bestvals</code> .
<code>ncondition</code>	Numeric scalar. The number of conditions
<code>var.data</code>	Numeric vector. The variance of each condition-response pair. There are as many values as hypothesized nondecision densities.
<code>var.m</code>	Numeric vector. The variance of the model distributions. There are as many values as hypothesized nondecision densities.
<code>restr.mat</code>	Numeric matrix. Contains the restrictions used.
<code>splits</code>	Numeric vector. Equal to the input argument with the same name.
<code>n</code>	Numeric scalar. The total number of observations.
<code>DstarM</code>	Logical. Equal to the input argument with the same name.
<code>fun.density</code>	Function. Equal to the input argument with the same name.
<code>fun.dist</code>	Function. Equal to the input argument with the same name.
<code>h</code>	Scalar. Equal to the input argument with the same name.
<code>args.density</code>	Named list. Equal to the input argument with the same name.
<code>args.dist</code>	Named list. Equal to the input argument with the same name.

**Examples**

```

# simulate data with three stimuli of different difficulty.
# this implies different drift rates across conditions.
# define a time grid. A more reasonable stepsize is .01; this is just for speed.
tt = seq(0, 5, .1)
pars = c(.8, 2, .5, .5, .5, # condition 1
        .8, 3, .5, .5, .5, # condition 2
        .8, 4, .5, .5, .5) # condition 3
pdfND = dbeta(tt, 10, 30)
# simulate data
data = simData(n = 3e3, pars = pars, tt = tt, pdfND = pdfND)
# define restriction matrix
restr = matrix(1:5, 5, 3)
restr[2, 2:3] = 6:7 # allow drift rates to differ
# fix variance parameters
fixed = matrix(c('sz1', .5, 'sv1', .5), 2, 2)
## Not run:
# Run D*M analysis
res = estDstarM(data = data, tt = tt, restr = restr, fixed = fixed)
coef(res)
summary(res)

## End(Not run)

```

---

estND

*Estimate nondecision density*


---

**Description**

Estimate nondecision density

**Usage**

```

estND(
  res,
  tt = NULL,
  data = NULL,
  h = res$h,
  zp = 5,
  upper.bound = 1,
  lower.bound = 0,
  Optim = list(),
  verbose = TRUE,
  dist = NULL,
  NDindex,
  max = 100,
  useRcpp = TRUE
)

```

**Arguments**

res	an object of class D*M.
tt	optional timegrid if the nondecision density is to be estimated at a different grid than the model density.
data	if tt is specified then the original dataset must be supplied too.
h	Optional smoothing parameter to be used when estimating the nondecision model on a different time grid than the decision model. If omitted, the smoothing parameter of the decision model is used.
zp	Zero padding the estimated nondecision density by this amount to avoid numerical artefacts.
upper.bound	An upper bound for the nondecision density. Defaults to one. Lowering this bound can increase estimation speed, at the cost of assuming that the density of the nondecision distribution is zero past this value.
lower.bound	A lower bound for the nondecision density. Defaults to zero. Increasing this bound can increase estimation speed, at the cost of assuming that the density of the nondecision distribution is zero past this value.
Optim	a named list with identical arguments to <a href="#">DEoptim.control</a> . In addition, if verbose == TRUE Optim\$steptol can be a vector, i.e. c(200, 50, 10) means: Do 200 iterations then check for convergence, do 50 iterations then check for convergence, check every 10 iterations for convergence until itermax is reached. If there are multiple nondecision distributions to estimate, one can supply different estimation parameters for every nondecision distribution by supplying Optim as a list of lists. Every sublist then corresponds to parameters for one nondecision distribution and should consist of arguments for <a href="#">DEoptim.control</a> . Defaults to Optim = list(reltol = 1e-6, itermax = 1e4, steptol = 200, CR = .9, trace = 0).
verbose	Numeric, should intermediate output be printed? Defaults to 1, higher values result in more progress output. Estimation will speed up if set to 0. If nonzero, Optim\$trace will be forced to 0, hereby disabling the build in printing of DEoptim. To enable the printing of DEoptim, set verbose to 0 and specify Optim\$trace.
dist	A matrix where columns represent nondecision distributions. If this argument is supplied then the objective function will be evaluated in these values.
NDindex	A vector containing indices of which nondecision distributions to estimate. If omitted, all nondecision distributions that complement the results in res are estimated.
max	A positive float which indicates the maximum height of the nondecision distribution. If estimated nondecision distributions appear chopped off or have a lot of values at this max value it is recommended to re-estimate the nondecision distributions with a higher max value. Increasing the max value without reason will increase the size of the parameter space and slow the estimation procedure.
useRcpp	Logical, setting this to true will make use of an Rcpp implementation of the objective function. This gains speed at the cost of flexibility.

