

Package ‘HomomorphicEncryption’

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Title BFV, BGV, CKKS Schema for Fully Homomorphic Encryption

Version 0.9.0

Description Implements the Brakerski-Fan-Vercauteren (BFV, 2012) <<https://eprint.iacr.org/2012/144>>, Brakerski-Gentry-Vaikuntanathan (BGV, 2014) <[doi:10.1145/2633600](https://doi.org/10.1145/2633600)>, and Cheon-Kim-Kim-Song (CKKS, 2016) <<https://eprint.iacr.org/2016/421.pdf>> schema for Fully Homomorphic Encryption. The included vignettes demonstrate the encryption procedures.

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Encoding UTF-8

RoxygenNote 7.2.3

Depends polynom, stats, HEtools

Suggests covr, knitr, rmarkdown, testthat (>= 3.0.0)

VignetteBuilder knitr

Config/testthat/edition 3

NeedsCompilation no

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 BFV_encrypt

BFV encryption

Description

BFV encryption

Usage

BFV_encrypt(m, pk)

Arguments

| | |
|----|------------|
| m | message |
| pk | public key |

Value

polynomial

 BFV_KeyGen

Brakerski / Fan-Vercauteren

Description

Brakerski / Fan-Vercauteren

Usage

BFV_KeyGen(d = 4, q = 424242)

Arguments

| | |
|---|-------------|
| d | the d input |
| q | the q input |

Value

polynomial

Examples

```
d = 4
n = 2^d
p = (n/2)-1
q = 424242
GenPolyMod(n)
```

 compute_basis_coordinates

compute basis coordinates

Description

Compute basis coordinates

Usage

compute_basis_coordinates(sigma_R_basis, z)

Arguments

| | |
|---------------|---------------|
| sigma_R_basis | sigma_R_basis |
| z | z |

Value

basis coordinates

coordinate_wise_random_rounding
coordinate-wise random rounding

Description

Coordinate-wise random rounding

Usage

```
coordinate_wise_random_rounding(coordinates)
```

Arguments

coordinates coordinates

Value

rounded coordinates

decode *decode*

Description

Decode

Usage

```
decode(xi, M, scale, p)
```

Arguments

| | |
|-------|-------|
| xi | xi |
| M | M |
| scale | scale |
| p | p |

Value

decoded xi

encode *encode*

Description

Encode

Usage

encode(xi, M, scale, z)

Arguments

| | |
|-------|-------|
| xi | xi |
| M | M |
| scale | scale |
| z | z |

Value

encode polynomial

EncryptPoly0 *Encrypt Polynomial Message Part 0*

Description

Encrypt Polynomial Message Part 0

Usage

EncryptPoly0(m, pk0, u, e1, p, pm, q)

Arguments

| | |
|-----|-------------------|
| m | message |
| pk0 | public key part 0 |
| u | u |
| e1 | e1 |
| p | p |
| pm | pm |
| q | q |

Value

polynomial which contains the message in ciphertext

 EncryptPoly1

Encrypt Polynomial Message Part 1

Description

Encrypt Polynomial Message Part 1

Usage

EncryptPoly1(pk1, u, e2, pm, q)

Arguments

| | |
|-----|-------------------|
| pk1 | public key part 1 |
| u | u |
| e2 | e2 |
| pm | pm |
| q | q |

Value

polynomial which contains the message in ciphertext

GenA

Generate a

Description

Generate a

Usage

GenA(n, q)

Arguments

| | |
|---|-------------------------------|
| n | the order |
| q | the ciphermod of coefficients |

Value

polynomial of order x^n with coefficients 0,...,q

Examples

```
n = 16
q = 7
GenA(n, q)
```

| | |
|----------|-------------------|
| GenError | <i>Generate a</i> |
|----------|-------------------|

Description

Generate a

Usage

GenError(n)

Arguments

n the order

Value

polynomial of order x^n with discrete Gaussian distribution, bounded (not strictly true) by $-n, n$

Examples

n = 16
GenError(n)

| | |
|-------------|------------------------------------|
| GenEvalKey0 | <i>Generate the Evaluation Key</i> |
|-------------|------------------------------------|

Description

Generate the Evaluation Key

Usage

GenEvalKey0(a, s, e)

Arguments

| | |
|---|---|
| a | a |
| s | s |
| e | e |

Value

polynomial

GenPubKey *Generate the Public Key*

Description

Generate the Public Key

Usage

GenPubKey(a, n, e, pm, q)

Arguments

| | |
|----|----|
| a | a |
| n | n |
| e | e |
| pm | pm |
| q | q |

Value

list with the two polynomials that form the public key

GenPubKey0 *Generate part 0 of the Public Key*

Description

Generate part 0 of the Public Key

Usage

GenPubKey0(a, s, e, pm, q)

Arguments

| | |
|----|----|
| a | a |
| s | s |
| e | e |
| pm | pm |
| q | q |

Value

polynomial

GenPubKey1 *Generate part 1 of the Public Key*

Description

Generate part 1 of the Public Key

Usage

GenPubKey1(a)

Arguments

a a

Value

polynomial

GenSecretkey *Generate Secret key*

Description

Generate Secret key

Usage

GenSecretKey(n)

Arguments

n the order

Value

polynomial of order x^n with coefficients (-1,-,1)

Examples

n = 16
GenSecretKey(n)

 GenU

Generate u

Description

Generate u

Usage

GenU(n)

Arguments

n the order

Value

polynomial of order x^{n-1} with coefficients (-1,-,1)

Examples

```
n = 16
GenU
```

 pi_function

pi function

Description

Pi function

Usage

pi_function(M, z)

Arguments

M M
z z

Value

Pi of M

pi_inverse *pi inverse function*

Description

Pi inverse function

Usage

`pi_inverse(z)`

Arguments

`z` `z`

Value

inverse of `z`

round_coordinates *round coordinates*

Description

Round coordinates

Usage

`round_coordinates(coordinates)`

Arguments

`coordinates` `coordinates`

Value

rounded coordinates

| | |
|----------------|-----------------------|
| sigma_function | <i>sigma function</i> |
|----------------|-----------------------|

Description

Sigma

Usage

sigma_function(xi, M, p)

Arguments

| | |
|----|----|
| xi | xi |
| M | M |
| p | p |

Value

sigma of xi

| | |
|---------------|----------------------|
| sigma_inverse | <i>sigma inverse</i> |
|---------------|----------------------|

Description

Sigma inverse

Usage

sigma_inverse(xi, M, b)

Arguments

| | |
|----|----|
| xi | xi |
| M | M |
| b | b |

Value

sigma inverse of xi

sigma_R_discretization
sigma discretization

Description

Sigma discretization

Usage

sigma_R_discretization(xi, M, z)

Arguments

| | |
|----|----|
| xi | xi |
| M | M |
| z | z |

Value

sigma R discretization

vandermonde *vandermonde*

Description

Vandermonde

Usage

vandermonde(xi, M)

Arguments

| | |
|----|----|
| xi | xi |
| M | M |

Value

The Vandermonde matrix

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