

Package ‘ARCoKrig’

January 20, 2025

Type Package

Title Autoregressive Cokriging Models for Multifidelity Codes

Version 0.1.2

Date 2021-11-10

Maintainer Pulong Ma <mpulong@gmail.com>

Description

For emulating multifidelity computer models. The major methods include univariate autoregressive cokriging and multivariate autoregressive cokriging. The autoregressive cokriging methods are implemented for both hierarchically nested design and non-nested design. For hierarchically nested design, the model parameters are estimated via standard optimization algorithms; For non-nested design, the model parameters are estimated via Monte Carlo expectation-maximization (MCEM) algorithms. In both cases, the priors are chosen such that the posterior distributions are proper. Notice that the uniform priors on range parameters in the correlation function lead to improper posteriors. This should be avoided when Bayesian analysis is adopted. The development of objective priors for autoregressive cokriging models can be found in Pulong Ma (2020) <DOI:10.1137/19M1289893>. The development of the multivariate autoregressive cokriging models with possibly non-nested design can be found in Pulong Ma, Georgios Karagiannis, Bledar A Konomi, Taylor G Asher, Gabriel R Toro, and Andrew T Cox (2019) <arXiv:1909.01836>.

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Encoding UTF-8

URL <https://CRAN.R-project.org/package=ARCoKrig>

BugReports <https://github.com/pulongma/ARCoKrig/issues>

Depends R (>= 3.5.0)

Imports Rcpp, mvtnorm (>= 1.0-10), stats, methods, ggplot2

LinkingTo Rcpp, RcppArmadillo, RcppEigen

RoxygenNote 7.1.1

NeedsCompilation yes

Author Pulong Ma [aut, cre]

Repository CRAN

Date/Publication 2021-12-02 21:30:02 UTC

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ARCokrig

Fit the AR-Cokriging model and make predictions

Description

This is a simple and high-level function to fit autoregressive cokriging models to multifidelity computer model outputs.

Usage

```
ARCokrig(
  formula = list(~1, ~1),
  output,
  input,
  cov.model = "matern_5_2",
  nugget.est = FALSE,
  input.new,
  prior = list(),
  opt = list(),
  NestDesign = TRUE,
  tuning = list(),
  info = list()
)
```

Arguments

formula	a list of s elements, each of which contains the formula to specify fixed basis functions or regressors.
output	a list of s elements, each of which contains a matrix of computer model outputs.

<code>input</code>	a list of s elements, each of which contains a matrix of inputs.
<code>cov.model</code>	a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include <ul style="list-style-type: none"> exp product form of exponential covariance functions. matern_3_2 product form of Matern covariance functions with smoothness parameter $3/2$. matern_5_2 product form of Matern covariance functions with smoothness parameter $5/2$. Gaussian product form of Gaussian covariance functions. powexp product form of power-exponential covariance functions with roughness parameter fixed at 1.9.
<code>nugget.est</code>	a logical value indicating whether nugget parameter is included or not. Default value is FALSE.
<code>input.new</code>	a matrix including new inputs for making prediction
<code>prior</code>	a list of arguments to setup the prior distributions <ul style="list-style-type: none"> name the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys hyperparam hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: a refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; b refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; <code>nugget.UB</code> is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support $(0, 1)$.
<code>opt</code>	a list of arguments to setup the <code>optim</code> routine.
<code>NestDesign</code>	a logical value indicating whether the experimental design is hierarchically nested within each level of the code.
<code>tuning</code>	a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments <ul style="list-style-type: none"> maxit the maximum number of MCEM iterations. tol a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped. n.sample the number of Monte Carlo samples in the MCEM algorithm. verbose a logical value to show the MCEM iterations if it is true.
<code>info</code>	a list that contains <ul style="list-style-type: none"> iter number of iterations used in the MCEM algorithm eps parameter difference after the MCEM algorithm stops

Value

The main call inside `ARCokrig` consists of `cokm`, `cokm.fit`, and `cokm.predict`. Thus, the function returns the `cokm` object and predictions over new inputs.