**Details**

When verbose is set to 1, the ETA is an estimated of the time it takes to execute ALL iterations. Convergence can (and is usually) reached before then.

**Examples**

```
# simulate data with three stimuli of different difficulty.
# this implies different drift rates across conditions.
# define a time grid. A more reasonable stepsize is .01; this is just for speed.
tt = seq(0, 5, .1)
pars = c(.8, 2, .5, .5, .5, # condition 1
         .8, 3, .5, .5, .5, # condition 2
         .8, 4, .5, .5, .5) # condition 3
pdfND = dbeta(tt, 10, 30)
# simulate data
dat = simData(n = 3e5, pars = pars, tt = tt, pdfND = pdfND)
# define restriction matrix
restr = matrix(1:5, 5, 3)
restr[2, 2:3] = 6:7 # allow drift rates to differ
# fix variance parameters
fixed = matrix(c('sz1', .5, 'sv1', .5), 2, 2)
## Not run:
# Run D*M analysis
res = estDstarM(data = dat, tt = tt, restr = restr, fixed = fixed)
# Estimate nondecision density
resND = estND(res)
plot(resND)
lines(tt, pdfND, type = 'b', col = 2)

## End(Not run)
```

---

 estObserved

*Estimate observed data density*


---

**Description**

Estimates the density of the observed data by convoluting the estimated decision distributions with the estimated nondecision distributions. If a traditional analysis was run the argument resND can be omitted.

**Usage**

```
estObserved(
  resDecision,
  resND = NULL,
  data = NULL,
  interpolateND = FALSE,
  tt = NULL
)
```

**Arguments**

resDecision	output of <code>estDstarM</code> .
resND	output of <code>estND</code> .
data	Optional. If the data used to estimate the decision model is supplied additional fitmeasures are calculated.
interpolateND	Logical. If the decision model and nondecision model have been estimated on different time grids, should the rougher time grid be interpolated to match the smaller grid? If FALSE (the default) the decision model will be recalculated on the grid of the nondecision model. This tends to produce better fit values.
tt	Optional time grid to recalculate the model densities on. Unused in case of a DstarM analysis.

**Value**

Returns a list of class `DstarM.fitObs` that contains:

obsNorm	A matrix containing normalized densities of each condition response pair.
obs	A matrix containing unnormalized densities of each condition response pair.
tt	The time grid used.
fit	A list containing the values of the objective function for the total model ( <code>\$total</code> ), for the decision model ( <code>\$Decision</code> ) and for the nondecision distribution(s) ( <code>\$ND</code> ).
npar	The number of parameters used in the decision model.
obsIdx	A numeric vector containing indices of any not observed condition-response pairs.

