## Package 'vglmer'

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Type Package

Title Variational Inference for Hierarchical Generalized Linear Models

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License GPL (>= 2)

Description Estimates hierarchical models using variational inference. At present, it can estimate logistic, linear, and negative binomial models. It can accommodate models with an arbitrary number of random effects and requires no integration to estimate. It also provides the ability to improve the quality of the approximation using marginal augmentation. Goplerud (2022) <doi:10.1214/21-BA1266> and Goplerud (2024) <doi:10.1017/S0003055423000035>

provide details on the variational algorithms.

**Imports** Rcpp (>= 1.0.1), lme4, CholWishart, mvtnorm, Matrix, stats, graphics, methods, lmtest, splines, mgcv

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Suggests SuperLearner, MASS, tictoc, testthat, gKRLS

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MAVB

Perform MAVB after fitting vglmer

## Description

Given a model estimated using vglmer, this function performs marginally augmented variational Bayes (MAVB) to improve the approximation quality.

#### Usage

MAVB(object, samples, verbose = FALSE, var\_px = Inf)

#### Arguments

object	Model fit using vglmer.
samples	Number of samples to draw.
verbose	Show progress in drawing samples.
var_px	Variance of working prior for marginal augmentation. Default (Inf) is a flat, improper, prior.

## Details

This function returns the improved estimates of the *parameters*. To use MAVB when generating predictions, one should use predict\_MAVB. At present, MAVB is only enabled for binomial models.

#### Value

This function returns a matrix with samples rows and columns for each fixed and random effect.

#### References

Goplerud, Max. 2022. "Fast and Accurate Estimation of Non-Nested Binomial Hierarchical Models Using Variational Inference." *Bayesian Analysis*. 17(2): 623-650.

posterior\_samples.vglmer

Draw samples from the variational distribution

#### Description

This function draws samples from the estimated variational distributions. If using MAVB to improve the quality of the approximating distribution, please use MAVB or predict\_MAVB.

#### Usage

```
posterior_samples.vglmer(object, samples, verbose = FALSE)
```

## Arguments

object	Model fit using vglmer.
samples	Number of samples to draw.
verbose	Show progress in drawing samples.

## Value

This function returns a matrix with samples rows and columns for each fixed and random effect.

sl_vglmer	SuperLearner with (Variational) Hierarchical Models
-----------	---

#### Description

These functions integrate vglmer (or glmer) into SuperLearner. Most of the arguments are standard for SuperLearner functions.

## Usage

```
SL.vglmer(
    Y,
    X,
    newX,
    formula,
    family,
    id,
    obsWeights,
    control = vglmer_control()
)
### S3 method for class 'SL.vglmer'
```

sl\_vglmer

```
predict(object, newdata, allow_missing_levels = TRUE, ...)
SL.glmer(Y, X, newX, formula, family, id, obsWeights, control = NULL)
## S3 method for class 'SL.glmer'
predict(object, newdata, allow.new.levels = TRUE, ...)
add_formula_SL(learner, env = parent.frame())
```

#### Arguments

Υ	From SuperLearner: The outcome in the training data set.	
Х	From SuperLearner: The predictor variables in the training data.	
newX	From SuperLearner: The predictor variables in validation data.	
formula	The formula used for estimation.	
family	From SuperLearner: Currently allows gaussian or binomial.	
id	From SuperLearner: Optional cluster identification variable. See SuperLearner for more details.	
obsWeights	From SuperLearner: Weights for each observation. Not permitted for SL.vglmer.	
control	Control object for estimating vglmer (e.g., vglmer_control) or [g]lmer.	
object	Used in predict for SL.glmer and SL.vglmer. A model estimated using either SL.vglmer or SL.glmer.	
newdata	Dataset to use for predictions.	
allow_missing_levels		
	Default (TRUE) allows prediction for levels not observed in the estimation data; the value of 0 (with no uncertainty) is used for the corresponding random effect. <b>Note:</b> This default differs from predict.vglmer.	
	Not used; included to maintain compatibility with existing methods.	
allow.new.levels		
	From 1me4: Allow levels in prediction that are not in the training data. Default is TRUE for SuperLearner.	
learner	Character name of model from SuperLearner. See "Details" for how this is used.	
env	Environment to assign model. See "Details" for how this is used.	