Author(s)

Pulong Ma <mpulong@gmail.com>

References

- Ma, P. (2019). "Objective Bayesian Analysis of a Cokriging Model for Hierarchical Multifidelity Codes." arXiv:1910.10225. <https://arxiv.org/abs/1910.10225>.
- Ma, P., Karagiannis, G., Konomi, B., Asher, T., Toro, G., and Cox, A. (2019) "Multifidelity Computer Model Emulation with High-Dimensional Output: An Application to Storm Surge." arXiv:1909.01836. <https://arxiv.org/abs/1909.01836>.

See Also

[cokm](#), [cokm.param](#), [cokm.fit](#), [cokm.predict](#)

Examples

```
#####
#####
##### Example
Funcc = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Funcc(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

#####
##### Nested design
#####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Funcc(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## fit and predict with the AR-Cokriging model

out = ARCokrig(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
  input=list(as.matrix(Dc), as.matrix(Df)),
  cov.model="matern_5_2",
  input.new=input.new)

## plot results
```

```

library(ggplot2)
cokrig = out$cokrig
df.l1 = data.frame(x=c(Dc), y=c(zc))
df.l2 = data.frame(x=c(Df), y=c(zf))
CI.lower = cokrig$lower95[[2]]
CI.upper = cokrig$upper95[[2]]
df.CI = data.frame(x=c(input.new), lower=CI.lower, upper=CI.upper)
df.pred = data.frame(x=c(input.new), y=cokrig$mu[[2]])

g = ggplot(data.frame(x=c(-1,1)), aes(x)) +
  stat_function(fun=Func, geom="line", aes(colour="level 1"), n=500) +
  stat_function(fun=Funcf, geom="line", aes(colour="level 2"), n=500)

g = g + geom_point(data=df.l1, mapping=aes(x=x, y=y), shape=16, size=2, color="black") +
  geom_point(data=df.l2, mapping=aes(x=x, y=y), shape=17, size=2, color="black")

g = g + geom_line(data=df.pred, aes(x=x, y=y, colour="cokriging"), inherit.aes=FALSE) +
  geom_ribbon(data=df.CI, mapping=aes(x=x, ymin=lower, ymax=upper), fill="gray40",
            alpha=0.3, inherit.aes=FALSE)
g = g + scale_colour_manual(name=NULL, values=c("red", "blue", "turquoise3"),
                           breaks=c("cokriging", "level 1", "level 2"))

g = g + ggtitle("A Two-Level Example") +
  theme(plot.title=element_text(size=14),
        axis.title.x=element_text(size=14),
        axis.text.x=element_text(size=14),
        axis.title.y=element_text(size=14),
        axis.text.y=element_text(size=14),
        legend.text = element_text(size=12),
        legend.direction = "horizontal",
        legend.position = c(0.6, 0.1)) + xlab("") + ylab("")
print(g)

```

cokm

Construct the cokm object

Description

This function constructs the cokm object in autogressive cokriging models

Usage

```

cokm(
  formula = list(~1, ~1),
  output,

```

```

input,
cov.model = "matern_5_2",
nugget.est = FALSE,
prior = list(),
opt = list(),
NestDesign = TRUE,
tuning = list(),
info = list()
)

```

Arguments

formula	a list of s elements, each of which contains the formula to specify fixed basis functions or regressors.
output	a list of s elements, each of which contains a matrix of computer model outputs.
input	a list of s elements, each of which contains a matrix of inputs.
cov.model	a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include exp product form of exponential covariance functions. matern_3_2 product form of Matern covariance functions with smoothness parameter $3/2$. matern_5_2 product form of Matern covariance functions with smoothness parameter $5/2$. Gaussian product form of Gaussian covariance functions. powexp product form of power-exponential covariance functions with roughness parameter fixed at 1.9.
nugget.est	a logical value indicating whether the nugget is included or not. Default value is FALSE.
prior	a list of arguments to setup the prior distributions with the reference prior as default. name the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys hyperparam hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: a refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; b refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support $(0, 1)$.
opt	a list of arguments to setup the <code>optim</code> routine.
NestDesign	a logical value indicating whether the experimental design is hierarchically nested within each level of the code.
tuning	a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments maxit the maximum number of MCEM iterations.

tol a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped.

n.sample the number of Monte Carlo samples in the MCEM algorithm.

verbose a logical value to show the MCEM iterations if it is true.