**Examples**

```
# simulate data with three stimuli of different difficulty.
# this implies different drift rates across conditions.
# define a time grid. A more reasonable stepsize is .01; this is just for speed.
tt = seq(0, 5, .1)
pars = c(.8, 2, .5, .5, .5, # condition 1
        .8, 3, .5, .5, .5, # condition 2
        .8, 4, .5, .5, .5) # condition 3
pdfND = dbeta(tt, 10, 30)
# simulate data
lst = simData(n = 3e5, pars = pars, tt = tt, pdfND = pdfND, return.pdf = TRUE)
dat = lst$dat
# define restriction matrix
restr = matrix(1:5, 5, 3)
restr[2, 2:3] = 6:7 # allow drift rates to differ
# fix variance parameters
fixed = matrix(c('sz1', .5, 'sv1', .5), 2, 2)
## Not run:
# Run D*M analysis
resD = estDstarM(dat = dat, tt = tt, restr = restr, fixed = fixed)
```

```

# Estimate nondecision density
resND = estND(resD)
# Estimate observed density
resObs = estObserved(resD, resND)
# plot histograms with overlaid
# densities per condition-response pair
plotObserved(resObserved = resObs, data = dat,
             xlim = c(0, 1))
# plot estimated and true densities
plot(resObs, col = rep(1:3, each = 2), xlim = 0:1)
matlines(tt, lst$pdfNormalized, col = rep(1:3, each = 2), lty = 2)

## End(Not run)

```

---

estQdf

*Estimate quantiles of distribution*


---

## Description

Estimate quantiles of distribution

## Usage

```
estQdf(p, x, cdf)
```

## Arguments

p	A vector of probabilities.
x	The x-axis values corresponding to the cumulative distribution function.
cdf	A cumulative distributions function, i.e. output of <a href="#">estCdf</a> .

## Details

Quantiles are obtained in the following manner. For  $p = 0$  and  $p = 1$ , the minimum and maximum of  $x$  is used. For other probabilities the quantiles are obtained via  $q[i] = \text{uniroot}(x, \text{cdf} - p[i])\$root$ . Y values are interpolated via [approxfun](#).

## Value

Quantiles of cumulative distribution function(s). If the input was a matrix of cumulative distributions functions, a matrix of quantiles is returned.

**Examples**

```
x = seq(-9, 9, .1) # x-grid
d = dnorm(x) # density functions
p = seq(0, 1, .2) # probabilities of interest
cEst = estCdf(d) # estimate cumulative distribution functions
qEst = estQdf(p = p, x = x, cdf = cEst) # estimate quantiles
plot(x, cEst, bty = 'n', las = 1, type = 'l', ylab = 'Probability') # plot cdf
abline(h = p, v = qEst, col = 1:6, lty = 2) # add lines for p and for obtained quantiles
points(x = qEst, y = p, pch = 18, col = 1:6, cex = 1.75) # add points for intersections
```

getPdfs

*(Re)Calculate model densities with given parameters and time grid***Description**

This function is a convenience function for calculating model pdfs for multiple sets of parameters at a specified timegrid. If `resDecision` is supplied, the density function and any additional arguments for the density function will be extracted from that object. If `pars` is missing these will also be extracted from this object. This function is intended to recalculate model densities at a new timegrid.

**Usage**

```
getPdfs(
  resDecision,
  tt,
  pars,
  DstarM = TRUE,
  fun.density = Voss.density,
  args.density = list()
)
```

**Arguments**

<code>resDecision</code>	output of <a href="#">estDstarM</a> .
<code>tt</code>	Time grid to calculate the model densities on.
<code>pars</code>	Model parameters, can be a matrix where every column is a set of parameters.
<code>DstarM</code>	Logical. Do the model pdfs also describe the nondecision distribution?
<code>fun.density</code>	density function to calculate pdfs from.
<code>args.density</code>	Additional arguments for <code>fun.density</code>

**Value**

A matrix containing model pdfs.

---

getSter	<i>Estimate variance of nondecision density</i>
---------	---

---

**Description**

Estimate variance of nondecision density

**Usage**

```
getSter(res)
```

**Arguments**

res	An object of class D*M.
-----	-------------------------

**Details**

The object res can either be output from estDstarM or output from estND. If the former is supplied, getSter attempts to calculate the variance of the nondecision distribution by subtracting the variance of the model distribution from the variance of the data distribution. If the latter is supplied, the variance is calculated by integrating the nondecision distribution.

---

getTer	<i>Calculate Mean of the nondecision distribution.</i>
--------	--

---

**Description**

Calculate Mean of the nondecision distribution.

**Usage**

```
getTer(res, data, formula = NULL)
```

**Arguments**

res	An object of class D*M.
data	The data object used to create res.
formula	Optional formula argument, for when columns names in the data are different from those used to obtain the results.