## Details

This documentation describes two types of function.

**Estimating Hierarchical Models in SuperLearner**: Two methods for estimating hierarchical models are provided one for variational methods (SL.vglmer) and one for non-variational methods (SL.glmer). The accompanying prediction functions are also provided.

**Formula with SuperLearner**: The vglmer package provides a way to estimate models that require or use a formula with SuperLearner. This allows for a design to be passed that contains variables that are *not* used in estimation. This can be used as follows (see "Examples").

#### vglmer

One calls the function add\_formula\_SL around the quoted name of a SuperLearner model, e.g. add\_formula\_SL(learner = "SL.knn"). This creates a new model and predict function with the suffix "\_f". This **requires** a formula to be provided for estimation.

With this in hand, "SL.knn\_f" can be passed to SuperLearner with the accompanying formula argument and thus one can compare models with different formula or design on the same ensemble. The env argument may need to be manually specified to ensure the created functions can be called by SuperLearner.

#### Value

The functions here return different types of output. SL.vglmer and SL.glmer return fitted models with the in-sample predictions as standard for SuperLearner. The predict methods return vectors of predicted values. add\_formula\_SL creates two objects in the environment (one for estimation model\_f and one for prediction predict.model\_f) used for SuperLearner.

#### Examples

```
set.seed(456)
```

```
if (requireNamespace('SuperLearner', quietly = TRUE)){
require(SuperLearner)
sim_data <- data.frame(</pre>
 x = rnorm(100),
 g = sample(letters, 100, replace = TRUE)
)
sim_data$y <- rbinom(nrow(sim_data),</pre>
 1, plogis(runif(26)[match(sim_data$g, letters)]))
sim_data$g <- factor(sim_data$g)</pre>
sl_vglmer <- function(...){SL.vglmer(..., formula = y ~ x + (1 | g))}
SL.glm <- SuperLearner::SL.glm
add_formula_SL('SL.glm')
sl_glm_form <- function(...){SL.glm_f(..., formula = ~ x)}</pre>
   SuperLearner::SuperLearner(
    Y = sim_data$y, family = 'binomial',
     X = sim_data[, c('x', 'g')],
     cvControl = list(V = 2),
     SL.library = c('sl_vglmer', 'sl_glm_form')
   )
}
```

vglmer

Variational Inference for Hierarchical Generalized Linear Models

#### Description

This function estimates hierarchical models using mean-field variational inference. vglmer accepts standard syntax used for lme4, e.g.,  $y \sim x + (x \mid g)$ . Options are described below. Goplerud (2022; 2024) provides details on the variational algorithms.

#### Usage

vglmer(formula, data, family, control = vglmer\_control())

#### Arguments

formula	lme4 style-formula for random effects. Typically, $(1 + z   g)$ indicates a random effect for each level of variable "g" with a differing slope for the effect of variable "z" and an intercept (1); see "Details" for further discussion and how to incorporate splines.
data	data.frame containing the outcome and predictors.
family	Options are "binomial", "linear", or "negbin" (experimental). If "binomial", outcome must be either binary ( $\{0,1\}$ ) or cbind(success, failure) as per standard glm(er) syntax. Non-integer values are permitted for binomial if force_whole is set to FALSE in vglmer_control.
control	Adjust internal options for estimation. Must use an object created by vglmer_control.

#### Details

**Estimation Syntax:** The formula argument takes syntax designed to be a similar as possible to lme4. That is, one can specify models using  $y \sim x + (1 \mid g)$  where  $(1 \mid g)$  indicates a random intercept. While not tested extensively, terms of  $(1 \mid g / f)$  should work as expected. Terms of  $(1 + x \mid \mid g)$  may work, although will raise a warning about duplicated names of random effects.  $(1 + x \mid \mid g)$  terms may not work with spline estimation. To get around this, one can might copy the column g to g\_copy and then write  $(1 \mid g) + (0 + x \mid g_copy)$ .