info a list that contains

iter number of iterations used in the MCEM algorithm

eps parameter difference after the MCEM algorithm stops

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[ARCokrig](#), [cokm.fit](#), [cokm.predict](#)

cokm-class

cokm Class

Description

This is an S4 class definition for `cokm` in the `ARCokrig` package

Slots

output a list of s elements, each of which contains a matrix of computer model outputs.

input a list of s elements, each of which contains a matrix of inputs.

param a list of s elements, each of which contains a vector of initial values for correlation parameters (and nugget variance parameters if nugget terms are included in AR-cokriging models).

cov.model a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include

exp product form of exponential covariance functions.

matern_3_2 product form of Matern covariance functions with smoothness parameter $3/2$.

matern_5_2 product form of Matern covariance functions with smoothness parameter $5/2$.

Gaussian product form of Gaussian covariance functions.

powexp product form of power-exponential covariance functions with roughness parameter fixed at 1.9.

nugget.est a logical value indicating whether nugget parameter is included or not. Default value is FALSE.

prior a list of arguments to setup the prior distributions with the reference prior as default

name the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys

hyperparam hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: *a* refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; *b* refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support (0, 1).

opt a list of arguments to setup the `optim` routine.

NestDesign a logical value indicating whether the experimental design is hierarchically nested within each level of the code.

tuning a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments

maxit the maximum number of MCEM iterations.

tol a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped.

n.sample the number of Monte Carlo samples in the MCEM algorithm.

verbose a logical value to show the MCEM iterations if it is true.

info a list that contains

iter number of iterations used in the MCEM algorithm

eps parameter difference after the MCEM algorithm stops.

Author(s)

Pulong Ma <mpulong@gmail.com>

cokm.condsim

Conditional simulation at new inputs in the autoregressive cokriging model

Description

This function simulate from predictive distributions in autoregressive cokriging models

Usage

```
cokm.condsim(obj, input.new, nsample = 30)
```

Arguments

<code>obj</code>	a <code>cokm</code> object constructed via the function <code>cokm</code> in this package
<code>input.new</code>	a matrix including new inputs for making prediction
<code>nsample</code>	a numerical value indicating the number of samples

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[cokm](#), [cokm.fit](#), [cokm.predict](#), [ARCokrig](#)

Examples

```

Func = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Func(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

#####
##### Nested design
#####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Func(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## create the cokm object
prior = list(name="Reference")
obj = cokm(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
           input=list(as.matrix(Dc), as.matrix(Df)),
           prior=prior, cov.model="matern_5_2")

## update model parameters in the cokm object

obj = cokm.fit(obj)

cokrige = cokm.condsim(obj, input.new, nsample=30)

```

cokm.fit

fit the autoregressive cokriging model

Description

This function estimates parameters in autoregressive cokriging models

Usage

```
cokm.fit(obj)
```

Arguments

obj a `cokm` object constructed via the function `cokm` in this package

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[cokm](#), [cokm.param](#), [cokm.predict](#), [ARCoKrig](#)

Examples

```

Funccc = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Funccc(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

#####
##### Nested design
#####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Funccc(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## create the cokm object
prior = list(name="JR")
obj = cokm(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
           input=list(as.matrix(Dc), as.matrix(Df)),
           prior=prior, cov.model="matern_5_2")

## update model parameters in the cokm object

obj = cokm.fit(obj)

```

cokm.param	<i>Get model parameters in the autoregressive cokriging model</i>
------------	---

Description

This function compute estimates for regression and variance parameters given the correlation parameters are known. It is used to show all model parameters in one place.

Usage

```
cokm.param(obj)
```

Arguments

obj a `cokm` object constructed via the function `cokm` in this package

Value

a list of model parameters including regression coefficients β , scale discrepancy γ , variance parameters σ^2 , and correlation parameters ϕ in covariance functions. If nugget parameters are included in the model, then nugget parameters are shown in ϕ .

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[cokm](#), [cokm.fit](#), [cokm.condsim](#), [ARCoKrig](#)

cokm.predict	<i>Prediction at new inputs in the autoregressive cokriging model</i>
--------------	---

Description

This function makes prediction in autoregressive cokriging models. If a nested design is used, the predictive mean and predictive variance are computed exactly; otherwise, Monte Carlo simulation from the predictive distribution is used to approximate the predictive mean and predictive variance.