**Details**

The object res can either be output from estDstarM or output from estND. If the former is supplied it is also necessary to supply the data used for the estimation. The mean will then be estimated by subtracting the mean of the model densities from the mean of the data density. If the latter is supplied than this is not required; the mean will be calculated by integrating the nondecision distribution.



**Value**

A vector containing estimates for the mean of the nondecision densities.

---

normalize	<i>Normalize two pdfs</i>
-----------	---------------------------

---

**Description**

Normalize two pdfs

**Usage**

```
normalize(x, tt, props = NULL)
```

**Arguments**

x	Probability density function(s) evaluated at grid x. Input should be either a vector or matrix. If input is a matrix, each column represents a single pdf.
tt	a numeric grid defined in x.
props	the value each density should integrate to.

**Examples**

```
tt <- seq(0, 9, length.out = 1e4)
# 2 poper densities
x1 <- cbind(dexp(tt, .5), dexp(tt, 2))
# still 2 poper densities
x2 <- normalize(10*x1, tt)
# 2 densities that integrate to .5
x3 <- normalize(x1, tt, props = c(.5, .5))
# plot the results
matplot(tt, cbind(x1, x2, x3), type = "l", ylab = "density",
          col = rep(1:3, each = 2), lty = rep(1:2, 3), las = 1, bty = "n")
legend("topright", legend = rep(paste0("x", 1:3), each = 2),
       col = rep(1:3, each = 2), lty = rep(1:2, 3), bty = "n")
```

---

obsQuantiles	<i>Calculate model fit</i>
--------------	----------------------------

---

**Description**

This function is nothing but a wrapper for [quantile](#).

**Usage**

```
obsQuantiles(data, probs = seq(0, 1, 0.01), what = "cr")
```

**Arguments**

data	A dataframe with: a column named <code>rt</code> containing response times in ms, a column named <code>response</code> containing at most 2 response options, and an optional column named <code>condition</code> containing a numeric index as to which conditions observations belong.
probs	vector of probabilities for which the corresponding values should be called
what	Character. <code>'cr'</code> if the quantiles are to be calculated per condition-response pair, <code>'c'</code> if the quantiles are to be calculated per condition, and <code>'r'</code> if the quantiles are to be calculated per response.

**Examples**

```
tt = seq(0, 5, .01)
pars = c(.8, 2, .5, .5, .5, # condition 1
         .8, 3, .5, .5, .5, # condition 2
         .8, 4, .5, .5, .5) # condition 3
pdfND = dbeta(tt, 10, 30)
# simulate data
data = simData(n = 3e3, pars = pars, tt = tt, pdfND = pdfND)
probs = seq(0, 1, .01)
q = obsQuantiles(data, probs = probs)
matplot(probs, q, type = 'l', las = 1, bty = 'n')
```

---

plotObserved

---

*Plot quantiles of data against model implied quantiles.*


---

**Description**

Plots histograms for each condition-response pair/ condition/ response with overlaid estimated densities.

**Usage**

```
plotObserved(
  resObserved,
  data,
  what = c("cr", "c", "r"),
  layout = NULL,
  main = NULL,
  linesArgs = list(),
  ggplot = FALSE,
  prob = seq(0, 1, 0.01),
  probType = 3,
  ...
)
```

**Arguments**

resObserved	output of <a href="#">estObserved</a> .
data	The dataset used to estimate the model.
what	What to plot. Can be 'cr' for 'condition-response pairs', 'c' for condition, and 'r' for response.
layout	An optional layout matrix.
main	an optional vector containing names for each plot.
linesArgs	A list containing named arguments to be passed to <a href="#">lines</a> .
ggplot	Deprecated and ignored.
prob	Should a qqplot of observed vs model implied quantiles be plotted? By default, it is <code>seq(0, 1, .01)</code> , the probabilities between 0 and 1 to compare the model implied quantiles to the observed quantiles. If this argument is NULL, then a histogram overlaid with model implied densities will be plotted. Internally, <a href="#">estQdf</a> is used for generating quantiles.
probType	A numeric value defining several plotting options. 0 does nothing, 1 removes the 0% quantile, 2 removes the 100% quantile and 3 removes both the 0% and 100% quantile.
...	Further arguments to be passed to hist.