**Splines:** Splines can be added using the term  $v_s(x)$  for a spline on the variable x. These are transformed into hierarchical terms in a standard fashion (e.g. Ruppert et al. 2003) and then estimated using the variational algorithms. At the present, only truncated linear functions (type = "tpf"; the default) and O'Sullivan splines (Wand and Ormerod 2008) are included. The options are described in more detail at  $v_s$ .

It is possible to have the spline vary across some categorical predictor by specifying the "by" argument such as  $v_s(x, by = g)$ . In effect, this adds additional hierarchical terms for the group-level deviations from the "global" spline. *Note:* In contrast to the typical presentation of these splines interacted with categorical variables (e.g., Ruppert et al. 2003), the default use of "by" includes the lower order interactions that are regularized, i.e. (1 + x | g), versus their unregularized version (e.g., x \* g); this can be changed using the by\_re argument described in v\_s. Further, all group-level deviations from the global spline share the same smoothing parameter (same prior distribution).

**Default Settings:** By default, the model is estimated using the "strong" (i.e. fully factorized) variational assumption. Setting vglmer\_control(factorization\_method = "weak") will improve the quality of the variance approximation but may take considerably more time to estimate. See Goplerud (2022) for discussion.

By default, the prior on each random effect variance  $(\Sigma_j)$  uses a Huang-Wand prior (Huang and Wand 2013) with hyper-parameters  $\nu_j = 2$  and  $A_{j,k} = 5$ . This is designed to be proper but weakly informative. Other options are discussed in vglmer\_control under the prior\_variance argument.

By default, estimation is accelerated using SQUAREM (Varadhan and Roland 2008) and (onestep-late) parameter expansion for variational Bayes. Under the default "strong" factorization, a

#### vglmer

"translation" expansion is used; under other factorizations a "mean" expansion is used. These can be adjusted using vglmer\_control. See Goplerud (2024) for more discussion of these methods.

#### Value

This returns an object of class vglmer. The available methods (e.g. coef) can be found using methods(class="vglmer").

- **beta** Contains the estimated distribution of the fixed effects ( $\beta$ ). It is multivariate normal. mean contains the means; var contains the variance matrix; decomp\_var contains a matrix L such that  $L^T L$  equals the full variance matrix.
- **alpha** Contains the estimated distribution of the random effects ( $\alpha$ ). They are all multivariate normal. mean contains the means; dia.var contains the variance of each random effect. var contains the variance matrix of each random effect (j,g). decomp\_var contains a matrix L such that  $L^T L$  equals the full variance of the entire set of random effects.
- **joint** If factorization\_method="weak", this is a list with one element (decomp\_var) that contains a matrix L such that  $L^T L$  equals the full variance matrix between the fixed and random effects  $q(\beta, \alpha)$ . The marginal variances are included in beta and alpha. If the factorization method is not "weak", this is NULL.
- **sigma** Contains the estimated distribution of each random effect covariance  $\Sigma_j$ ; all distributions are Inverse-Wishart. cov contains a list of the estimated scale matrices. df contains a list of the degrees of freedom.
- **hw** If a Huang-Wand prior is used (see Huang and Wand 2013 or Goplerud 2024 for more details), then the estimated distribution. Otherwise, it is NULL. All distributions are Inverse-Gamma. a contains a list of the scale parameters. b contains a list of the shape parameters.
- sigmasq If family="linear", this contains a list of the estimated parameters for  $\sigma^2$ ; its distribution is Inverse-Gamma. a contains the scale parameter; b contains the shape parameter.
- **ln\_r** If family="negbin", this contains the variational parameters for the log dispersion parameter  $\ln(r)$ . mu contains the mean; sigma contains the variance.
- family Family of outcome.
- **ELBO** Contains the ELBO at the termination of the algorithm.
- **ELBO\_trajectory** data.frame tracking the ELBO per iteration.
- control Contains the control parameters from vglmer\_control used in estimation.
- internal\_parameters Variety of internal parameters used in post-estimation functions.
- **formula** Contains the formula used for estimation; contains the original formula, fixed effects, and random effects parts separately for post-estimation functions. See formula.vglmer for more details.

#### References

Goplerud, Max. 2022. "Fast and Accurate Estimation of Non-Nested Binomial Hierarchical Models Using Variational Inference." *Bayesian Analysis*. 17(2): 623-650.