Usage

```
cokm.predict(obj, input.new)
```

Arguments

obj a `cokm` object constructed via the function `cokm` in this package
input.new a matrix including new inputs for making prediction

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[cokm](#), [cokm.fit](#), [cokm.condsim](#), [ARCokrig](#)

Examples

```

Func = function(x){
  return(0.5*(6*x-2)^2*sin(12*x-4)+10*(x-0.5)-5)
}

Funcf = function(x){
  z1 = Func(x)
  z2 = 2*z1-20*x+20 + sin(10*cos(5*x))
  return(z2)
}

#####
##### Nested design
#####
Dc <- seq(-1,1,0.1)
indDf <- c(1, 3, 6, 8, 10, 13, 17, 21)
zc <- Func(Dc)
Df <- Dc[indDf]
zf <- Funcf(Df)

input.new = as.matrix(seq(-1,1,length.out=200))

## create the cokm object
prior = list(name="Reference")
obj = cokm(formula=list(~1,~1+x1), output=list(c(zc), c(zf)),
           input=list(as.matrix(Dc), as.matrix(Df)),
           prior=prior, cov.model="matern_5_2")

## update model parameters in the cokm object

obj = cokm.fit(obj)

cokrige = cokm.predict(obj, input.new)

```

Description

This function compute the continous rank probability score for normal distributions. It is mainly used to evaluate the validity of predictive distributions.

Usage

```
CRPS(x, mu, sig)
```

Arguments

x	a vector of true values (held-out data)
mu	a vector of predictive means
sig	a vector of predictive standard deviations

Author(s)

Pulong Ma <mpulong@gmail.com>

mvcokm

Construct the mvcokm object

Description

This function constructs the mvcokm object in autogressive cokriging models for multivariate outputs. The model is known as the parallel partial (PP) cokriging emulator.

Usage

```
mvcokm(
  formula = list(~1, ~1),
  output,
  input,
  cov.model = "matern_5_2",
  nugget.est = FALSE,
  prior = list(),
  opt = list(),
  NestDesign = TRUE,
  tuning = list(),
  info = list()
)
```

Arguments

formula	a list of s elements, each of which contains the formula to specify fixed basis functions or regressors.
output	a list of s elements, each of which contains a matrix of computer model outputs.
input	a list of s elements, each of which contains a matrix of inputs.
cov.model	a string indicating the type of covariance function in the PP cokriging models. Current covariance functions include exp product form of exponential covariance functions. matern_3_2 product form of Matern covariance functions with smoothness parameter 3/2. matern_5_2 product form of Matern covariance functions with smoothness parameter 5/2. Gaussian product form of Gaussian covariance functions. powexp product form of power-exponential covariance functions with roughness parameter fixed at 1.9.
nugget.est	a logical value indicating whether the nugget is included or not. Default value is FALSE.
prior	a list of arguments to setup the prior distributions with the jointly robust prior as default name the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys hyperparam hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: a refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; b refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; nugget.UB is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support (0, 1).
opt	a list of arguments to setup the <code>optim</code> routine.
NestDesign	a logical value indicating whether the experimental design is hierarchically nested within each level of the code.
tuning	a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments maxit the maximum number of MCEM iterations. tol a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped. n.sample the number of Monte Carlo samples in the MCEM algorithm. verbose a logical value to show the MCEM iterations if it is true.
info	a list that contains iter number of iterations used in the MCEM algorithm eps parameter difference after the MCEM algorithm stops

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[ARCokrig](#), [mvcokm.fit](#), [mvcokm.predict](#), [mvcokm.condsim](#)

 mvcokm-class

mvcokm Class

Description

This is an S4 class definition for `mvcokm` in the `ARCokrig` package

Slots

`output` a list of s elements, each of which contains a matrix of computer model outputs.

`input` a list of s elements, each of which contains a matrix of inputs.

`param` a list of s elements, each of which contains a vector of initial values for correlation parameters (and nugget variance parameters if nugget terms are included in AR-cokriging models).

`cov.model` a string indicating the type of covariance function in AR-cokriging models. Current covariance functions include

exp product form of exponential covariance functions.

matern_3_2 product form of Matern covariance functions with smoothness parameter $3/2$.

matern_5_2 product form of Matern covariance functions with smoothness parameter $5/2$.