**Details**

Keep in mind when using `what = 'c'` or `what = 'r'` pdfs are simply averaged, not weighted to the number of observed responses.

**Value**

if `ggplot` is FALSE `invisible()`, otherwise a list

**Examples**

```
# simulate data with three stimuli of different difficulty.
# this implies different drift rates across conditions.
# define a time grid. A more reasonable stepsize is .01; this is just for speed.
tt = seq(0, 5, .1)
pars = c(.8, 2, .5, .5, .5, # condition 1
         .8, 3, .5, .5, .5, # condition 2
         .8, 4, .5, .5, .5) # condition 3
pdfND = dbeta(tt, 10, 30)
# simulate data
lst = simData(n = 3e5, pars = pars, tt = tt, pdfND = pdfND, return.pdf = TRUE)
dat = lst$dat
# define restriction matrix
restr = matrix(1:5, 5, 3)
restr[2, 2:3] = 6:7 # allow drift rates to differ
# fix variance parameters
fixed = matrix(c('sz1', .5, 'sv1', .5), 2, 2)
## Not run:
```

```

# Run D*M analysis
resD = estDstarM(dat = dat, tt = tt, restr = restr, fixed = fixed)
# Estimate nondecision density
resND = estND(resD)
# Estimate observed density
resObs = estObserved(resD, resND)
# plot histograms with overlaid
# densities per condition-response pair
plotObserved(resObserved = resObs, data = dat,
             xlim = c(0, 1))
# plot estimated and true densities
plot(resObs, col = rep(1:3, each = 2), xlim = 0:1)
matlines(tt, lst$pdfNormalized, col = rep(1:3, each = 2), lty = 2)
# other uses of plotObserved
plotObserved(resObserved = resObs, data = dat, what = 'cr', xlim = c(0, 1))
plotObserved(resObserved = resObs, data = dat, what = 'c', xlim = c(0, 1))
plotObserved(resObserved = resObs, data = dat, what = 'r', xlim = c(0, 1))

## End(Not run)

```

---

rtDescriptives

*Descriptives of reaction time data*


---

## Description

Descriptives of reaction time data

## Usage

```
rtDescriptives(formula = NULL, data, plot = TRUE, verbose = TRUE)
```

## Arguments

formula	A formula object of the form: binary response ~ reaction time + condition1 * condition2
data	A dataframe for looking up data specified in formula. For backwards compatibility this can also be with: a column named <code>rt</code> containing response times in ms, a column named <code>response</code> containing at most 2 response options, and an optional column named <code>condition</code> containing a numeric index as to which conditions observations belong.
plot	Logical, should a density plot of all condition-response pairs be made?
verbose	Logical, should a table of counts and proportions be printed?

## Details

This function and [rtHist](#) are helper functions to inspect raw data.

**Value**

Invisibly returns an object of class 'D\*M'. It's first element is table and contains raw counts and proportions for condition response pairs, conditions, and responses. It's second element plot contains a ggplot object.

**Examples**

```
tt <- seq(0, 5, .01)
pars <- matrix(.5, 5, 2)
pars[1, ] <- 1
pars[2, ] <- c(0, 2)
dat <- simData(n = 3e3, pars = pars, tt = tt, pdfND = dbeta(tt, 10, 30))
x <- rtDescriptives(data = dat)

print(x$table, what = 'cr')
print(x$table, what = 'c')
print(x$table, what = 'r')
```

---

rtHist

*Make histograms of reaction time data*


---

**Description**

Make histograms of reaction time data

**Usage**

```
rtHist(data, what = "cr", layout = NULL, nms = NULL, ggplot = FALSE, ...)
```

**Arguments**

data	A reaction time dataset. Must be a dataframe with \$rt, \$condition and \$response.
what	@param what What to plot. Can be 'cr' for 'condition-response pairs, 'c' for condition, and 'r' for response.
layout	An optional layout.
nms	An optional vector of names for each plot. If omitted the names will be based on the contents of data\$condition and/or data\$response.
ggplot	ggplot Logical, should ggplot2 be used instead of base R graphics? If set to TRUE, some arguments from linesArgs and ... will be ignored (but can be added to plots manually).
...	Arguments to be passed to hist

**Details**

This function and [rtDescriptives](#) are helper functions to inspect raw data.