Goplerud, Max. 2024. "Re-Evaluating Machine Learning for MRP Given the Comparable Performance of (Deep) Hierarchical Models." *American Political Science Review*. 118(1): 529-536.

Huang, Alan, and Matthew P. Wand. 2013. "Simple Marginally Noninformative Prior Distributions for Covariance Matrices." *Bayesian Analysis*. 8(2):439-452.

Ruppert, David, Matt P. Wand, and Raymond J. Carroll. 2003. *Semiparametric Regression*. Cambridge University Press.

Varadhan, Ravi, and Christophe Roland. 2008. "Simple and Globally Convergent Methods for Accelerating the Convergence of any EM Algorithm." *Scandinavian Journal of Statistics*. 35(2): 335-353.

Wand, Matt P. and Ormerod, John T. 2008. "On Semiparametric Regression with O'Sullivan Penalized Splines". *Australian & New Zealand Journal of Statistics*. 50(2): 179-198.

#### Examples

```
set.seed(234)
sim_data <- data.frame(</pre>
 x = rnorm(100),
 y = rbinom(100, 1, 0.5),
 g = sample(letters, 100, replace = TRUE)
)
# Run with defaults
est_vglmer <- vglmer(y ~ x + (x | g), data = sim_data, family = "binomial")</pre>
# Simple prediction
predict(est_vglmer, newdata = sim_data)
# Summarize results
summary(est_vglmer)
# Extract parameters
coef(est_vglmer); vcov(est_vglmer)
# Comparability with lme4,
# although ranef is formatted differently.
ranef(est_vglmer); fixef(est_vglmer)
# Run with weaker (i.e. better) approximation
vglmer(y \sim x + (x \mid g)),
 data = sim_data,
 control = vglmer_control(factorization_method = "weak"),
 family = "binomial")
```

```
# Use a spline on x with a linear outcome
vglmer(y ~ v_s(x),
    data = sim_data,
    family = "linear")
```

vglmer-class

## Description

vglmer uses many standard methods from 1m and 1me4 with limited changes. These provide summaries of the estimated variational distributions.

#### Usage

```
## S3 method for class 'vglmer'
fixef(object, ...)
## S3 method for class 'vglmer'
sigma(object, ...)
## S3 method for class 'vglmer'
ranef(object, ...)
## S3 method for class 'vglmer'
coef(object, ...)
## S3 method for class 'vglmer'
vcov(object, ...)
## S3 method for class 'vglmer'
fitted(object, ...)
## S3 method for class 'vglmer'
print(x, ...)
## S3 method for class 'vglmer'
summary(object, display_re = TRUE, ...)
## S3 method for class 'vglmer'
formula(x, form = "original", ...)
format_vglmer(object)
format_glmer(object)
```

ELBO(object, type = c("final", "trajectory"))

#### Arguments

object	Model fit using vglmer.
	Not used; included to maintain compatibility with existing methods.

х	Model fit using vglmer.
display_re	Default (TRUE) prints a summary of the random effects alongside the fixed effects.
form	Describes the type of formula to report: "original" returns the user input, "fe" returns the fixed effects only, "re" returns the random effects only.
type	Default ("final") gives the ELBO at convergence. "trajectory" gives the ELBO estimated at each iteration. This is used to assess model convergence.

#### Details

The accompanying functions are briefly described below.

coef and vcov return the mean and variance of the fixed effects ( $\beta$ ). fixef returns the mean of the fixed effects.

ranef extracts the random effects ( $\alpha$ ) in a similar, although slightly different format, to lme4. It includes the estimated posterior mean and variance in a list of data.frames with one entry per random effect *j*.

fitted extracts the estimated expected *linear predictor*, i.e.  $E_{q(\theta)}[x_i^T\beta + z_i^T\alpha]$  at convergence.

summary reports the estimates for all fixed effects as in 1m as well as some summaries of the random effects (if display\_re=TRUE).

format\_vglmer collects the mean and variance of the fixed and random effects into a single data.frame. This is useful for examining all of the posterior estimates simultaneously. format\_glmer converts an object estimated with [g]lmer into a comparable format.