Gaussian product form of Gaussian covariance functions.

powexp product form of power-exponential covariance functions with roughness parameter fixed at 1.9.

aniso_exp anisotropic form of exponential covariance function.

aniso_matern_3_2 anisotropic form of Matern covariance functions with smoothness parameter $3/2$.

aniso_matern_5_2 anisotropic form of Matern covariance functions with smoothness parameter $5/2$.

`nugget.est` a logical value indicating whether the nugget is included or not. Default value is FALSE.

`prior` a list of arguments to setup the prior distributions with the jointly robust prior as default

name the name of the prior. Current implementation includes JR, Reference, Jeffreys, Ind_Jeffreys

hyperparam hyperparameters in the priors. For jointly robust (JR) prior, three parameters are included: a refers to the polynomial penalty to avoid singular correlation matrix with a default value 0.2; b refers to the exponential penalty to avoid diagonal correlation matrix with a default value 1; `nugget.UB` is the upper bound of the nugget variance with default value 1, which indicates that the nugget variance has support $(0, 1)$.

`opt` a list of arguments to setup the `optim` routine.

`NestDesign` a logical value indicating whether the experimental design is hierarchically nested within each level of the code.

`tuning` a list of arguments to control the MCEM algorithm for non-nested design. It includes the arguments

- maxit** the maximum number of MCEM iterations.
- tol** a tolerance to stop the MCEM algorithm. If the parameter difference between any two consecutive MCEM algorithm is less than this tolerance, the MCEM algorithm is stopped.
- n.sample** the number of Monte Carlo samples in the MCEM algorithm.

`info` a list that contains

- iter** number of iterations used in the MCEM algorithm
- eps** parameter difference after the MCEM algorithm stops

Author(s)

Pulong Ma <mpulong@gmail.com>

mvcokm.condsim *Conditional simulation at new inputs in autoregressive cokriging models for multivariate output*

Description

This function makes prediction based on conditional simulation in autoregressive cokriging models for multivariate output

Usage

```
mvcokm.condsim(obj, input.new, nsample = 30)
```

Arguments

<code>obj</code>	a <code>mvcokm</code> object constructed via the function <code>mvcokm</code> in this package
<code>input.new</code>	a matrix including new inputs for making prediction
<code>nsample</code>	a numerical value indicating the number of samples

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[mvcokm](#), [mvcokm.fit](#), [mvcokm.predict](#), [ARCoKrig](#)

mvcokm.fit	<i>fit the autoregressive cokriging model for multivariate output</i>
------------	---

Description

This function estimates parameters in the parallel partial cokriging model

Usage

```
mvcokm.fit(obj)
```

Arguments

obj a [mvcokm](#) object constructed via the function [mvcokm](#) in this package

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[mvcokm](#), [mvcokm.predict](#), [mvcokm.condsim](#), [ARCokrig](#)

mvcokm.param	<i>Get model parameters in autoregressive cokriging models for multivariate output</i>
--------------	--

Description

This function computes estimates for regression and variance parameters given the correlation parameters are known. It is used to show all model parameters in one place.

Usage

```
mvcokm.param(obj)
```

Arguments

obj a [mvcokm](#) object constructed via the function [mvcokm](#) in this package

Value

a list of model parameters including regression coefficients β , scale discrepancy γ , variance parameters σ^2 , and correlation parameters ϕ in covariance functions. If nugget parameters are included in the model, then nugget parameters are shown in ϕ .

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[mvcokm](#), [mvcokm.fit](#), [mvcokm.predict](#), [ARCokrig](#)

mvcokm.predict	<i>Prediction at new inputs in autoregressive cokriging models for multi-varite output</i>
----------------	--

Description

This function makes prediction in the parallel partial cokriging model. If a nested design is used, the predictive mean and predictive variance are computed exactly; otherwise, Monte Carlo simulation from the predictive distribution is used to approximate the predictive mean and predictive variance.

Usage

```
mvcokm.predict(obj, input.new)
```

Arguments

obj	a mvcokm object constructed via the function mvcokm in this package
input.new	a matrix including new inputs for making prediction

Author(s)

Pulong Ma <mpulong@gmail.com>

See Also

[mvcokm](#), [mvcokm.fit](#), [mvcokm.condsim](#), [ARCokrig](#)

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