**Value**

invisible()

**Examples**

```
tt = seq(0, 5, .01)
dat = simData(n = 3e4, pars = rep(.5, 5), tt = tt, pdfND = dbeta(tt, 10, 30))
rtHist(dat, breaks = tt, xlim = c(0, 1))
```

simData

*Simulate data from a given density function via multinomial sampling***Description**

Simulate data from a given density function via multinomial sampling

**Usage**

```
simData(
  n,
  pars,
  tt,
  pdfND,
  fun.density = Voss.density,
  args.density = list(prec = 3),
  npars = 5,
  return.pdf = FALSE,
  normalizePdfs = TRUE
)
```

**Arguments**

n	Number of observations to be sampled
pars	Parameter values for the density function to be evaluated with. length(pars) must be a multiple of npars.
tt	time grid on which the density function will be evaluated. Responses not in this time grid cannot appear.
pdfND	either a vector of length tt specifying the nondecision density for all condition-response pairs, or a matrix where columns corresponds to the nondecision densities of condition-response pairs. Supplying NULL implies no nondecision distribution.
fun.density	Density function to use.
args.density	Additional arguments to be passed to fun.density, aside from tt, pars, and a boundary argument ('upper' or 'lower')

npars	Number of parameters <code>fun.density</code> must be evaluated with. If <code>length(pars) &gt; npars</code> each <code>npars</code> values in <code>pars</code> will be seen as the parameter values of a condition.
return.pdf	Logical, if TRUE <code>genData</code> returns a list containing the probability density function used and the data, if FALSE <code>genData</code> returns a dataframe with simulated data.
normalizePdfs	Logical, should the pdf of the nondecision distribution be normalized?

### Details

Simulate data via multinomial sampling. The response options to sample from should be provided in `tt`. The number of conditions is defined as `length(pars) / npars`.

### Value

A sorted dataframe where rows represent trials. It contains: a column named `rt` containing reaction times in seconds, a column named `response` containing either response option `lower` or `upper`, and a column named `condition` indicating which condition a trials belongs to. If `return.pdf` is TRUE it returns a list where the first element is the sorted dataframe, the second through the fifth elements are lists that contain densities used for simulating data.

### Examples

```
tt = seq(0, 5, .01)
pdfND = dbeta(tt, 10, 30)
n = 100
pars = c(1, 2, .5, .5, .5)
dat = simData(n, pars, tt, pdfND)
head(dat)
```

---

testFun	<i>Test fun.density with lower and upper bounds</i>
---------	---

---

### Description

Test `fun.density` with lower and upper bounds

### Usage

```
testFun(fun.density, lower, upper, args = list())
```

### Arguments

<code>fun.density</code>	A density function to be evaluated.
<code>lower</code>	Lower bounds of the parameter space with which <code>fun.density</code> can be evaluated.
<code>upper</code>	Upper bounds of the parameter space with which <code>fun.density</code> can be evaluated.
<code>args</code>	Additional arguments for <code>fun.density</code> .

**Details**

A function that is called whenever a nondefault density function is passed to DstarM. It does some rough error checking.

**Value**

Returns TRUE if no errors occurred, otherwise returns an error message

**Examples**

```
lower = c(.5, -6, .1, 0, 0)
upper = c(2, 6, .99, .99, 10)
args = list(t = seq(0, 5, .01), pars = lower, boundary = 'lower',
DstarM = TRUE)
testFun(fun.density = Voss.density, lower = lower, upper = upper,
args = args)
# TRUE
```

---

upgradeDstarM

*Upgrade a DstarM object for backwards compatibility*

---

**Description**

Upgrade a DstarM object for backwards compatibility

**Usage**

```
upgradeDstarM(x)
```

**Arguments**

x                    an object of class D\*M or DstarM.