ELBO extracts the ELBO from the estimated model. type can be set equal to "trajectory" to get the estimated ELBO at each iteration and assess convergence.

sigma extracts the square root of the posterior mode of  $q(\sigma^2)$  if a linear model is used.

formula extracts the formula associated with the vglmer object. By default, it returns the formula provided. The fixed and random effects portions can be extracted separately using the form argument.

#### Value

The functions here return a variety of different objects depending on the specific function. "Details" describes the behavior of each one. Their output is similar to the typical behavior for the corresponding generic functions.

vglmer\_control Control for vglmer estimation

#### Description

This function controls various estimation options for vglmer.

#### vglmer\_control

#### Usage

```
vglmer_control(
  iterations = 1000,
  prior_variance = "hw",
  factorization_method = c("strong", "partial", "weak"),
  parameter_expansion = "translation",
  do_SQUAREM = TRUE,
  tolerance_elbo = 1e-08,
  tolerance_parameters = 1e-05,
  force_whole = TRUE,
  print_prog = NULL,
  do_timing = FALSE,
  verbose_time = FALSE,
  return_data = FALSE,
  linpred_method = "joint",
  vi_r_method = "VEM",
  verify_columns = FALSE,
  debug_param = FALSE,
  debug_ELB0 = FALSE,
  debug_px = FALSE,
  quiet = TRUE,
  quiet_rho = TRUE,
  px_method = "dynamic",
  px_numerical_it = 10,
  hw_inner = 10,
  init = "EM_FE"
)
```

#### Arguments

iterations Default of 1000; this sets the maximum number of iterations used in estimation.

- prior\_variance Prior distribution on the random effect variance  $\Sigma_j$ . Options are hw, jeffreys, mean\_exists, uniform, and gamma. The default (hw) is the Huang-Wand (2013) prior whose hyper-parameters are  $\nu_j = 2$  and  $A_{j,k} = 5$ . Otherwise, the prior is an Inverse Wishart with the following parameters where  $d_j$  is the dimensionality of the random effect j.
  - mean\_exists:  $IW(d_j + 1, I)$
  - jeffreys: IW(0,0)
  - uniform:  $IW(-[d_i + 1], 0)$
  - limit:  $IW(d_i 1, 0)$

Estimation may fail if an improper prior (jeffreys, uniform, limit) is used.

#### factorization\_method

Factorization assumption for the variational approximation. Default of "strong", i.e. a fully factorized model. Described in detail in Goplerud (2022). "strong", "partial", and "weak" correspond to Schemes I, II, and III respectively in that paper.

#### parameter\_expansion

Default of "translation" (see Goplerud 2022b). Valid options are "translation", "mean", or "none". "mean" should be employed if "translation" is not enabled or is too computationally expensive. For negative binomial estimation or any estimation where factorization\_method != "strong", only "mean" and "none" are available.

- do\_SQUAREM Default (TRUE) accelerates estimation using SQUAREM (Varadhan and Roland 2008).
- tolerance\_elbo Default (1e-8) sets a convergence threshold if the change in the ELBO is below the tolerance.

tolerance\_parameters

Default (1e-5) sets a convergence threshold that is achieved if no parameter changes by more than the tolerance from the prior estimated value.

- force\_whole Default (TRUE) requires integers for observed outcome for binomial or count models. FALSE allows for fractional responses.
- print\_prog Default (NULL) prints a "." to indicate once 5% of the total iterations have elapsed. Set to a positive integer int to print a "." every int iterations.
- do\_timing Default (FALSE) does not estimate timing of each variational update; TRUE requires the package tictoc.
- verbose\_time Default (FALSE) does not print the time elapsed for each parameter update. Set to TRUE, in conjunction with do\_timing=TRUE, to see the time taken for each parameter update.
- return\_data Default (FALSE) does not return the original design. Set to TRUE to debug convergence issues.
- linpred\_method Default ("joint") updates the mean parameters for the fixed and random effects simultaneously. This can improve the speed of estimation but may be costly for large datasets; use "cyclical" to update each parameter block separately.
- vi\_r\_method Default ("VEM") uses a variational EM algorithm for updating r if family="negbin". This assumes a point mass distribution on r. A number can be provided to fix r. These are the only available options.
- verify\_columns Default (FALSE) **does not** verify that all columns are drawn from the data.frame itself versus the environment. Set to TRUE to debug potential issues.
- debug\_param Default (FALSE) does not store parameters before the final iteration. Set to TRUE to debug convergence issues.
- debug\_ELB0 Default (FALSE) does not store the ELBO after each parameter update. Set to TRUE to debug convergence issues.
- debug\_px Default (FALSE) does not store information about whether parameter expansion worked. Set to TRUE to convergence issues.
- quiet Default (FALSE) does not print intermediate output about convergence. Set to TRUE to debug.
- quiet\_rho Default (FALSE) does not print information about parameter expansions. Set to TRUE to debug convergence issues.

px_method	When code parameter_expansion="translation", default ("dynamic") tries a one-step late update and, if this fails, a numerical improvement by L-BFGS- B. For an Inverse-Wishart prior on $\Sigma_j$ , this is set to "osl" that only attempts a one-step-late update.
<pre>px_numerical_it</pre>	
	Default of 10; if L-BFGS_B is needed for a parameter expansion, this sets the number of steps used.
hw_inner	If prior_variance="hw", this sets the number of repeated iterations between estimating $\Sigma_j$ and $a_{j,k}$ variational distributions at each iteration. A larger num- ber approximates jointly updating both parameters. Default (10) typically per- forms well.
init	Default ("EM_FE") initializes the mean variational parameters for $q(\beta, \alpha)$ by setting the random effects to zero and estimating the fixed effects using a short-running EM algorithm. "EM" initializes the model with a ridge regression with a guess as to the random effect variance. "random" initializes the means randomly. "zero" initializes them at zero.

#### Value

This function returns a named list with class vglmer\_control. It is passed to vglmer in the argument control. This argument only accepts objects created using vglmer\_control.

#### References

Goplerud, Max. 2022. "Fast and Accurate Estimation of Non-Nested Binomial Hierarchical Models Using Variational Inference." *Bayesian Analysis*. 17(2): 623-650.

Goplerud, Max. 2024. "Re-Evaluating Machine Learning for MRP Given the Comparable Performance of (Deep) Hierarchical Models." *American Political Science Review*. 118(1): 529-536.

Huang, Alan, and Matthew P. Wand. 2013. "Simple Marginally Noninformative Prior Distributions for Covariance Matrices." *Bayesian Analysis*. 8(2):439-452.

Varadhan, Ravi, and Christophe Roland. 2008. "Simple and Globally Convergent Methods for Accelerating the Convergence of any EM Algorithm." *Scandinavian Journal of Statistics*. 35(2): 335-353.

vglmer\_predict Predict after vglmer

#### Description

These functions calculate the estimated linear predictor using the variational distributions. predict.vglmer draws predictions using the estimated variational distributions; predict\_MAVB does so using the MAVB procedure described in Goplerud (2022).

## Usage

```
## S3 method for class 'vglmer'
predict(
 object,
 newdata,
type = "link",
  samples = 0,
  samples_only = FALSE,
  summary = TRUE,
 allow_missing_levels = FALSE,
  . . .
)
predict_MAVB(
 object,
 newdata,
  samples = 0,
  samples_only = FALSE,
 var_px = Inf,
 summary = TRUE,
 allow_missing_levels = FALSE
)
```

## Arguments

object	Model fit using vglmer.		
newdata	Dataset to use for predictions. It cannot be missing.		
type	Default ("link") returns the linear predictor; "terms" returns the predicted value for each random effect (or spline) separately as well as one that collects all fixed effects. At the moment, other options are not enabled.		
samples	Number of samples to draw. Using $0$ (default) gives the expectation of the linear predictor. A positive integer draws samples samples from the variational distributions and calculates the linear predictor.		
samples_only	Default (FALSE) returns the samples from the variational distributions, <b>not</b> the prediction. Each row is a sample and each column is a parameter.		
summary	Default (TRUE) returns the mean and variance of the samples for each observa- tion. FALSE returns a matrix of the sampled linear predictor for each observation. Each row is a sample and each column is an observation.		
allow_missing_levels			
	Default (FALSE) does not allow prediction for levels not observed in the original data. TRUE allows for prediction on unseen levels; the value of $0$ (with no uncertainty) is used for the corresponding random effect.		
	Not used; included to maintain compatibility with existing methods.		
var_px	Variance of working prior for marginal augmentation. Default (Inf) is a flat, improper, prior.		