**Value**

An object of class DstarM.fitD, DstarM.fitND, or DstarM.fitObs.



---

Voss.density	<i>Calculate model density for a given set of parameters</i>
--------------	--

---

**Description**

Calculate model density for a given set of parameters

**Usage**

```
Voss.density(t, pars, boundary, DstarM = TRUE, prec = 3)
```

```
LBA.density(t, pars, boundary, DstarM = TRUE, ...)
```

```
Wiener.density(t, pars, boundary, DstarM)
```

**Arguments**

t	Time grid for density to be calculated on.
pars	Parameter vector where (if <code>DstarM == TRUE</code> ) the first index contains the boundary parameter, the second contains the drift speed, the third contains the relative starting point, the fourth contains a proportion of the maximum size of the variance on the relative starting point, the fifth contains the standard deviation of the drift speed. if <code>DstarM == FALSE</code> then third index of <code>pars</code> contains the <code>Ter</code> , the fifth the drift speed, the the sixth contains a proportion of the maximum size of the variance on the relative starting point, the fifth contains the standard deviation of the drift speed, and the seventh contains a proportion of the maximum variance of the <code>Ter</code> .
boundary	For which response option will the density be calculated? Either 'upper' or 'lower'.
DstarM	Logical, see <code>pars</code> .
prec	Precision with which the density is calculated. Corresponds roughly to the number of decimals accurately calculated.
...	Other arguments, see <a href="#">dLBA</a>

**Details**

These functions are examples of what `fun.density` should look like. `Voss.density` is an adaptation of [ddiffusion](#), `LBA.density` is an adaptation of [dLBA](#), and `wiener.density` is an adaptation of [dwiener](#). To improve speed one can remove error handling. Normally error handling is useful, however because differential evolution can result in an incredible number of function evaluations (more than 10.000) it is recommended to omit error handling in custom density functions. `estDstarM` will apply some internal error checks (see [testFun](#)) on the density functions before starting differential evolution. A version of `ddiffusion` without error handling can be found in the source code (commented out to pass R check). Note that for in `Voss.density` if `DstarM == FALSE` nondecision parameters are implemented manually and might differ from from how they are implemented in other packages. The parameter `t0` specifies the mean of a uniform distribution and `st0`

specifies the relative size of this uniform distribution. To obtain the lower and upper range of the uniform distribution calculate  $a = t_0 - t_0 \cdot st_0$ , and  $b = t_0 + t_0 \cdot st_0$ .

### Value

A numeric vector of length `length(t)` containing a density.

### Examples

```
t = seq(0, .75, .01)
V.pars = c(1, 2, .5, .5, .5)
L.pars = c(1, .5, 2, 1, 1, 1)
W.pars = V.pars[1:3]
V1 = Voss.density(t = t, pars = V.pars, boundary = 'upper', DstarM = TRUE)
V2 = Voss.density(t = t, pars = V.pars, boundary = 'lower', DstarM = TRUE)
L1 = LBA.density(t = t, pars = L.pars, boundary = 'upper', DstarM = TRUE)
L2 = LBA.density(t = t, pars = L.pars, boundary = 'lower', DstarM = TRUE)
W1 = Wiener.density(t = t, pars = W.pars, boundary = 'upper', DstarM = TRUE)
W2 = Wiener.density(t = t, pars = W.pars, boundary = 'lower', DstarM = TRUE)
densities = cbind(V1, V2, L1, L2, W1, W2)
matplot(t, densities, type = 'b', ylab = 'Density', lty = 1, las = 1, bty = 'n',
        col = rep(1:3, each = 2), pch = c(0, 15, 1, 16, 2, 17), cex = .8,
        main = 'Model densities')
legend('topright', legend = c('Voss', 'LBA', 'RWiener'), lty = 1,
      pch = 15:17, col = 1:3, bty = 'n')
```

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