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 $V\_S$ 

Value

This function returns an estimate of the linear predictor. The default returns the expected mean, i.e.  $E_{q(\alpha,\beta)}[x_i^T\beta + z_i^T\alpha]$ . If samples > 0, these functions return a summary of the prediction for each observation, i.e. the estimated mean and variance. If summary = FALSE, the sampled values of the linear predictor are returned as a matrix. predict\_MAVB performs MAVB as described in Goplerud (2022) before returning the linear predictor.

If allow\_missing\_levels = TRUE, then observations with a new (unseen) level for the random effect are given a value of zero for that term of the prediction.

#### Examples

```
set.seed(123)
sim_data <- data.frame(</pre>
 x = rnorm(100),
 y = rbinom(100, 1, 0.5),
 g = sample(letters, 100, replace = TRUE)
)
# Run with defaults
est_vglmer <- vglmer(y ~ x + (x | g), data = sim_data, family = "binomial")
# Simple prediction
predict(est_vglmer, newdata = sim_data)
# Return 10 posterior draws of the linear predictor for each observation.
predict_MAVB(est_vglmer, newdata = sim_data, summary = FALSE, samples = 10)
# Predict with a new level; note this would fail if
# allow_missing_levels = FALSE (the default)
predict(est_vglmer,
 newdata = data.frame(g = "AB", x = 0),
 allow_missing_levels = TRUE
)
```

v\_s

Create splines for use in vglmer

#### Description

This function estimates splines in vglmer, similar to s(...) in mgcv albeit with many fewer options than mgcv. It allows for truncated (linear) splines (type="tpf"), O'Sullivan splines (type="o"), or kernel ridge regression (type="gKRLS"). Please see vglmer for more discussion and examples. For information on kernel ridge regression, please consult gKRLS.

#### Usage

v\_s( ..., type = "tpf", knots = NULL,

```
by = NA,
xt = NULL,
by_re = TRUE,
force_vector = FALSE,
outer_okay = FALSE
)
```

#### Arguments

	Variable name, e.g. v_s(x)
type	Default ("tpf") uses truncated linear splines for the basis. "o" uses O'Sullivan splines (Wand and Ormerod 2008). Smoothing across multiple covariates, e.g. $v_s(x,x^2,type="gKRLS")$ , can be done using kernel ridge regression. Chang and Goplerud (2024) provide a detailed discussion. Note that "gKRLS" by default uses random sketching to create the relevant bases and thus a seed would need to be set to ensure exact replicability.
knots	Default (NULL) uses $K = min(N/4, 35)$ knots evenly spaced at quantiles of the covariate x. A single number specifies a specific number of knots; a vector can set custom locations for knots.
by	A categorical or factor covariate to interact the spline with; for example, $v_s(x, by = g)$ .
xt	Arguments passed to xt from mgcv; at the moment, this is only used for type="gKRLS" to pass the function gKRLS(). Please see the documentation of gKRLS for more details.
by_re	Default (TRUE) regularizes the interactions between the categorical factor and the covariate. See "Details" in vglmer for more discussion.
force_vector	Force that argument to knots is treated as vector. This is usually not needed unless knots is a single integer that should be treated as a single knot (vs. the number of knots).
outer_okay	Default (FALSE) does not permit values in x to exceed the outer knots.

#### Value

This function returns a list of class of vglmer\_spline that is passed to unexported functions. It contains the arguments noted above where ... is parsed into an argument called term.

## References

Chang, Qing, and Max Goplerud. 2024. "Generalized Kernel Regularized Least Squares." *Political Analysis* 32(2):157-171.

Wand, Matt P. and Ormerod, John T. 2008. "On Semiparametric Regression with O'Sullivan Penalized Splines". *Australian & New Zealand Journal of Statistics*. 50(2): 179-198.

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